## Data Management－exam of 08／06／2023（A）

## Problem 1

Let $R(A, B, C)$（with 26.000 pages）and $Q(D, E, F)$（with 10.000 pages）be two relations stored in a heap at processor $P_{0}$ ．We know that 200 free buffer frames are available at $P_{0}$ and that 100 tuples of each relation fit in one page．Also，we know that attribute $C$ of $R$ contains 500 values uniformly distributed in the tuples of the relation，and the same holds for attribute D of Q．Finally，we know that there are 10 processors $P_{1}, \ldots, P_{10}$ that we can use for processing queries，each with 80 free frames available．Consider the query that computes the equi－join between R and Q on the condition $\mathrm{C}=\mathrm{D}$ ，and compare the following two cases：
1．1 The query is executed at processor $P_{0}$ ．
1．2 The query is executed in parallel after sending the tuples of the two relations to processors $P_{1}, \ldots, P_{10}$ ． For each of the above cases，illustrate the algorithm you would use and discuss its cost in terms of number of page accesses（case 1．1）and elapsed time（case 1．2）．

## Problem 2

Consider the following schedule $S$ ：
$B_{1} w_{1}(A) B_{2} w_{2}(D) B_{3} w_{3}(E) c_{3} B_{4} r_{4}(E) r_{4}(D) w_{4}(C) B_{5} r_{5}(C) c_{4} w_{5}(C) w_{1}(D) c_{1} w_{2}(A) c_{2} c_{5}$
where the action $B_{i}$ means＂begin transaction $T_{i}$＂，the initial value of every item $A, C, D, E$ is 100 and every write action increases the value of the element on which it operates by 100 ．Suppose that $S$ is executed by PostgreSQL，and describe what happens when the scheduler analyzes each action（illustrating also which are the values read and written by all the＂read＂and＂write＂actions）in both the following two cases：（1）all the transactions are defined with the isolation level＂read committed＂；（2）all the transactions are defined with the isolation level＂repeatable read＂．

## Problem 3

Answer the following two questions，providing a suitable motivation for each answer．
3．1 Give an example of three transactions，which obey 2PL and have the following properties：$(i)$ there exists a schedule $S$ on the three transactions such that when $S$ is given in input to a 2 PL scheduler， a deadlock occurs；（ii）for each pair of the three transactions and for any schedule $S$ on such pair，no deadlock occurs when $S$ is given in input to a 2 PL scheduler．
3．2 Try to generalize the above example to the case of $n$ transactions．More precisely，try to come up with an example of $n$ transactions，which obey 2PL and have the following properties：（i）There exists a schedule $S$ on the $n$ transactions such that when $S$ is given in input to a 2PL scheduler，a deadlock occurs．（ii）For each $n-1$ transactions of the $n$ chosen transactions and for any schedule $S$ on such $n-1$ transactions，no deadlock occurs when $S$ is given in input to a 2 PL scheduler．

## Problem 4

Let Person（id，age）be a relation with 500 pages stored in a file sorted on 〈id，age〉，City（name，region） a relation with 200 pages sorted on 〈name，region〉 and Visited（id，age，name，region）a relation with 20.000 pages sorted on 〈id，age，name，region〉．With the goal of knowing，for each person，the cities that （s）he has not visited，we want to compute the set difference between the cartesian product of Person and City and the relation Visited．Tell which is the best algorithm that a query engine with 206 free buffer frames should use for this task，indicating also the cost of executing such algorithm．
Problem 5 （only for students enrolled in an A．Y．before 2021／22 who do not do the project）
Consider a database $B$ about high schools，where：$(i)$ for each student we are interested in the id，the age， the sex，the city of birth，the family（s）he is living with，and the school where（s）he has been enrolled in the various years，with the decades of the years；（ii）for each school we are interested in the type（classical， scientific，technical，etc．）and the city where the school is located；（iii）for each city we are interested in the province，the region and the number of inhabitants；（iv）for each family we are interested in the level of the income and the number of members．We want to build a data warehouse on all the above data for various analyses on student enrollments in the last 30 years．You are asked to show（1）the ER schema of the database $B,(2)$ the DFM schema of the data warehouse，（3）the corresponding star schema（optionally， with the queries used to populate the star schema tables），and（4）based on such tables，the SQL query that computes the number of students，for each province of the school where they are enrolled，for each region of the city of residence of the students，and for each level of the income of the family of the students．

