Problem 1 Let \mathcal{T}_2 be the class of schedules that are defined on two transactions, and that are accepted by the timestamp-based scheduler. Prove or disprove the following two statements:

- 1. \mathcal{T}_2 coincides with the class of conflict-serializable schedules defined on two transactions.
- 2. \mathcal{T}_2 coincides with the class of strict schedules defined on two transactions.

Problem 2 By referring to the following schedule S:

 $r_1(x) r_1(y) w_2(z) w_1(x) c_1 w_2(x) c_2 r_3(x) w_4(x) w_5(y) c_5 w_3(y) c_3 w_4(y) c_4$

you are asked to:

- 2.1 Illustrate the various steps carried out by the timestamp-based scheduler when analyzing S, assuming that, initially, $rts(\alpha) = wts(\alpha) = wts-c(\alpha) = cb(\alpha) = true$ for each element α of the database, and assuming that the timestamp of each transaction T_i is *i*.
- 2.2 Tell whether S is conflict serializable.
- 2.3 Tell whether S is in 2PL with shared and exclusive locks.

Problem 3 Suppose that there are 3 available frames in the buffer, and that relations R and S (possibly with duplicates) are stored in memory sorted according to all the attributes. Under these conditions, is it possible to compute the bag difference between R and S in one pass? If the answer is positive, then describe the algorithm you would choose. If the answer is negative, then explain the answer in detail.

Problem 4 Consider the relations R(A,B,D,E) and S(C,F,G,H,L,M), and the query: select R.A, R.B, S.C, S.F from R, S where R.B >= 50 and R.A = S.C

We know that R has 5.000.000 tuples, S has 150.000 tuples, each page contains 100 tuples of S, all values and pointers occupy the same space, and the number of available frames is 510.

- 4.1 Describe the logical query plan associated to the query code, and illustrate both the logical and the physical query plan you would select, motivating the choices.
- 4.2 Tell which is the cost (in terms of number of page accesses) of executing the query according to the selected physical query plan.

Problem 5 Consider the relations R(A,B,C,D,E,F) and S(G,H,L,M), where A,B is the primary key of R, and G is the primary key of S. We know that R is stored in 400.000 pages, S is stored in 200.000 pages, both relations have a B⁺-tree index with the primary key as search key, all values and pointers occupy the same space, and the number of available frames is 50. Consider the query:

select R.B, S.G
from R join S on R.A = S.G
where B >100

- 5.1 Describe the logical query plan associated to the query code, and illustrate both the logical and the physical query plan you would select, motivating the choices.
- 5.2 Tell which is the cost (in terms of number of page accesses) of executing the query according to the selected physical query plan.