

# Automatic Composition of e-Services <sup>\*</sup>

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**Abstract.** The main focus of this paper is on automatic *e-Service* composition. We start by developing a framework in which the exported behavior of an *e-Service* is described in terms of its possible executions (execution trees). Then we specialize the framework to the case in which such exported behavior (i.e., the execution tree of the *e-Service*) is represented by a finite state machine. In this specific setting, we analyze the complexity of synthesizing a composition, and develop sound and complete algorithms to check the existence of a composition and to return one such a composition if one exists. To the best of our knowledge, our work is the first attempt to provide an algorithm for the automatic synthesis of *e-Service* composition, that is both proved to be correct, and has an associated computational complexity characterization.

## 1 Introduction

*Service Oriented Computing* (SOC [20]) aims at building agile networks of collaborating business applications, distributed within and across organizational boundaries.<sup>1</sup> *e-Services*, which are the basic building blocks of SOC, represent a new model in the utilization of the network, in which self-contained, modular applications can be described, published, located and dynamically invoked, in a programming language independent way.

The commonly accepted and *minimal* framework for *e-Services*, referred to as Service Oriented Architecture (SOA [21]), consists of the following basic roles: (i) the *service provider*, which is the subject (e.g., an organization) providing services; (ii) the *service directory*, which is the subject providing a repository/registry of service descriptions, where providers publish their services and requestors find services; and, (iii) the *service requestor*, also referred to as client, which is the subject looking for and invoking the service in order to fulfill some goals. A requestor discovers a suitable service in the directory, and then it connects to the specific service provider and uses the service.

Research on *e-Services* spans over many interesting issues regarding, in particular, composability, synchronization, coordination, and verification [26]. In this paper, we are particularly interested in automatic *e-Service* composition. *e-Service composition* addresses the situation when a client request cannot be satisfied by an available *e-Service*, but a *composite e-Service*, obtained by combining “parts of” available *component e-Services*, might be used. Each composite *e-Service* can be regarded as a kind of client wrt its components, since it (indirectly) looks for and invokes them. *e-Service* composition leads to enhancements of the SOA, by adding new elements and roles, such as brokers and integration systems, which are able to satisfy client needs by combining available *e-Services*.

Composition involves two different issues. The first, sometimes called *composition synthesis*, or simply *composition*, is concerned with synthesizing a new composite *e-Service*, thus producing a specification of how to coordinate the component *e-Services* to obtain the composite *e-Service*. Such a specification can be obtained either *automatically*, i.e., using a tool that implements a composition algorithm, or *manually* by a human. The second, often referred to as *orchestration*, is concerned with coordinating the various component *e-Services* according to some given specification, and also monitoring control and data flow among the

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<sup>1</sup> cf., Service Oriented Computing Net: <http://www.eusoc.net/>

involved *e*-Services, in order to guarantee the correct execution of the composite *e*-Service, synthesized in the previous phase.

Our main focus in this paper is on automatic composition synthesis. In order to address this issue in an effective and well-founded way, our first contribution is a general formal framework for representing *e*-Services. Note that several works published in the literature address service oriented computing from different points of views (see [13] for a survey), but an agreed comprehension of what an *e*-Service is, in an abstract and general fashion, is still lacking. Our framework, although simplified in several aspects, provides not only a clear definition of *e*-Services, but also a formal setting for a precise characterization of automatic composition of *e*-Services.

The second contribution of the paper is an effective technique for automatic *e*-Service composition. In particular, we specialize the general framework to the case where *e*-Services are specified by means of finite state machines, and we present an algorithm that, given a specification of a target *e*-Service, i.e., specified by a client, and a set of available *e*-Services, synthesizes a composite *e*-Service that uses only the available *e*-Services and fully captures the target one. We also study the computational complexity of our algorithm, and we show that it runs in exponential time with respect to the size of the input state machines.

Although several papers have been already published that discuss either a formal model of *e*-Services (even more expressive than ours, see e.g., [7]), or propose algorithms for computing composition (e.g., [19]), to the best of our knowledge, the work presented in this paper is the first one tackling simultaneously the following issues: (i) presenting a formal model where the problem of *e*-Service composition is precisely characterized, (ii) providing techniques for computing *e*-Service composition in the case of *e*-Services represented by finite state machines, and (iii) providing a computational complexity characterization of the algorithm for automatic composition.

The rest of this paper is organized as follows. In Section 2 and 3 we define our general formal framework, and in Section 4 we define the problem of composition synthesis in such a framework. In Section 5 we specialize the general framework to the case where *e*-Services are specified by means of finite state machines, and in Section 6 we present an EXPTIME algorithm for automatic *e*-Service composition in the specialized framework. Finally, in Section 7 we consider related research work and in Section 8 we draw conclusions by discussing future work.

## 2 General Framework

Generally speaking, an *e*-Service is a software artifact (delivered over the Internet) that interacts with its clients in order to perform a specified task. A client can be either a human user, or another *e*-Service. When executed, an *e*-Service performs its task by directly executing certain actions, and interacting with other *e*-Services to delegate to them the execution of other actions. In order to address SOC from an abstract and conceptual point of view, we start by identifying several facets, each one reflecting a particular aspect of an *e*-Service during its life time, as shown in Figure 1:

- The *e*-Service *schema* specifies the features of an *e*-Service, in terms of functional and non-functional requirements. Functional requirements represent *what* an *e*-Service does. All other characteristics of *e*-Services, such as those related to quality, privacy, performance, etc. constitute the non-functional requirements. In what follows, we do not deal with non-functional requirements, and hence use the term “*e*-Service schema” to denote the specification of functional requirements only.
- The *e*-Service *implementation and deployment* indicate *how* an *e*-Service is realized, in terms of software applications corresponding to the *e*-Service schema, deployed on specific platforms. This aspect regards the technology underlying the *e*-Service implementation, and it goes beyond the scope of this paper. Therefore, although implementation issues, and other related characteristics such as recovery mechanisms or exception handling, are important issues in SOC, in what follows we abstract from these properties of *e*-Services.
- An *e*-Service *instance* is an occurrence of an *e*-Service effectively running and interacting with a client. In general, several running instances corresponding to the same *e*-Service schema exist, each one executing independently from the others.

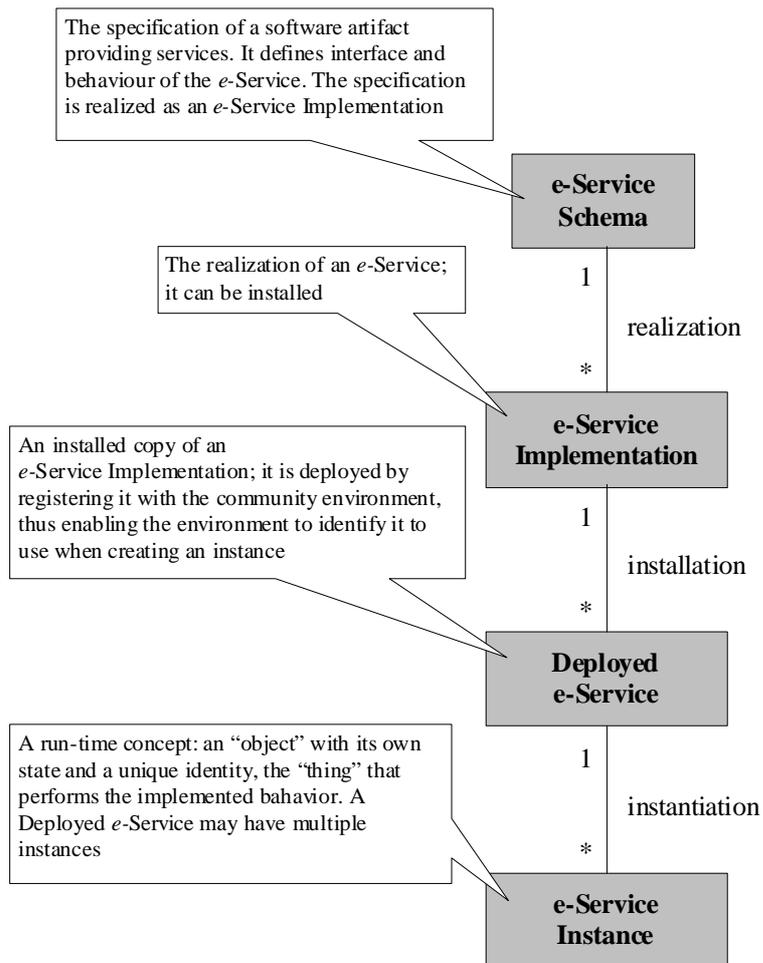


Fig. 1. e-Service facets

In order to execute an *e-Service*, the client needs to *activate* an instance from a deployed *e-Service*. In our abstract model, the client can then interact with the *e-Service* instance by repeatedly *choosing* an action and waiting for either the fulfillment of the specific task, or the return of some information. On the basis of the information returned the client chooses the next action to invoke. In turn, the activated *e-Service* instance executes (the computation associated to) the invoked action; after that, it is ready to execute new actions. Under certain circumstances, i.e., when the client has reached his goal, he may explicitly *end* (i.e., terminate) the *e-Service* instance. However, in principle, a given *e-Service* instance may need to interact with a client for an unbounded, or even infinite, number of steps, thus providing the client with a continuous service. In this case, no operation for ending the *e-Service* instance is ever executed.

In general, when a client invokes an *e-Service* instance  $e$ , it may happen that  $e$  does not execute all of its actions on its own, but instead it *delegates* some or all of them to other *e-Service* instances. All this is transparent to the client. To precisely capture the situations when the execution of certain actions can be delegated to other *e-Service* instances, we introduce the notion of *community* of *e-Services*, which is formally characterized by:

- a finite common set of actions  $\Sigma$ , called the *action alphabet*, or simply the *alphabet* of the community,
- a set of *e-Services* specified in terms of the common set of actions.

Hence, to join a community, an *e-Service* needs to export its service(s) in terms of the alphabet of the community. The added value of a community is the fact that an *e-Service* of the community may delegate the execution of some or all of its actions to other instances of *e-Services* in the community. We call such an *e-Service composite*. If this is not the case, an *e-Service* is called *simple*. Simple *e-Services* realize offered actions directly in the software artifacts implementing them, whereas composite *e-Services*, when receiving requests from clients, can invoke other *e-Service* instances in order to fulfill the client’s needs.

Notably, the community can be used to generate (virtual) *e-Services* whose execution completely delegates actions to other members of the community. In other words, the community can be used to realize a target *e-Service* requested by the client, not simply by selecting a member of the community to which delegate the target *e-Service* actions, but more generally by suitably “composing” parts of *e-Service* instances in the community in order to obtain a virtual *e-Service* which is coherent with the target one. This function of composing existing *e-Services* on the basis of a target *e-Service* is known as *e-Service composition*, and is the main subject of the research reported in this paper.

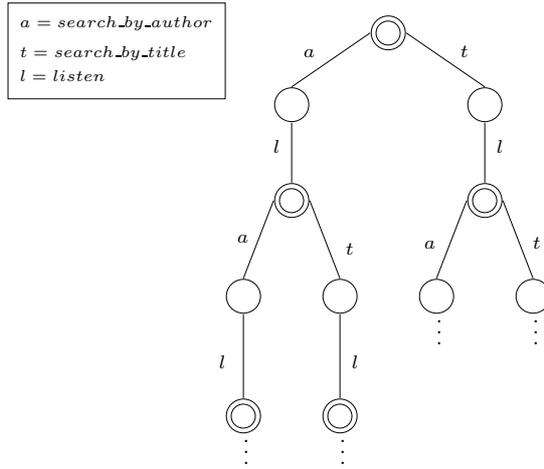
### 3 *e-Service* Schema

From the external point of view, i.e., that of a client, an *e-Service*  $E$ , belonging to a community  $C$ , is seen as a black box that exhibits a certain *exported behavior* represented as sequences of atomic *actions* of  $C$  with constraints on their invocation order. From the internal point of view, i.e., that of an application deploying  $E$  and activating and running an instance of it, it is also of interest how the actions that are part of the behavior of  $E$  are effectively executed. Specifically, it is relevant to specify whether each action is executed by  $E$  itself or whether its execution is delegated to another *e-Service* belonging to the community  $C$  with which  $E$  interacts, transparently to the client of  $E$ . To capture these two points of view we introduce the notion of *e-Service schema*, as constituted by two different parts, called *external schema* and *internal schema*, respectively.

Also *e-Service* instances can be characterized by an external and an internal view: further details can be found in [5].

#### 3.1 External Schema

The aim of the external schema is to specify the exported behavior of the *e-Service*. For now we are not concerned with any particular specification formalism, rather we only assume that, whatever formalism is used, the external schema specifies the behavior in terms of a tree of actions, called *external execution tree*. The external execution tree abstractly represents all possible executions of all possible instances of an *e-Service*. Therefore, any instance of an *e-Service* executes a path of such a tree. In this sense, each node  $x$  of



**Fig. 2.** External execution tree of  $e$ -Service  $E_0$

an external execution tree represents the history of the sequence of actions of all  $e$ -Service instances<sup>2</sup>, that have executed the path to  $x$ . For every action  $a$  belonging to the alphabet  $\Sigma$  of the community, and that can be executed at the point represented by  $x$ , there is a (single) successor node  $x \cdot a$ . The node  $x \cdot a$  represents the fact that, after performing the sequence of actions leading to  $x$ , the client chooses to execute action  $a$ , among those possible, thus getting to  $x \cdot a$ . Therefore, each node represents a choice point at which the client makes a decision on the next action the  $e$ -Service should perform. We call the pair  $(x, x \cdot a)$  *edge* of the tree and we say that such an edge is *labeled* with action  $a$ . The root  $\varepsilon$  of the tree represents the fact that the  $e$ -Service has not yet executed any action. Some nodes of the execution tree are *final*: when a node is final, and only then, the client can stop the execution of the  $e$ -Service. In other words, the execution of an  $e$ -Service can correctly terminate only at these points<sup>3</sup>.

Notably, an execution tree does not represent the information returned to the client by the  $e$ -Service instance execution, since the purpose of such information is to let the client choose the next action, and the rationale behind this choice depends entirely on the client.

Given the external schema  $E^{ext}$  of an  $e$ -Service  $E$ , we denote with  $T(E^{ext})$  the external execution tree specified by  $E^{ext}$ .

*Example 1.* Figure 2 shows (a portion of) an (infinite) external execution tree representing  $e$ -Service  $E_0$  that allows for searching and listening to mp3 files<sup>4</sup>. In particular, the client may choose to search for a song by specifying either its author(s) or its title (action `search_by_author` and `search_by_title`, respectively). Then the client selects and listens to a song (action `listen`). Finally, the client chooses whether to perform those actions again.  $\square$

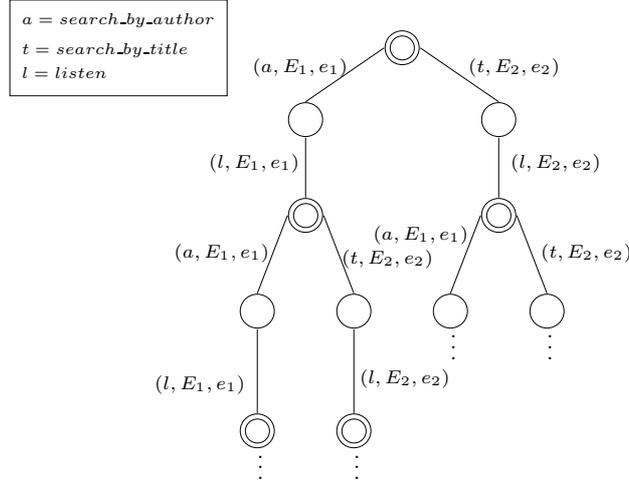
### 3.2 Internal Schema

The internal schema specifies, besides the external behavior of the  $e$ -Service, the information on which  $e$ -Service instances in the community execute each given action. As before, for now, we abstract from the specific formalism chosen for giving such a specification, instead we concentrate on the notion of *internal execution tree*. An internal execution tree is analogous to an external execution tree, except that each edge is labeled by  $(a, I)$ , where  $a$  is the executed action and  $I$  is a nonempty set denoting the  $e$ -Service instances executing  $a$ . Every element of  $I$  is a pair  $(E', e')$ , where  $E'$  is an  $e$ -Service and  $e'$  is the identifier of an instance of  $E'$ . The identifier  $e'$  uniquely identifies the instance of  $E'$  within the internal execution tree. In

<sup>2</sup> In what follows, we omit the terms “schema” and “instance” when clear from the context.

<sup>3</sup> Typically, in an  $e$ -Service, the root is final, to model that the computation of the  $e$ -Service may not be started at all by the client.

<sup>4</sup> Final nodes are represented by two concentric circles.



**Fig. 3.** Internal execution tree of  $e$ -Service  $E_0$

general, in the internal execution tree of an  $e$ -Service  $E$ , some actions may be executed also by the running instance of  $E$  itself. In this case we use the special instance identifier **this**. Note that, since  $I$  is in general not a singleton, the execution of each action can be delegated to more than one other  $e$ -Service instance.

An internal execution tree *induces* an external execution tree: given an internal execution tree  $T_{int}$  we call *offered external execution tree* the external execution tree  $T_{ext}$  obtained from  $T_{int}$  by dropping the part of the labeling denoting the  $e$ -Service instances, and therefore keeping only the information on the actions. An internal execution tree  $T_{int}$  *conforms to* an external execution tree  $T_{ext}$  if  $T_{ext}$  is equal to the offered external execution tree of  $T_{int}$ .

Given an  $e$ -Service  $E$ , the internal schema  $E^{int}$  of  $E$  is a specification that uniquely represents an internal execution tree. We denote such an internal execution tree by  $T(E^{int})$ .

An  $e$ -Service  $E$  with external schema  $E^{ext}$  and internal schema  $E^{int}$  is *well formed*, if  $T(E^{int})$  conforms to  $T(E^{ext})$ , i.e., its internal execution tree conforms with its external execution tree.

We now formally define when an  $e$ -Service of a community correctly delegates actions to other  $e$ -Services of the community. We need a preliminary definition: given the internal execution tree  $T_{int}$  of an  $e$ -Service  $E$ , and a path  $p$  in  $T_{int}$  starting from the root, we call the *projection* of  $p$  on an instance  $e'$  of an  $e$ -Service  $E'$  the path obtained from  $p$  by removing each edge whose label  $(a, I)$  is such that  $I$  does not contain  $e'$ , and collapsing start and end node of each removed edge.

We say that the internal execution tree  $T_{int}$  of an  $e$ -Service  $E$  is *coherent* with a community  $C$  if:

- for each edge labeled with  $(a, I)$ , the action  $a$  is in the alphabet of  $C$ , and for each pair  $(E', e')$  in  $I$ ,  $E'$  is a member of the community  $C$ ;
- for each path  $p$  in  $T_{int}$  from the root of  $T_{int}$  to a node  $x$ , and for each pair  $(E', e')$  appearing in  $p$ , with  $e'$  different from **this**, the projection of  $p$  on  $e'$  is a path in the external execution tree  $T'_{ext}$  of  $E'$  from the root of  $T'_{ext}$  to a node  $y$ , and moreover, if  $x$  is final in  $T_{int}$ , then  $y$  is final in  $T'_{ext}$ .

Observe that, if an  $e$ -Service of a community  $C$  is simple, i.e., it does not delegate actions to other  $e$ -Service instances, then it is trivially coherent with  $C$ . Otherwise, it is composite and hence delegates actions to other  $e$ -Service instances. In the latter case, the behavior of each one of such  $e$ -Service instances must be correct according to its external schema.

A community of  $e$ -Services is *well-formed* if each  $e$ -Service in the community is *well-formed*, and the internal execution tree of each  $e$ -Service in the community is coherent with the community.

*Example 2.* Figure 3<sup>5</sup> shows (a portion of) an (infinite) internal execution tree, conforming to the external execution tree of  $e$ -Service  $E_0$  shown in Figure 2, where all the actions are delegated to  $e$ -Services of the

<sup>5</sup> In the figure, each action is delegated to exactly one instance of an  $e$ -Service schema. Hence, for simplicity, we have denoted a label  $(a, \{(E_i, e_i)\})$  simply by  $(a, E_i, e_i)$ , for  $i = 1, 2$ .

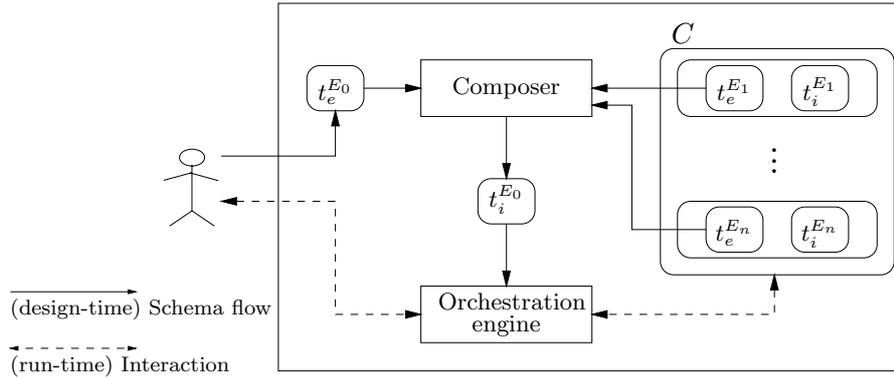


Fig. 4. *e-Service Integration System*

community. In particular, the execution of `search_by_title` action and its subsequent `listen` action are delegated to instance  $e_2$  of *e-Service*  $E_2$ , and `search_by_author` action and its subsequent `listen` action to instance  $e_1$  of *e-Service*  $E_1$ .  $\square$

## 4 Composition Synthesis

When a user requests a certain service from an *e-Service* community, there may be no *e-Service* in the community that can deliver it directly. However, it may still be possible to synthesize a new composite *e-Service*, which suitably delegates action execution to the *e-Services* of the community, and when suitably orchestrated, provides the user with the service he requested. Formally, given an *e-Service* community  $C$  and the external schema  $E^{ext}$  of a target *e-Service*  $E$  expressed in terms of the alphabet  $\Sigma$  of  $C$ , a *composition* of  $E$  wrt  $C$  is an internal schema  $E^{int}$  such that (i)  $T(E^{int})$  conforms to  $T(E^{ext})$ , (ii)  $T(E^{int})$  delegates all actions to the *e-Services* of  $C$  (i.e., **this** does not appear in  $T(E^{int})$ ), and (iii)  $T(E^{int})$  is coherent with  $C$ .

The problem of *composition existence* is the problem of checking whether there exists some internal schema  $E^{int}$  that is a composition of  $E$  wrt  $C$ . Observe that, since for now we are not placing any restriction of the form of  $E^{int}$ , this corresponds to checking if there exists an internal execution tree  $T_{int}$  such that (i)  $T_{int}$  conforms to  $T(E^{ext})$ , (ii)  $T_{int}$  delegates all actions to the *e-Services* of  $C$ , and (iii)  $T_{int}$  is coherent with  $C$ .

The problem of *composition synthesis* is the problem of synthesizing an internal schema  $E^{int}$  for  $E$  that is a composition of  $E$  wrt  $C$ .

Figure 4 shows the architecture of an *e-Service Integration System*, which delivers possibly composite *e-Services* on the basis of user requests, exploiting the available *e-Services* of a community  $C$ . When a client requests a new *e-Service*  $E$ , he presents his request in the form of an external *e-Service* schema  $E^{ext}$  for  $E$ , and expects the *e-Service* Integration System to execute an instance of  $E$ . To do so, first a *composer* module makes the composite *e-Service*  $E$  available for execution, by synthesizing an internal schema  $E^{int}$ <sup>6</sup> of  $E$  that is a composition of  $E$  wrt the community  $C$ . Then, following the internal execution tree  $T(E^{int})$  specified by  $E^{int}$ , an *orchestration engine* activates an (internal) instance of  $E$ , and orchestrates the different available *e-Services*, by activating and interacting with their external view, so as to fulfill the client's needs.

The orchestration engine is also in charge of terminating the execution of component *e-Service* instances, offering the correct set of actions to the client, as defined by the external execution tree, and invoking the action chosen by the client on the *e-Service* that offers it.

All this happens in a transparent manner for the client, who interacts only with the *e-Service* Integration System and is not aware that a composite *e-Service* is being executed instead of a simple one.

<sup>6</sup> If at least one exists.

## 5 e-Services as Finite State Machines

Till now, we have not referred to any specific form of *e-Service* schemas. In what follows, we consider *e-Services* whose schema (both internal and external) can be represented using only a *finite number of states*, i.e., using (deterministic) Finite State Machines (FSMs).

The class of *e-Services* that can be captured by FSMs are of particular interest. This class allows us to address an interesting set of *e-Services*, that are able to carry on rather complex interactions with their clients, performing useful tasks. Indeed, several papers in the *e-Service* literature adopt FSMs as the basic model of exported behavior of *e-Services* [7, 6]. Also, FSMs constitute the core of statecharts, which are one of the main components of UML and are becoming a widely used formalism for specifying the dynamic behavior of entities.

In the study we report here, we make the simplifying assumption that the number of instances of an *e-Service* in the community that can be involved in the internal execution tree of another *e-Service* is bounded and fixed a priori. In fact, wlog we assume that it is equal to one. If more instances correspond to the same external schema, we simply duplicate the external schema for each instance. Considering that the number of *e-Services* in a community is finite, this implies that the overall number of instances orchestrated by the orchestrator in executing an *e-Service* is finite and bounded by the number of *e-Services* belonging to the community. Within this setting, in the next section, we show how to solve the composition problem, and how to synthesize a composition that is a FSM. Instead, how to deal with an unbounded number of instances remains open for future work.

We consider here *e-Services* whose external schemas can be represented with a finite number of states. Intuitively, this means that we can factorize the sequence of actions executed at a certain point into a finite number of states, which are sufficient to determine the future behavior of the *e-Service*. Formally, for an *e-Service*  $E$ , the external schema of  $E$  is a FSM  $A_E^{ext} = (\Sigma, S_E, s_E^0, \delta_E, F_E)$ , where:

- $\Sigma$  is the alphabet of the FSM, which is the alphabet of the community;
- $S_E$  is the set of states of the FSM, representing the finite set of states of the *e-Service*  $E$ ;
- $s_E^0$  is the initial state of the FSM, representing the initial state of the *e-Service*;
- $\delta_E : S_E \times \Sigma \rightarrow S_E$  is the (partial) transition function of the FSM, which is a partial function that given a state  $s$  and an action  $a$  returns the state resulting from executing  $a$  in  $s$ ;
- $F_E \subseteq S_E$  is the set of final states of the FSM, representing the set of states that are final for the *e-Service*  $E$ , i.e., the states where the interactions with  $E$  can be terminated.

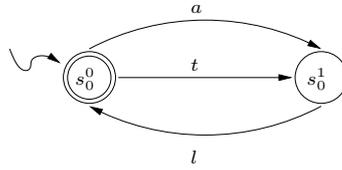
*Example 3.* Figure 5(a) shows the external schema of the (target) *e-Service*  $E_0$  of Examples 1 and 2, specified by the client as a FSM  $A_0$ . Figure 5 (b) and (c) show the external schema, represented as FSMs  $A_1$  and  $A_2$ , respectively associated to component *e-Services*  $E_1$  and  $E_2$  of Example 2. In other words,  $A_1$  and  $A_2$  are the external schema of the *e-Services* that should be composed in order to obtain a new *e-Service* that behaves like  $E_0$ . In particular,  $E_1$  allows for searching for a song by specifying its author(s) (action `search_by_author`) and for listening to the song selected by the client (action `listen`). Then, it allows for executing these actions again.  $E_2$  behaves like  $E_1$ , but it allows for retrieving a song by specifying its title (action `search_by_title`).

$E_1$  and  $E_2$  belong to the same community of *e-Services*  $C$ . Wlog, we assume that  $C$  is composed by only  $E_1$  and  $E_2$  and therefore, the (finite) alphabet of actions of  $C$  is  $\Sigma = \{\text{search\_by\_author}, \text{search\_by\_title}, \text{listen}\}$ . According to our setting, the client specifies the external schema  $A_0$  of his target *e-Service* in terms of  $\Sigma$ .  $\square$

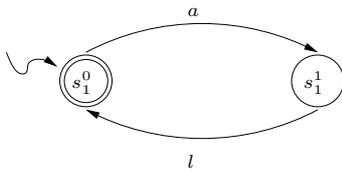
The FSM  $A_E^{ext}$  is an external schema in the sense that it *specifies* an external execution tree  $T(A_E^{ext})$ . Specifically, given  $A_E^{ext}$  we define  $T(A_E^{ext})$  inductively on the level of nodes in the tree, by making use of an auxiliary function  $\sigma(\cdot)$  that associates to each node of the tree a state in the FSM. We proceed as follows:

- $\varepsilon$ , as usual, is the root of  $T(A_E^{ext})$  and  $\sigma(\varepsilon) = s_E^0$ ;
- if  $x$  is a node of  $T(A_E^{ext})$ , and  $\sigma(x) = s$ , for some  $s \in S_E$ , then for each  $a$  such that  $s' = \delta_E(s, a)$  is defined,  $x \cdot a$  is a node of  $T(A_E^{ext})$  and  $\sigma(x \cdot a) = s'$ ;
- $x$  is final iff  $\sigma(x) \in F_E$ .

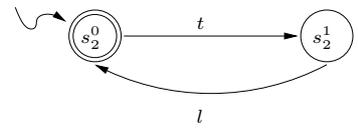
$a = \text{search\_by\_author}$   
 $t = \text{search\_by\_title}$   
 $l = \text{listen}$



(a) External schema  $A_0$  of target  $e$ -Service  $E_0$



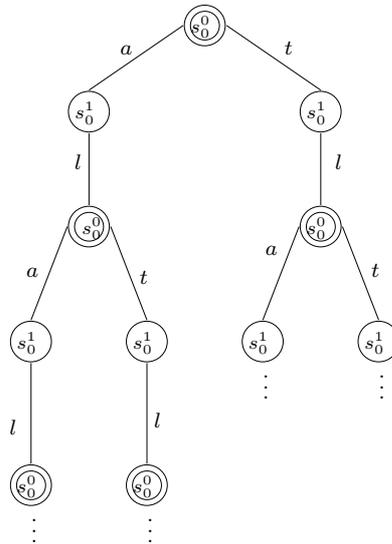
(b) External schema  $A_1$  of component  $e$ -Service  $E_1$



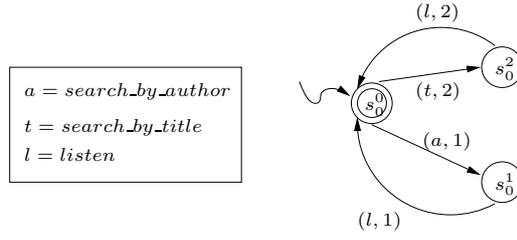
(c) External schema  $A_2$  of component  $e$ -Service  $E_2$

**Fig. 5.** Composition of  $e$ -Services

$a = \text{search\_by\_author}$   
 $t = \text{search\_by\_title}$   
 $l = \text{listen}$



**Fig. 6.** External execution tree  $T(A_0)$ .



**Fig. 7.**  $e$ -Service internal specification as MFSM  $M_0$ .

*Example 4.* Figure 6 shows (a portion of the) the external execution tree  $T(A_0)$  defined from  $A_0$  by a mapping  $\sigma$  (from nodes of  $T(A_0)$  to states of  $A_0$ ): each node of the tree is labeled with the state of  $A_0$  that  $\sigma$  associates to it. The mapping  $\sigma$  is defined as follows.

$$\begin{aligned} \sigma(\varepsilon) &= s_0^0 \\ \sigma(a) &= \sigma(t) = s_0^1 \\ \sigma(a \cdot l) &= \sigma(t \cdot l) = s_0^0 \\ \sigma(a \cdot l \cdot a) &= \sigma(a \cdot l \cdot t) = \sigma(t \cdot l \cdot a) = \sigma(t \cdot l \cdot t) = s_0^1 \\ \sigma(a \cdot l \cdot a \cdot l) &= \sigma(a \cdot l \cdot t \cdot l) = \sigma(t \cdot l \cdot a \cdot l) = \sigma(t \cdot l \cdot t \cdot l) = s_0^0 \\ &\dots \end{aligned}$$

$\sigma$  maps over  $s_0^1$  the nodes of the tree that represent strings ending by  $a$  or  $t$ ; it maps over  $s_0^0$  the root and the nodes of the tree associated to strings ending by  $l$ . Note that  $T(A_0)$  is equal to the external execution tree  $T_{ext}$  of Figure 2. That is,  $T_{ext}$  has a finite representation as a FSM.

The external execution trees  $T(A_1)$  and  $T(A_2)$  for the FSMs  $A_1$  and  $A_2$ , respectively, can be defined similarly.

Finally, note that in general there may be several FSMs that specify the same execution tree.  $\square$

Since we have assumed that each  $e$ -Service in the community can contribute to the internal execution tree of another  $e$ -Service with at most one instance, in specifying internal execution trees we do not need to distinguish between  $e$ -Service and  $e$ -Service instances. Hence, when the community  $C$  is formed by  $n$   $e$ -Services  $E_1, \dots, E_n$ , it suffices to label the internal execution tree of an  $e$ -Service  $E$  by the action that caused the transition and a subset of  $[n] = \{1, \dots, n\}$  that identifies which  $e$ -Services in the community have contributed in executing the action. The empty set  $\emptyset$  is used to (implicitly) denote **this**.

We are interested in internal schemas, for an  $e$ -Service  $E$ , that have a finite number of states, i.e., that can be represented as a Mealy FSM (MFSM)  $A_E^{int} = (\Sigma, 2^{[n]}, S_E^{int}, s_E^{0 \ int}, \delta_E^{int}, \omega_E^{int}, F_E^{int})$ , where:

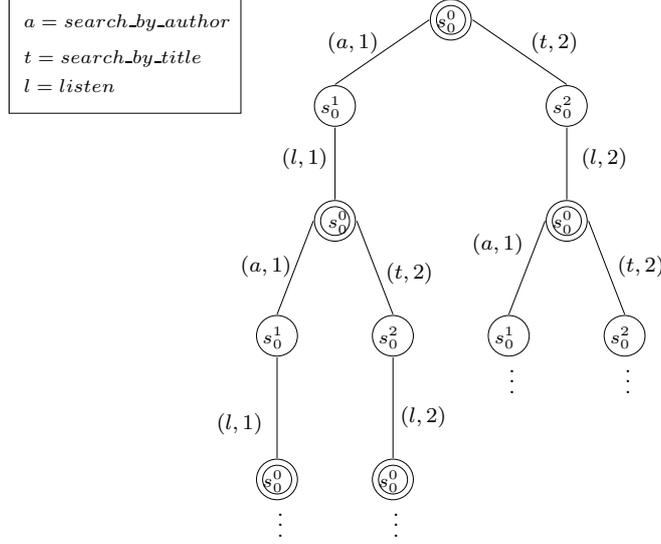
- $\Sigma, S_E^{int}, s_E^{0 \ int}, \delta_E^{int}, F_E^{int}$ , have the same meaning as for  $A_E^{ext}$ ;
- $2^{[n]}$  is the output alphabet of the MFSM, which is used to denote which  $e$ -Service instances execute each action;
- $\omega_E^{int} : S_E^{int} \times \Sigma \rightarrow 2^{[n]}$  is the output function of the MFSM, that, given a state  $s$  and an action  $a$ , returns the subset of  $e$ -Services that executes action  $a$  when  $e$ -Service  $E$  is in state  $s$ ; if such a set is empty then **this** is implied; we assume that the output function  $\omega_E^{int}$  is defined exactly when  $\delta_E^{int}$  is so.

*Example 5.* Figure 7 shows a possible internal schema for the target  $e$ -Service  $E_0$ . It is represented as a MFSM  $M_0$ . In the figure, we have defined the output function  $\omega^{int}$  as follows:

$$\begin{aligned} \omega^{int}(s_0^0, a) &= \{1\} & \omega^{int}(s_0^0, t) &= \{2\} \\ \omega^{int}(s_0^1, l) &= \{1\} & \omega^{int}(s_0^2, l) &= \{2\} \end{aligned}$$

$\square$

The MFSM  $A_E^{int}$  is an internal schema in the sense that it specifies an internal execution tree  $T(A_E^{int})$ . Given  $A_E^{int}$  we, again, define the internal execution tree  $T(A_E^{int})$  by induction on the level of the nodes, by making use of an auxiliary function  $\sigma^{int}(\cdot)$  that associates each node of the tree with a state in the MFSM, as follows:



**Fig. 8.** Internal execution tree  $T(M_0)$ .

- $\varepsilon$  is, as usual, the root of  $T(A_E^{int})$  and  $\sigma^{int}(\varepsilon) = s_E^0$ ;
- if  $x$  is a node of  $T(A_E^{int})$ , and  $\sigma^{int}(x) = s$ , for some  $s \in S_E^{int}$ , then for each  $a$  such that  $s' = \delta_E^{int}(s, a)$  is defined,  $x \cdot a$  is a node of  $T(A_E^{int})$  and  $\sigma^{int}(x \cdot a) = s'$ ;
- if  $x$  is a node of  $T(A_E^{int})$ , and  $\sigma^{int}(x) = s$ , for some  $s \in S_E^{int}$ , then for each  $a$  such that  $\omega_E^{int}(s, a)$  is defined (i.e.,  $\delta_E^{int}(s, a)$  is defined), the edge  $(x, x \cdot a)$  of the tree is labeled by  $\omega_E^{int}(s, a)$ ;
- $x$  is final iff  $\sigma^{int}(x) \in F_E^{int}$ .

*Example 6.* Figure 8 shows a portion of the internal execution tree  $T(M_0)$  defined from  $M_0$ , shown in Figure 7. Each node of the tree is labeled with the state of  $M_0$  that mapping  $\sigma^{int}$  from nodes of  $T(M_0)$  to states of  $M_0$ , associates to it. The mapping  $\sigma^{int}$  is defined as follows.

$$\begin{aligned}
\sigma^{int}(\varepsilon) &= s_0^0 \\
\sigma^{int}(a) &= s_0^1 \\
\sigma^{int}(t) &= s_0^2 \\
\sigma^{int}(a \cdot l) &= \sigma^{int}(t \cdot l) = s_0^0 \\
\sigma^{int}(a \cdot l \cdot a) &= \sigma^{int}(t \cdot l \cdot a) = s_0^1 \\
\sigma^{int}(a \cdot l \cdot t) &= \sigma^{int}(t \cdot l \cdot t) = s_0^2 \\
\sigma^{int}(a \cdot l \cdot a \cdot l) &= \sigma^{int}(a \cdot l \cdot t \cdot l) = \sigma^{int}(t \cdot l \cdot a \cdot l) = \sigma^{int}(t \cdot l \cdot t \cdot l) = s_0^0 \\
&\dots
\end{aligned}$$

$\sigma^{int}$  maps over  $s_0^1$  the nodes of the tree that represent strings ending by  $a$ , and over  $s_0^2$  the nodes that represent strings ending by  $t$ ; it maps over  $s_0^0$  the root and the nodes of the tree associated to strings ending by  $l$ .

Note that  $T(M_0)$  is equal to the internal execution tree  $T_{int}$  of Figure 3. That is,  $T_{int}$  has a finite representation as a MFSM. Therefore,  $M_0$  is a specification of an internal execution tree that conforms to the external execution tree specified by the FSM  $A_0$  of Figure 5(a).

Finally, note that in general, a FSM and its corresponding MFSM may have different structures.  $\square$

Given an  $e$ -Service  $E$  whose external schema is an FSM and whose internal schema is an MFSM, checking whether  $E$  is well formed, i.e., whether the internal execution tree conforms to the external execution tree, can be done using standard finite state machine techniques. Similarly for coherency of  $E$  with a community of  $e$ -Services whose external schemas are FSMs. In this paper, we do not go into the details of these problems, and instead we concentrate on composition.

## 6 Automatic *e*-Service Composition

We address the problem of actually checking the existence of a composite *e*-Service in the FSM-based framework introduced above. We show that if a composition exists then there is one where the internal schema is constituted by a MFSM, and we show how to actually synthesize such a MFSM. The basic tool we use to show such results is reducing the problem of composition existence into satisfiability of a suitable formula of Deterministic Propositional Dynamic Logic (DPDL), a well-known logic of programs developed to verify properties of program schemas [15]. We refer to Appendix A for a brief tutorial on DPDL. In order to make clearer the technique, we show how to build a MFSM for the target *e*-Service whose external schema is represented in Figure 5(a), and for the community of Example 3.

Given the target *e*-Service  $E_0$  whose external schema is a FSM  $A_0$  and a community of *e*-Services formed by  $n$  component *e*-Services  $E_1, \dots, E_n$  whose external schemas are FSM  $A_1, \dots, A_n$  respectively, we build a DPDL formula  $\Phi$  as follows. As set of atomic propositions  $\mathcal{P}$  in  $\Phi$  we have (i) one proposition  $s_j$  for each state  $s_j$  of  $A_j$ ,  $j = 0, \dots, n$ , denoting whether  $A_j$  is in state  $s_j$ ; (ii) propositions  $F_j$ ,  $j = 0, \dots, n$ , denoting whether  $A_j$  is in a final state; and (iii) propositions  $moved_j$ ,  $j = 1, \dots, n$ , denoting whether (component) automaton  $A_j$  performed a transition. As set of atomic actions  $\mathcal{A}$  in  $\Phi$  we have the actions in  $\Sigma$  (i.e.,  $\mathcal{A} = \Sigma$ ).

*Example 7.* The set  $\mathcal{P}$  of atomic propositions is defined as follows:

$$\mathcal{P} = \{s_0^0, s_0^1, s_1^0, s_1^1, s_2^0, s_2^1, F_0, F_1, F_2, moved_1, moved_2\}$$

The meaning of atomic propositions is as follows:

- $s_j^i$ , for  $i = 0, 1$  and  $j = 0, \dots, 2$ : automaton  $A_j$  is in state  $s_j^i$
- $F_j$  for  $j = 0, \dots, 2$ : automaton  $A_j$  is in a final state
- $moved_j$   $j = 1, \dots, 2$ : (component) automaton  $A_j$  performed a transition.

The set  $\mathcal{A}$  of deterministic atomic actions is defined as follows:

$$\mathcal{A} = \{a, t, l\}$$

where:

- $a$  denotes action `search_by_author`
- $t$  denotes action `search_by_title`
- $l$  denotes action `listen`

□.

In order to state universal assertions, we introduce the master modality  $[u]$ . In our running example, we set

$$u = (a \cup t \cup l)^*$$

i.e., as the reflexive and transitive closure of the union of all atomic actions in  $\mathcal{A}$ . In other words,  $u$  represents the iteration of a non deterministic choice among all the possible atomic actions. Indeed, we recall that  $[u]\phi$ , where  $\phi$  is a proposition, asserts that  $\phi$  holds after any regular expression involving  $a, t, l$ .

The formula  $\Phi$  is built as a conjunction of the following formulas.

- The formulas representing  $A_0 = (\Sigma, S_0, s_0^0, \delta_0, F_0)$ :
  - $[u](s \rightarrow \neg s')$  for all pairs of states  $s \in S_0$  and  $s' \in S_0$ , with  $s \neq s'$ ; these say that propositions representing different states are disjoint (cannot be true simultaneously).
  - $[u](s \rightarrow \langle a \rangle \mathbf{true} \wedge [a]s')$  for each  $a$  such that  $s' = \delta_0(s, a)$ ; these encode the transitions of  $A_0$ .
  - $[u](s \rightarrow [a]\mathbf{false})$  for each  $a$  such that  $\delta(s, a)$  is not defined; these say when a transition is not defined.
  - $[u](F_0 \leftrightarrow \bigvee_{s \in F_0} s)$ ; this highlights final states of  $A_0$ .

*Example 8.* Formulas capturing the external schema  $A_0$  of the target  $e$ -Service  $E_0$ .

$$[u]s_0^0 \rightarrow \neg s_0^1$$

This formula states that automaton  $A_0$  can never be simultaneously in the two states  $s_0^0$  and  $s_0^1$ . Note that it is equivalent to state  $[u]s_0^1 \rightarrow \neg s_0^0$ .

$$\begin{aligned} [u](s_0^0 \rightarrow \langle a \rangle \mathbf{true} \wedge [a]s_0^1) \\ [u](s_0^0 \rightarrow \langle t \rangle \mathbf{true} \wedge [t]s_0^1) \\ [u](s_0^0 \rightarrow \langle l \rangle \mathbf{true} \wedge [l]s_0^1) \end{aligned}$$

These formulas encode the transitions that  $A_0$  can perform. For example, the first formula asserts that, for all possible sequence of actions, if  $A_0$  is in state  $s_0^0$ , the automaton allows for searching an mp3 file by author, i.e., it can execute action  $a$ , and it necessarily moves to state  $s_0^1$ . Analogously for the other formulas.

$$\begin{aligned} [u](s_0^0 \rightarrow [l]\mathbf{false}) \\ [u](s_0^1 \rightarrow [a]\mathbf{false} \wedge [t]\mathbf{false}) \end{aligned}$$

These formulas encode the transitions that are not defined on  $A_0$ . For example, the first formula asserts that, for all possible sequences of actions, it is never possible to execute action **listen** when the automaton is in state  $s_0^0$ .

$$[u](F_0 \leftrightarrow s_0^0)$$

Finally, this formula asserts that  $s_0^0$  is a final state for  $A_0$ . □

– For each component FSM  $A_i = (\Sigma, S_i, s_i^0, \delta_i, F_i)$ , the following formulas:

- $[u](s \rightarrow \neg s')$  for all pairs of states  $s \in S_i$  and  $s' \in S_i$ , with  $s \neq s'$ ; these again say that propositions representing different states are disjoint.
- $[u](s \rightarrow [a](\mathit{moved}_i \wedge s' \vee \neg \mathit{moved}_i \wedge s))$  for each  $a$  such that  $s' = \delta_i(s, a)$ ; these encode the transitions of  $A_i$ , conditionalized to the fact that the component  $A_i$  is actually required to make a transition  $a$  in the composition.
- $[u](s \rightarrow [a]\neg \mathit{moved}_i)$  for each  $a$  such that  $\delta_i(s, a)$  is not defined; these say that when a transition is not defined,  $A_i$  cannot be asked to execute in the composition.
- $[u](F_i \leftrightarrow \bigvee_{s \in F_i} s)$ ; this highlights final states of  $A_i$ .

*Example 9.* Formulas capturing the external schema  $A_1$  of component  $e$ -Service  $E_1$ .

$$[u]s_1^0 \rightarrow \neg s_1^1$$

This formula has an analogous meaning as that relative to  $A_0$ .

$$\begin{aligned} [u](s_1^0 \rightarrow [a](\mathit{moved}_1 \wedge s_1^1 \vee \neg \mathit{moved}_1 \wedge s_1^0)) \\ [u](s_1^1 \rightarrow [l](\mathit{moved}_1 \wedge s_1^0 \vee \neg \mathit{moved}_1 \wedge s_1^1)) \end{aligned}$$

These formulas encode the transitions of  $A_1$ , conditioned to the fact that component  $A_1$  is actually required to make a transition in the composition. As an example, the first formula asserts that for all possible sequences of actions, if the automaton  $A_1$  is in  $s_1^0$ , then after action  $a$  has been executed, necessarily one of the following conditions must hold: either it is  $A_1$  that performed the transition and therefore it moved to state  $s_1^1$ , or the transition has been performed by another automaton, hence  $A_1$  did not move and remained in the current state  $s_1^0$ .

$$\begin{aligned} [u](s_1^0 \rightarrow [l]\neg \mathit{moved}_1 \wedge [t]\neg \mathit{moved}_1) \\ [u](s_1^1 \rightarrow [a]\neg \mathit{moved}_1 \wedge [t]\neg \mathit{moved}_1) \end{aligned}$$

These formulas encode the situation when a transition is not defined. For example, the first formula states that if the automaton is in state  $s_1^0$  and it receives actions  $l$  or  $t$  in input, it does not move; this

holds for all possible (previous) sequences of actions. Note that the situation when the automaton does not move is different from the situation when it loops on a state: indeed, in the latter case the transition is defined whereas in the former it does not.

Finally, the formula

$$[u](F_1 \leftrightarrow s_1^0)$$

asserts that state  $s_1^0$  is final for automaton  $A_1$ .

Formulas capturing the external schema  $A_2$  of component  $e$ -Service  $E_2$ .

Such formulas are analogous to the previous ones, therefore, we will just report them, without further comments.

$$[u]s_2^0 \rightarrow \neg s_2^1$$

$$\begin{aligned} [u](s_2^0 \rightarrow [t](moved_2 \wedge s_2^1 \vee \neg moved_2 \wedge s_2^0)) \\ [u](s_2^1 \rightarrow [l](moved_2 \wedge s_2^0 \vee \neg moved_2 \wedge s_2^1)) \end{aligned}$$

$$\begin{aligned} [u](s_2^0 \rightarrow [l]\neg moved_2 \wedge [a]\neg moved_2) \\ [u](s_2^1 \rightarrow [t]\neg moved_2 \wedge [a]\neg moved_2) \end{aligned}$$

$$[u](F_2 \leftrightarrow s_2^0)$$

□

– Finally, the following formulas:

- $s_0^0 \wedge \bigwedge_{i=1, \dots, n} s_i^0$ ; this says that initially all  $e$ -Services are in their initial state; note that this formula is not prefixed by  $[u]$ .
- $[u](\langle a \rangle \mathbf{true} \rightarrow [a] \bigvee_{i=1, \dots, n} moved_i)$ , for each  $a \in \Sigma$ ; these say that at each step at least one of the component FSM has moved.
- $[u](F_0 \rightarrow \bigwedge_{i=1, \dots, n} F_i)$ ; this says that when the target  $e$ -Service is in a final state also all component  $e$ -Services must be in a final state.

*Example 10.* The following formulas must hold for the overall composition.

$$s_0^0 \wedge s_1^0 \wedge s_2^0$$

It asserts that all  $e$ -Services start from their initial states.

$$\begin{aligned} [u](\langle a \rangle \mathbf{true} \rightarrow [a](moved_1 \vee moved_2)) \\ [u](\langle t \rangle \mathbf{true} \rightarrow [t](moved_1 \vee moved_2)) \\ [u](\langle l \rangle \mathbf{true} \rightarrow [l](moved_1 \vee moved_2)) \end{aligned}$$

Each formula expresses that at each step at least one FSM moves. For example, the first one asserts that for all possible execution sequences, if execution of  $a$  terminates, then necessarily  $a$  is executed by at least one component  $e$ -Service, either  $E_1$  or  $E_2$ .

Finally, if the composite  $e$ -Service is in a final state, both component  $e$ -Services must be in a final state: the composite  $e$ -Service may terminate only if also all the component  $e$ -Services can.

$$[u](F_0 \rightarrow F_1 \wedge F_2)$$

□

It is easy to prove that the Kripke structure for DPDL formula  $\Phi$  is deterministic, as it should be. Non determinism may be introduced by the operator  $\langle \rangle$ . However, we are guaranteed that no atomic action  $a$  relates state  $s_1$  with two different target states  $s_1$  and  $s_2$ , because  $\langle \rangle$  appears only in front of the atomic proposition **true**. Indeed, if  $a$  related  $s_1$  with  $s_2$  and  $s_3$ , such target states would actually be the same, since characterized by the same atomic proposition **true**.

**Theorem 1.** *The DPDL formula  $\Phi$ , constructed as above, is satisfiable if and only if there exists a composition of  $E_0$  wrt  $E_1, \dots, E_n$ .*

*Proof (sketch).* “ $\Leftarrow$ ” Suppose that there exists some internal schema (without restriction on its form)  $E_0^{int}$  which is a composition of  $E_0$  wrt  $E_1, \dots, E_n$ . Let  $T_{int} = T(E_0^{int})$  be the internal execution tree defined by  $E_0^{int}$ .

Then for the target  $e$ -Service  $E_0$  and each component  $e$ -Service  $E_i$ ,  $i = 1, \dots, n$ , we can define mappings  $\sigma$  and  $\sigma_i$  from nodes in  $T_{int}$  to states of  $A_0$  and  $A_i$ , respectively, by induction on the level of the nodes in  $T_{int}$  as follows.

- base case:  $\sigma(\varepsilon) = s_0^0$  and  $\sigma_i(\varepsilon) = s_i^0$ .
- inductive case: let  $\sigma(x) = s$  and  $\sigma_i(x) = s_i$ , and let the node  $x \cdot a$  be in  $T_{int}$  with the edge  $(x, x \cdot a)$  labeled by  $(a, I)$ , where  $I \subseteq [n]$  and  $I \neq \emptyset$  (notice that **this** may not occur since  $T_{int}$  is specified by a composition). Then we define

$$\sigma(x \cdot a) = s' = \delta_0(s, a)$$

and

$$\sigma_i(x \cdot a) = \begin{cases} s_i' = \delta_i(s_i, a) & \text{if } i \in I \\ s_i & \text{if } i \notin I \end{cases}$$

Once we have  $\sigma$  and  $\sigma_i$  in place we can define a model  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \Sigma}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$  of  $\Phi$  as follows:

- $\Delta^{\mathcal{I}} = \{x \mid x \in T_{int}\}$ ;
- $a^{\mathcal{I}} = \{(x, x \cdot a) \mid x, x \cdot a \in T_{int}\}$ , for each  $a \in \Sigma$ ;
- $s^{\mathcal{I}} = \{x \in T_{int} \mid \sigma(x) = s\}$ , for all propositions  $s$  corresponding to states of  $A_0$ ;
- $s_i^{\mathcal{I}} = \{x \in T_{int} \mid \sigma_i(x) = s_i\}$ , for all propositions  $s_i$  corresponding to states of  $A_i$ ;
- $moved_i^{\mathcal{I}} = \{x \cdot a \mid (x, x \cdot a) \text{ is labeled by } I \text{ with } i \in I\}$ , for  $i = 1, \dots, n$ ;
- $F_0^{\mathcal{I}} = \{x \in T_{int} \mid \sigma(x) = s \text{ with } s \in F_0\}$ ;
- $F_i^{\mathcal{I}} = \{x \in T_{int} \mid \sigma_i(x) = s_i \text{ with } s_i \in F_i\}$ , for  $i = 1, \dots, n$ .

It is easy to check that, being  $T_{int}$  specified by a composition  $E_{int}$ , the above model indeed satisfies  $\Phi$ .

“ $\Rightarrow$ ” Let  $\Phi$  be satisfiable and  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \Sigma}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$  be a tree-like model. From  $\mathcal{I}$  we can build an internal execution tree  $T_{int}$  for  $E_0$  as follows.

- the nodes of the tree are the elements of  $\Delta^{\mathcal{I}}$ ; actually, since  $\mathcal{I}$  is tree-like we can denote the elements in  $\Delta^{\mathcal{I}}$  as nodes of a tree, using the same notation that we used for internal/external execution tree;
- nodes  $x$  such that  $x \in F_0^{\mathcal{I}}$  are the final nodes;
- if  $(x, x \cdot a) \in a^{\mathcal{I}}$  and for all  $i \in I$ ,  $x \cdot a \in moved_i^{\mathcal{I}}$  and for all  $j \notin I$ ,  $x \cdot a \notin moved_j^{\mathcal{I}}$ , then  $(x, x \cdot a)$  is labeled by  $(a, I)$ .

It is possible to show that: (i)  $T_{int}$  conforms to  $T(A_0)$ , (ii)  $T_{int}$  delegates all actions to the  $e$ -Services of  $E_1, \dots, E_n$ , and (iii)  $T_{int}$  is coherent with  $E_1, \dots, E_n$ . Since we are not placing any restriction on the kind of specification allowed for internal schemas, it follows that there exists an internal schema  $E_{int}$  that is a composition of  $E_0$  wrt  $E_1, \dots, E_n$ .  $\square$

Observe that the size of  $\Phi$  is polynomially related to  $A_0$  and  $A_1, \dots, A_n$ . Hence, from the EXPTIME-completeness of satisfiability in DPDL and from Theorem 1 we get the following complexity result.

**Theorem 2.** *Checking the existence of an  $e$ -Service composition can be done in EXPTIME.*

Observe that, because of the small model property, from  $\Phi$  one can always obtain a model which is at most exponential in the size of  $\Phi$ . From such a model one can extract an internal schema for  $E_0$  that is a composition of  $E_0$  wrt  $E_1, \dots, E_n$ , which has the form of a MFSM. Specifically, given a finite model  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \Sigma}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$ , we define such an MFSM  $A_c = (\Sigma, 2^{[n]}, S_c, s_c^0, \delta_c, \omega_c, F_c)$  as follows:

- $S_c = \Delta^{\mathcal{I}}$ ;
- $s_c^0 = d_0$  where  $d_0 \in (s_0^0 \wedge \bigwedge_{i=1, \dots, n} s_i^0)^{\mathcal{I}}$ ;
- $s' = \delta_c(s, a)$  iff  $(s, s') \in a^{\mathcal{I}}$ ;
- $I = \omega_c(s, a)$  iff  $(s, s') \in a^{\mathcal{I}}$  and for all  $i \in I$ ,  $s' \in \text{moved}_i^{\mathcal{I}}$  and for all  $j \notin I$ ,  $s' \notin \text{moved}_j^{\mathcal{I}}$ ;
- $F_c = F_0^{\mathcal{I}}$ .

As a consequence of this, we get the following results.

**Theorem 3.** *If there exists a composition of  $E_0$  wrt  $E_1, \dots, E_n$ , then there exists one which is a MFSM of at most exponential size in the size of the external schemas  $A_0, A_1, \dots, A_n$  of  $E_0, E_1, \dots, E_n$  respectively.*

*Proof (sketch).* By Theorem 1, if  $A_0$  can be obtained by composing  $A_1, \dots, A_n$ , then the DPDL formula  $\Phi$  constructed as above is satisfiable. In turn, if  $\Phi$  is satisfiable, for the small-model property of DPDL there exists a model  $\mathcal{I}$  of size at most exponential in  $\Phi$ , and hence in  $A_0$  and  $A_1, \dots, A_n$ . From  $\mathcal{I}$  we can construct a MFSM  $A_c$  as above. It is possible to show that the internal execution tree  $T(A_c)$  defined by  $A_c$  satisfies all the conditions required for  $A_c$  to be a composition, namely: (i)  $T(A_c)$  conforms to  $T(A_0)$ , (ii)  $T(A_c)$  delegates all actions to the  $e$ -Services of  $E_1, \dots, E_n$ , and (iii)  $T(A_c)$  is coherent with  $E_1, \dots, E_n$ .  $\square$

From a practical point of view, because of the correspondence between Propositional Dynamic Logics (which DPDL belongs to) and Description Logics [8], one can use current highly optimized Description Logic systems [3]<sup>7</sup> to check the existence of  $e$ -Service compositions. Indeed, these systems are based on tableaux techniques that construct a model when checking for satisfiability, and from such a model one can construct a MFSM that is the composition.

## 6.1 Building composition

In this subsection, we first show how to build a possibly infinite model  $\mathcal{I}$  for the DPDL formula  $\Phi$  constituted as in the previous section. We follow the proof of Theorem 1 (“ $\Leftarrow$ ” direction). In order to build an internal execution tree for  $E_0$  from FMS  $A_1$  and  $A_2$ , i.e., to synthesize a composite  $e$ -Service  $E_0$  with components  $E_1$  and  $E_2$  (“ $\Rightarrow$ ” direction), it suffices to repeat the steps backwards. Some of these steps have been discussed in previous examples, but we report them here for sake of readability.

Then, assuming to have derived from  $\mathcal{I}$  a finite model  $\mathcal{I}_f$  for  $\Phi$ <sup>8</sup>, we show how to devise an internal schema conforming to  $A_0$  that has a finite state representation, and such that all conditions in Section 4 holds.

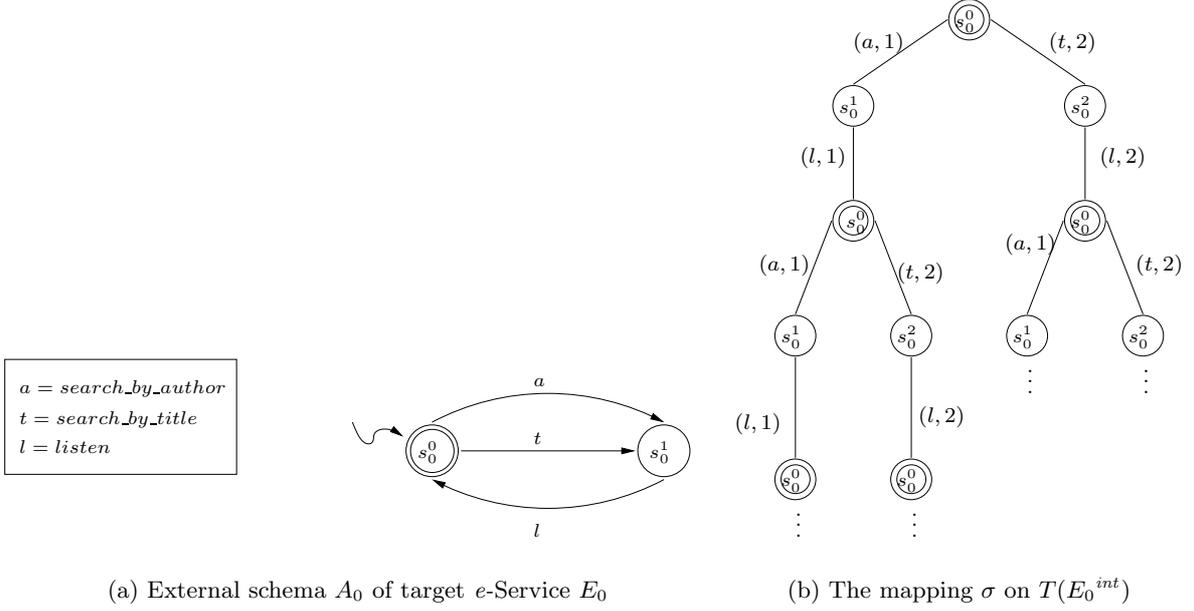
We assume that, given the component FSM  $A_1$  and  $A_2$  there exists a composite  $e$ -Service having FSM  $A_0$  as external schema and  $A_1$  and  $A_2$  as components. Let  $T(E_0^{int})$  be the internal execution tree for  $E_0$  wrt the community  $C$  to which  $E_1$  and  $E_2$  belong, such that: (i)  $T(E_0^{int})$  conforms to  $T(A_0)$ , i.e., to the external execution tree obtained by  $A_0$  as in Section 5, (ii)  $T(E_0^{int})$  delegates all actions to the  $e$ -Services of  $C$  and in particular to  $E_1$  and  $E_2$ , and (iii)  $T(E_0^{int})$  is coherent with  $C$ .

The mapping  $\sigma$  from nodes of  $T(E_0^{int})$  to states of the automata, is defined as follows by induction on the level of nodes in the tree. The existence of the mapping guarantees that condition (i) above is satisfied.

$$\begin{aligned}
\sigma(\varepsilon) &= s_0^0 \\
\sigma(a) &= \sigma(t) = s_0^1 \\
\sigma(a.l) &= \sigma(t.l) = s_0^0 \\
\sigma(a.l.a) &= \sigma(a.l.t) = \sigma(t.l.a) = \sigma(t.l.t) = s_0^1 \\
\sigma(a.l.a.l) &= \sigma(a.l.t.l) = \sigma(t.l.a.l) = \sigma(t.l.t.l) = s_0^0 \\
&\dots
\end{aligned}$$

<sup>7</sup> In fact, current Description Logics systems cannot handle Kleene star. However, since in  $\Phi$ ,  $*$  is only used to mimic universal assertions, and such systems have the ability of handling universal assertions, they can indeed check satisfiability of  $\Phi$ .

<sup>8</sup> Because of the small model property, we know that this is always possible.



**Fig. 9.** Composition of  $e$ -Services

Figure 9(b) represents the internal execution tree of  $E_0$ , where each node is labeled with the corresponding state of the automaton.  $\sigma$  maps over  $s_0^1$  the nodes of the tree that represent strings ending by  $a$  or  $t$ ; it maps over  $s_0^0$  the root of the tree and the nodes of the tree associated to strings ending by  $l$ .

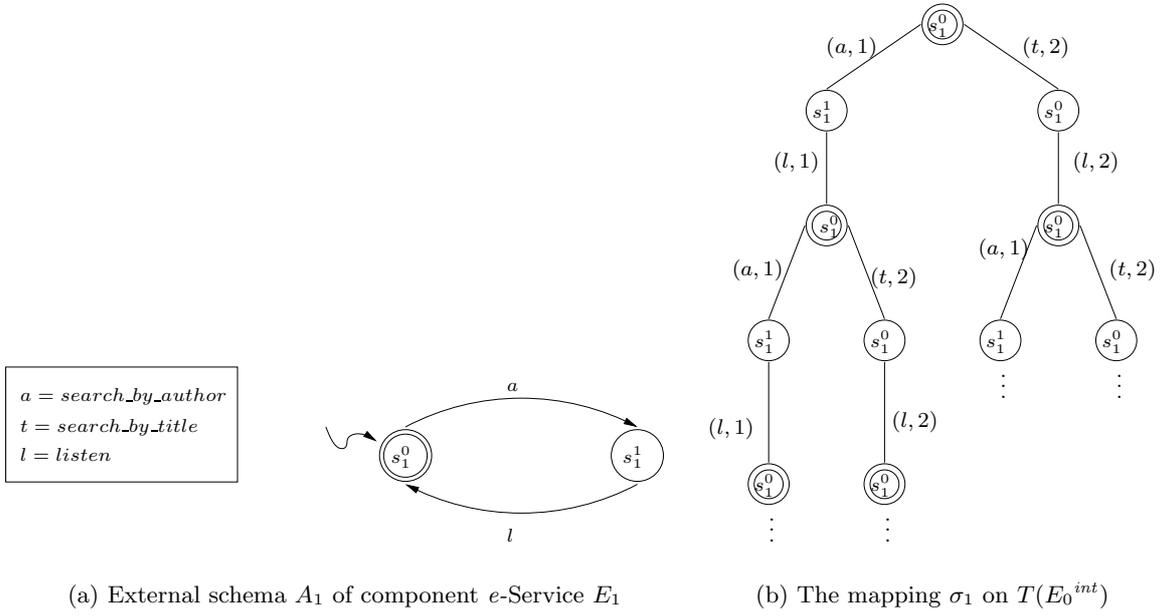
The mapping  $\sigma_1$  from nodes of  $T(E_0^{int})$  to states of  $A_1$  is defined as follows.

$$\begin{aligned}
\sigma_1(\varepsilon) &= s_1^0 \\
\sigma_1(a) &= s_1^1 \\
\sigma_1(t) &= s_1^0 \\
\sigma_1(a \cdot l) &= \sigma_1(t \cdot l) = s_1^0 \\
\sigma_1(a \cdot l \cdot a) &= \sigma_1(t \cdot l \cdot a) = s_1^1 \\
\sigma_1(a \cdot l \cdot t) &= \sigma_1(t \cdot l \cdot t) = s_1^0 \\
\sigma_1(a \cdot l \cdot a \cdot l) &= \sigma_1(a \cdot l \cdot t \cdot l) = \sigma_1(t \cdot l \cdot a \cdot l) = \sigma_1(t \cdot l \cdot t \cdot l) = s_1^0 \\
&\dots
\end{aligned}$$

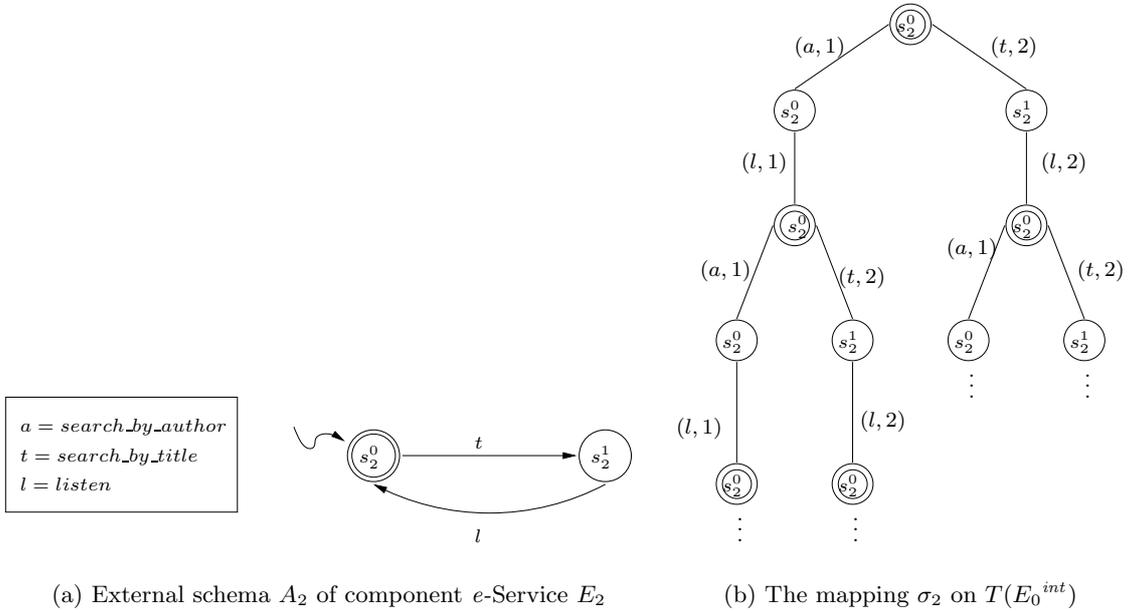
Figure 10(b) represents the internal execution tree of  $E_0$ , where each node is labeled with the corresponding state of the automaton.  $\sigma_1$  maps over  $s_1^1$  the nodes of the tree that represent strings ending by  $a$ ; it maps over  $s_1^0$  the root of the tree and the nodes of the tree associated to strings ending by  $l$  or by  $t$ . Note that since the automaton is not defined over  $t$ , it does not move when it receives  $t$  or  $t \cdot l$  as input.

The mapping  $\sigma_2$  from nodes of  $T(E_0^{int})$  to states of  $A_2$  is defined as follows.

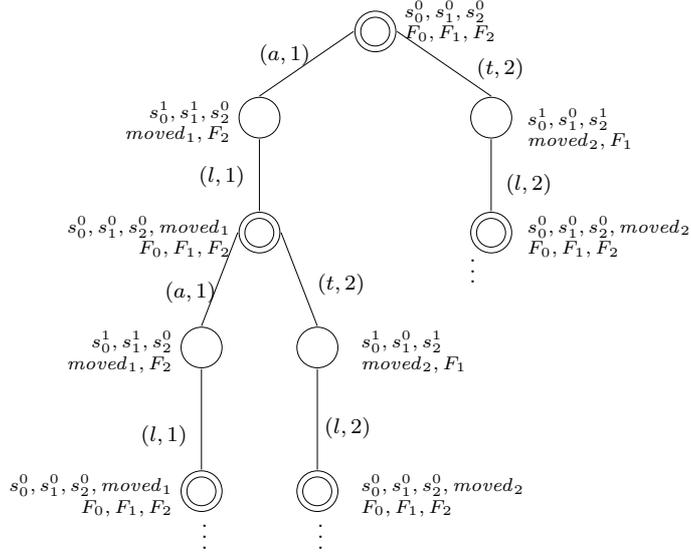
$$\begin{aligned}
\sigma_2(\varepsilon) &= s_2^0 \\
\sigma_2(a) &= s_2^0 \\
\sigma_2(t) &= s_2^1 \\
\sigma_2(a \cdot l) &= \sigma_2(t \cdot l) = s_2^0 \\
\sigma_2(a \cdot l \cdot a) &= \sigma_2(t \cdot l \cdot a) = s_2^0 \\
\sigma_2(a \cdot l \cdot t) &= \sigma_2(t \cdot l \cdot t) = s_2^1 \\
\sigma_2(a \cdot l \cdot a \cdot l) &= \sigma_2(a \cdot l \cdot t \cdot l) = \sigma_2(t \cdot l \cdot a \cdot l) = \sigma_2(t \cdot l \cdot t \cdot l) = s_2^0 \\
&\dots
\end{aligned}$$



**Fig. 10.** Composition of  $e$ -Services



**Fig. 11.** Composition of  $e$ -Services



**Fig. 12.** Infinite model  $\mathcal{I}$  for  $\Phi$ .

Figure 11(b) represents the internal execution tree of  $E_0$ , where each node is labeled with the corresponding state of the automaton.  $\sigma_2$  maps over  $s_2^1$  the nodes of the tree that represent strings ending by  $t$ ; it maps over  $s_2^0$  the root of the tree and the nodes of the tree associated to strings ending by  $l$  or by  $a$ .

Given  $\sigma$ ,  $\sigma_1$  and  $\sigma_2$ , we define  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \Sigma}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$  of  $\Phi$  as follows:

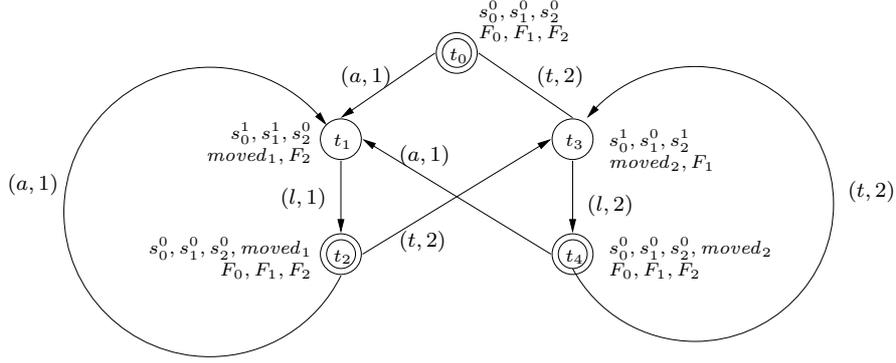
- $\Delta^{\mathcal{I}} = \{\varepsilon, a, t, a \cdot l, t \cdot l, a \cdot l \cdot a, a \cdot l \cdot t, t \cdot l \cdot a, t \cdot l \cdot t, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot a \cdot l, t \cdot l \cdot t \cdot l, \dots\}$ ,
- $a^{\mathcal{I}} = \{(\varepsilon, a), (a \cdot l, a \cdot l \cdot a), (t \cdot l, t \cdot l \cdot a), \dots\}$ ,
- $t^{\mathcal{I}} = \{(\varepsilon, t), (a \cdot l, a \cdot l \cdot t), (t \cdot l, t \cdot l \cdot t), \dots\}$ ,
- $l^{\mathcal{I}} = \{(a, a \cdot l), (t, t \cdot l), (a \cdot l \cdot a, a \cdot l \cdot a \cdot l), (a \cdot l \cdot t, a \cdot l \cdot t \cdot l), (t \cdot l \cdot a, t \cdot l \cdot a \cdot l), (t \cdot l \cdot t, t \cdot l \cdot t \cdot l), \dots\}$
- $(s_0^0)^{\mathcal{I}} = \{\varepsilon, a \cdot l, t \cdot l, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot a \cdot l, t \cdot l \cdot t \cdot l, \dots\}$
- $(s_1^0)^{\mathcal{I}} = \{a, t, a \cdot l \cdot a, a \cdot l \cdot t, t \cdot l \cdot a, t \cdot l \cdot t, \dots\}$
- $(s_1^1)^{\mathcal{I}} = \{\varepsilon, t, a \cdot l, t \cdot l, a \cdot l \cdot t, t \cdot l \cdot t, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot a \cdot l, t \cdot l \cdot t \cdot l, \dots\}$
- $(s_1^1)^{\mathcal{I}} = \{a, a \cdot l \cdot a, t \cdot l \cdot a, \dots\}$
- $(s_2^0)^{\mathcal{I}} = \{\varepsilon, a, a \cdot l, t \cdot l, a \cdot l \cdot a, t \cdot l \cdot a, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot a \cdot l, t \cdot l \cdot t \cdot l, \dots\}$
- $(s_2^1)^{\mathcal{I}} = \{t, a \cdot l \cdot t, t \cdot l \cdot t, \dots\}$
- $moved_1^{\mathcal{I}} = \{a, a \cdot l, a \cdot l \cdot a, t \cdot l \cdot a, a \cdot l \cdot a \cdot l, t \cdot l \cdot a \cdot l, \dots\}$
- $moved_2^{\mathcal{I}} = \{t, t \cdot l, a \cdot l \cdot t, t \cdot l \cdot t, a \cdot l \cdot t \cdot l, t \cdot l \cdot t \cdot l, \dots\}$
- $F_0^{\mathcal{I}} = \{\varepsilon, a \cdot l, t \cdot l, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot a \cdot l, t \cdot l \cdot t \cdot l, \dots\}$
- $F_1^{\mathcal{I}} = \{\varepsilon, t, a \cdot l, t \cdot l, a \cdot l \cdot t, t \cdot l \cdot t, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot t \cdot l, t \cdot l \cdot t \cdot l, \dots\}$
- $F_2^{\mathcal{I}} = \{\varepsilon, a, a \cdot l, t \cdot l, a \cdot l \cdot a, t \cdot l \cdot a, a \cdot l \cdot a \cdot l, a \cdot l \cdot t \cdot l, t \cdot l \cdot a \cdot l, t \cdot l \cdot t \cdot l, \dots\}$

Figure 12 shows that  $\mathcal{I}$  is a model for the formula  $\Phi^9$ . Each node of the tree is associated with the propositions in  $\mathcal{P}$  that hold in that node, according to  $\mathcal{I}$ . For example, consider the root:  $\mathcal{I}$  imposes that  $s_0^0 \wedge s_1^0 \wedge s_2^0 \wedge F_0 \wedge F_1 \wedge F_2$  holds in  $\varepsilon$ . Note that for sake of readability, in the figure we have associated to each node simply the list of atomic propositions that are true. Additionally, note that the DPDL encoding does not pose any constraint on the value of  $moved_i$  predicates in the root: we have arbitrarily chosen their value to be **false**. Finally, note that  $\mathcal{I}$  is not finite (the figure shows only a portion of the tree).

Because of the small model property,  $\Phi$  admits a finite model  $\mathcal{I}_f$ , shown in Figure 13 as a FSM.

The finite model  $\mathcal{I}_f$  induces mappings  $\sigma^f$ ,  $\sigma_1^f$  and  $\sigma_2^f$  from its states to states of the automata representing the external schema of the target  $e$ -Service and of the component ones.

<sup>9</sup> The action labeling on edges, of course, is not part of the model: we report it for readability.



**Fig. 13.** Finite model  $\mathcal{I}_f$  for  $\Phi$ .

$$\begin{aligned}
\sigma^f(t_0) &= \sigma^f(t_2) = \sigma^f(t_4) = s_0^0 \\
\sigma^f(t_1) &= \sigma^f(t_3) = s_0^1 \\
\sigma_1^f(t_0) &= \sigma_1^f(t_2) = \sigma_1^f(t_3) = \sigma_1^f(t_4) = s_1^0 \\
\sigma_1^f(t_1) &= s_1^1 \\
\sigma_2^f(t_0) &= \sigma_2^f(t_1) = \sigma_2^f(t_2) = \sigma_2^f(t_4) = s_2^0 \\
\sigma_2^f(t_3) &= s_2^1
\end{aligned}$$

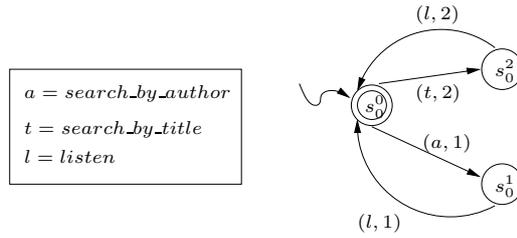
Given  $\sigma^f$ ,  $\sigma_1^f$  and  $\sigma_2^f$ , we can define  $\mathcal{I}_f = (\Delta_f^{\mathcal{I}}, \{a^{\mathcal{I}_f}\}_{a \in \Sigma}, \{P^{\mathcal{I}_f}\}_{P \in \mathcal{P}})$  of  $\Phi$  as follows:

- $\Delta_f^{\mathcal{I}} = \{t_0, t_1, t_2, t_3, t_4\}$ ,
- $a^{\mathcal{I}_f} = \{(t_0, t_1), (t_2, t_1), (t_4, t_1)\}$ ,
- $t^{\mathcal{I}_f} = \{(t_0, t_3), (t_2, t_3), (t_4, t_3)\}$ ,
- $l^{\mathcal{I}_f} = \{(t_1, t_2), (t_3, t_4)\}$
- $(s_0^0)^{\mathcal{I}_f} = \{t_0, t_2, t_4\}$
- $(s_0^1)^{\mathcal{I}_f} = \{t_1, t_3\}$
- $(s_1^0)^{\mathcal{I}_f} = \{t_0, t_2, t_3, t_4\}$
- $(s_1^1)^{\mathcal{I}_f} = \{t_1\}$
- $(s_2^0)^{\mathcal{I}_f} = \{t_0, t_1, t_2, t_4\}$
- $(s_2^1)^{\mathcal{I}_f} = \{t_3\}$
- $moved_1^{\mathcal{I}_f} = \{t_1, t_2\}$
- $moved_2^{\mathcal{I}_f} = \{t_3, t_4\}$
- $F_0^{\mathcal{I}_f} = \{t_0, t_2, t_4\}$
- $F_1^{\mathcal{I}_f} = \{t_0, t_2, t_3, t_4\}$
- $F_2^{\mathcal{I}_f} = \{t_0, t_1, t_2, t_4\}$

Given the finite model  $\mathcal{I}_f = (\Delta_f^{\mathcal{I}}, \{a^{\mathcal{I}_f}\}_{a \in \Sigma}, \{P^{\mathcal{I}_f}\}_{P \in \mathcal{P}})$  of  $\Phi$ , we define the Mealy Machine  $A_c = (\Sigma, 2^{[n]}, S_c, s_c^0, \delta_c, \omega_c, F_c, \cdot)$  representing the internal schema of the target  $e$ -Service, as follows:

- $S_c = \{t_0, t_1, t_2, t_3, t_4\}$ ;
- $s_c^0 = t_0$ , where  $t_0 \in (s_0^0 \wedge s_1^0 \wedge s_2^0)^{\mathcal{I}_f}$ ; note that we could have as well as chosen either  $t_2$  or  $t_4$  as initial state.
- $\delta_c$  is defined as:

$$\begin{array}{ll}
\delta_c(t_0, a) = t_1 & \delta_c(t_2, a) = t_1 \\
\delta_c(t_0, t) = t_3 & \delta_c(t_2, t) = t_3 \\
\delta_c(t_1, l) = t_2 & \delta_c(t_4, a) = t_1 \\
\delta_c(t_3, l) = t_4 & \delta_c(t_4, t) = t_3
\end{array}$$



**Fig. 14.** Minimal FSM associated to  $T(E_0^{int})$ .

–  $\omega_c$  is defined as:

$$\begin{array}{ll}
 \omega_c(t_0, a) = \{1\} & \omega_c(t_2, a) = \{1\} \\
 \omega_c(t_0, t) = \{2\} & \omega_c(t_2, t) = \{2\} \\
 \omega_c(t_1, l) = \{1\} & \omega_c(t_4, a) = \{1\} \\
 \omega_c(t_3, l) = \{2\} & \omega_c(t_4, t) = \{2\}
 \end{array}$$

–  $F_c = \{t_0, t_2, t_4\}$ .

This example shows also that the finite state machine associated to the finite model of  $\mathcal{P}$  is in general not minimal. Indeed, the minimal FSM associated to the tree representing the infinite model is shown in Figure 14. It is easy to see that it does not represent a model for  $\mathcal{P}$  since, for instance, state  $t_0$  is associated to both  $moved_1$  and  $\neg moved_1$ .

## 7 Related Work

Up to now, research on *e*-Services has mainly concentrated on three issues, namely (i) service description and modeling, (ii) service discovery (e.g., [24]) and (iii) service composition, including synthesis and orchestration.

Current research in description and modeling of *e*-Services is mainly founded on the work on workflows, which model business processes as sequences of (possibly partially) automated activities, in terms of data and control flow among them (e.g., [22, 14]). In [18] *e*-Services are represented as statecharts, and in [7], an *e*-Service is modeled as a Mealy machine, with input and output messages, and a queue is used to buffer messages that were received but not yet processed.

In our paper, we model *e*-Services as finite state machines, even if we do not consider communication delays and therefore any concept of message queuing is not taken into account. Indeed, from the survey of [13], it stems that the most practical approaches for modeling and describing *e*-Services are the ones based on specific forms of state machines. Additionally, our model of *e*-Service is oriented towards representing the interactions between a client and an *e*-Service. Therefore, our focus is on action sequences, rather than on message sequences as in [7], or on actions with input/output parameters as in [16].

As far as orchestration, it requires that the composite *e*-Service is specified in a precise way, considering both the specification of how various component *e*-Services are linked and the internal process flow of the component one. In [13], different technologies, standards and approaches for specification of composite *e*-Services are considered, including BPEL4WS, BPML, AZTEC, etc. Reference [13] identifies three different kinds of composition: (i) peer-to-peer, in which the individual *e*-Services are equals, (ii) the mediated approach, based on a hub-and-spoke topology, in which one service is given the role of process mediator, and (iii) the brokered approach, where process control is centralized but data can pass between component *e*-Services. With respect to such a classification, the approach proposed in this paper belongs to the mediated one.

Also most of other research works [9, 23, 17] can be classified into the mediated approach to composition. Conversely in [10] the enactment of a composite *e*-Service is carried out in a decentralized way, through peer-to-peer interactions.

The *DAML-S Coalition* [2] is defining a specific ontology and a related language for *e-Services*, with the aim of composing them in automatic way. In [25] the issue of service composition is addressed, in order to create composite services by re-using, specializing and extending existing ones; in [16, 19] composition of *e-Services* is addressed by using GOLOG and providing a semantics of the composition based on Petri Nets. In [1] a way of composing *e-Services* is presented, based on planning under uncertainty and constraint satisfaction techniques, and a request language, to be used for specifying client goals, is proposed. *e-Service* composition is indeed a form of program synthesis as is planning. The main conceptual difference is that, while in planning we typically are interested in synthesizing a *new* sequences of actions (or more generally a program, i.e., an execution tree) that achieves the client goal, in *e-Service* composition, we try to obtain (the execution tree of) the target *e-Service* by *reusing* in a suitable way fragments of the executions of the component *e-Services*.

In [7], the interplay between a composite *e-Service* (global) and component ones (local) is considered. The authors represent *e-Services* as FSMs and show that composite *e-Services* may no longer be a FSM in presence of unexpected behavior.

## 8 Conclusions

The main contribution of this paper wrt research on service oriented computing is in tackling *simultaneously* the following issues: (i) presenting a formal model where the problem of *e-Service* composition is precisely characterized, (ii) providing techniques for computing *e-Service* composition in the case of *e-Services* represented by finite state machines, and (iii) providing a computational complexity characterization of the algorithm for automatic composition.

In the future we plan to extend our work both in practical and theoretical directions. On one side, we are developing a Description Logic based prototype system that implements the composition technique presented in the paper. Such system will enable us to test how the complexity of composition in our framework impacts real world applications. On the theoretical side, we will address open issues such as the characterization of a lower bound for the complexity of the composition problem. Additionally, in the proposed framework, we have made the fundamental assumption that one has complete knowledge on the *e-Services* belonging to a community, in the form of their external and internal schema. We also assumed that a client gives a very precise specification (i.e., the external schema) of an *e-Service* he wants to have realized by a community. In particular, such a specification does not contain forms of “don’t care” nondeterminism. Both such assumptions can be relaxed, and this leads to a development of the proposed framework that is left for further research. Finally, we plan to extend our setting, by also considering the presence of communication delays and of an unbounded number of active instances.

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## A Deterministic Propositional Dynamic Logic

Propositional Dynamic Logics (PDLs) are a family of modal logics specifically developed for reasoning about computer programs [15]. They capture the properties of the interaction between programs and propositions that are independent of the domain of computation. In this appendix, we provide a brief overview of a logic of this family, namely Deterministic Propositional Dynamic Logic (DPDL). More details can be found in [12].

Syntactically, DPDL formulas are built by starting from a set  $\mathcal{P}$  of atomic propositions and a set  $\mathcal{A}$  of *deterministic* atomic actions as follows:

$$\begin{aligned} \phi &\longrightarrow \mathbf{true} \mid \mathbf{false} \mid P \mid \neg\phi \mid \phi_1 \wedge \phi_2 \mid \phi_1 \vee \phi_2 \mid \langle r \rangle \phi \mid [r] \phi \\ r &\longrightarrow a \mid r_1 \cup r_2 \mid r_1; r_2 \mid r^* \mid \phi? \end{aligned}$$

where  $P$  is an atomic proposition in  $\mathcal{P}$ ,  $r$  is a regular expression over the set of actions in  $\mathcal{A}$ , and  $a$  is an atomic action in  $\mathcal{A}$ . That is, DPDL formulas are composed from atomic propositions by applying arbitrary propositional connectives, and modal operators  $\langle r \rangle \phi$  and  $[r] \phi$ . The meaning of the latter two is, respectively, that there exists an execution of  $r$  reaching a state where  $\phi$  holds, and that all terminating executions of  $r$  reach a state where  $\phi$  holds. As far as compound programs,  $r_1 \cup r_2$  means “choose non deterministically between  $r_1$  and  $r_2$ ”;  $r_1; r_2$  means “first execute  $r_1$  then execute  $r_2$ ”;  $r^*$  means “execute  $r$  a non deterministically chosen number of times (zero or more)”;  $\phi?$  means “test  $\phi$ : if it is true proceed else fail”.

The main difference between PDLs (and modal logics in general) and classical logics relies on the use of modalities. A modality is a connective which takes a formula (or a set of formulas) and produces a new formula with a new meaning. Examples of modalities are  $\langle r \rangle$  and  $[r]$ . The classical logic operator  $\neg$ , too, is a connective, which takes a formula  $p$  and produces a new formula  $\neg p$ . The only difference is that in classical logic, the truth value of  $\neg p$  is uniquely determined by the value of  $p$ , instead modalities are not truth-functional. Because of modalities, the semantics of PDL formulas (and modal logics) is defined over a structure, namely a Kripke structure.

The semantics of a DPDL formula is based on a the notion of deterministic Kripke structure. A deterministic Kripke structure is a triple of the form  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \mathcal{A}}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$ , where  $\Delta^{\mathcal{I}}$  denotes a non-empty set of states (also called worlds);  $\{a^{\mathcal{I}}\}_{a \in \mathcal{A}}$  is a family of partial *functions*  $a^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$  from elements of  $\Delta^{\mathcal{I}}$  to elements of  $\Delta^{\mathcal{I}}$ , each of which denotes the state transitions caused by the atomic program  $a$ <sup>10</sup>;  $P^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$  denotes all the elements of  $\Delta^{\mathcal{I}}$  where  $P$  is true.

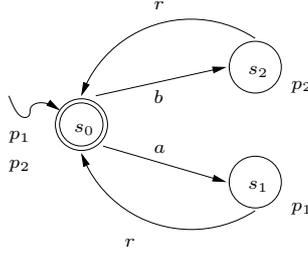
The semantic relation “a formula  $\phi$  holds at a state  $s$  of a structure  $\mathcal{I}$ ”, is written  $\mathcal{I}, s \models \phi$ , and is defined by induction on the form of  $\phi$ :

$$\begin{aligned} \mathcal{I}, s &\models \mathbf{true} && \text{always} \\ \mathcal{I}, s &\models \mathbf{false} && \text{never} \\ \mathcal{I}, s &\models P && \text{iff } s \in P^{\mathcal{I}} \\ \mathcal{I}, s &\models \neg\phi && \text{iff } \mathcal{I}, s \not\models \phi \\ \mathcal{I}, s &\models \phi_1 \wedge \phi_2 && \text{iff } \mathcal{I}, s \models \phi_1 \text{ and } \mathcal{I}, s \models \phi_2 \\ \mathcal{I}, s &\models \phi_1 \vee \phi_2 && \text{iff } \mathcal{I}, s \models \phi_1 \text{ or } \mathcal{I}, s \models \phi_2 \\ \mathcal{I}, s &\models \langle r \rangle \phi && \text{iff there is } s' \text{ such that } (s, s') \in r^{\mathcal{I}} \text{ and } \mathcal{I}, s' \models \phi \\ \mathcal{I}, s &\models [r] \phi && \text{iff for all } s', (s, s') \in r^{\mathcal{I}} \text{ implies } \mathcal{I}, s' \models \phi \end{aligned}$$

where the family  $\{a^{\mathcal{I}}\}_{a \in \mathcal{A}}$  is systematically extended so as to include, for every program  $r$ , the corresponding function  $r^{\mathcal{I}}$  defined by induction on the form of  $r$ :

$$\begin{aligned} a^{\mathcal{I}} &\subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}} \\ (r_1 \cup r_2)^{\mathcal{I}} &= r_1^{\mathcal{I}} \cup r_2^{\mathcal{I}} \\ (r_1; r_2)^{\mathcal{I}} &= r_1^{\mathcal{I}} \circ r_2^{\mathcal{I}} \\ (r^*)^{\mathcal{I}} &= (r^{\mathcal{I}})^* \\ (\phi?)^{\mathcal{I}} &= \{(s, s) \in \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}} \mid \mathcal{I}, s \models \phi\} \end{aligned}$$

<sup>10</sup> Note that the determinism of the Kripke structure derives from the fact that  $a^{\mathcal{I}}$  assigns to each state in  $\Delta^{\mathcal{I}}$  a unique successor state.



**Fig. 15.** Kripke structure for Example 11.

*Example 11.* Let  $\mathcal{P} = \{p_1, p_2\}$  be the set of atomic propositions, let  $\mathcal{A} = \{a, b, r\}$  be the set of atomic actions and let  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \mathcal{A}}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$  be the Kripke structure shown in Figure A with:

$$\begin{aligned}
 \Delta^{\mathcal{I}} &= \{s_0, s_1, s_2\} \\
 \{a^{\mathcal{I}}\} &= \{(s_0, s_1)\} \\
 \{b^{\mathcal{I}}\} &= \{(s_0, s_2)\} \\
 \{r^{\mathcal{I}}\} &= \{(s_1, s_0), (s_2, s_0)\} \\
 \{p_1^{\mathcal{I}}\} &= \{s_0, s_1\} \\
 \{p_2^{\mathcal{I}}\} &= \{s_0, s_2\}
 \end{aligned}$$

It is easy to see that in this structure,  $s_0 \models [a]p_1 \wedge [b]p_2 \wedge [r]\mathbf{false}$ ,  $s_1 \models [r](p_1 \wedge p_2)$ , and  $s_2 \models [r](p_1 \wedge p_2)$ .

It is important to understand, given a formula  $\phi$ , which are the formulas that play some role in establishing the truth-value of  $\phi$ . In simpler modal logics, these formulas are simply all the subformulas of  $\phi$ , but due to the presence of reflexive-transitive closure (on actions) this is not the case for PDLs. Such a set of formulas is given by the Fischer-Ladner closure [11].

A structure  $\mathcal{I} = (\Delta^{\mathcal{I}}, \{a^{\mathcal{I}}\}_{a \in \mathcal{A}}, \{P^{\mathcal{I}}\}_{P \in \mathcal{P}})$  is called a *model* of a formula  $\phi$  if there exists a state  $s \in \Delta^{\mathcal{I}}$  such that  $\mathcal{I}, s \models \phi$ . A formula  $\phi$  is *satisfiable* if there exists a model of  $\phi$ , otherwise the formula is *unsatisfiable*. A formula  $\phi$  is *valid* in structure  $\mathcal{I}$  if for all  $s \in \Delta^{\mathcal{I}}$ ,  $\mathcal{I}, s \models \phi$ . We call *axioms* formulas that are used to select the interpretations of interest. Formally, a structure  $\mathcal{I}$  is a model of an axiom  $\phi$ , if  $\phi$  is valid in  $\mathcal{I}$ . A structure  $\mathcal{I}$  is a model of a finite set of axioms  $\Gamma$  if  $\mathcal{I}$  is a model of all axioms in  $\Gamma$ . An axiom is satisfiable if it has a model and a finite set of axioms is satisfiable if it has a model. We say that a finite set  $\Gamma$  of axioms *logically implies* a formula  $\phi$ , written  $\Gamma \models \phi$ , if  $\phi$  is valid in every model of  $\Gamma$ . It is easy to see that satisfiability of a formula  $\phi$  as well as satisfiability of a finite set of axioms  $\Gamma$  can be reformulated by means of logical implication, as  $\emptyset \not\models \neg\phi$  and  $\Gamma \not\models \perp$  respectively.

DPDL enjoys two properties that are of particular interest. The first is the *tree model property*, which says that every model of a formula can be unwound to a (possibly infinite) tree-shaped model (considering domain elements as nodes and partial functions interpreting actions as edges). The second is the *small model property*, which says that every satisfiable formula admits a finite model whose size (in particular the number of domain elements) is at most exponential in the size of the formula itself.

Reasoning in DPDL (and, in general, in PDLs) has been thoroughly studied from the computational point of view. In particular, the following theorem holds [4]:

**Theorem 4.** *Satisfiability in DPDL is EXPTIME-complete.*