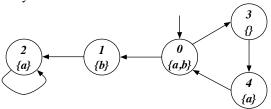
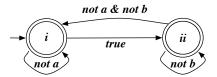
Formal Methods – July 5, 2023

(*Time to complete the test: 2:00 hours*)

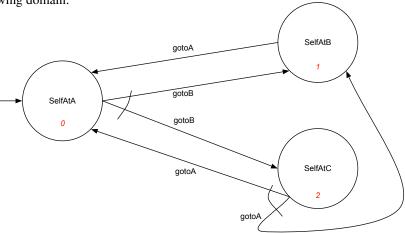
Part 1. Consider the following transition system:



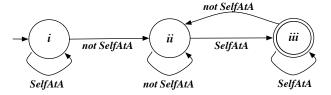
- Exercise 1.1: Model check the Mu-Calculus formula: $\nu X.\mu Y.((a \land \langle next \rangle X) \lor \langle next \rangle Y)$
- Exercise 1.2: Model check the CTL formula $AF(a \wedge AXb)$, by translating it in Mu-Calculus.
- Exercise 1.3: Model check the LTL formula $\diamondsuit(a \land \bigcirc b)$, by considering that the Büchi automaton for $\neg \diamondsuit(a \land \bigcirc b)$ is the one below:



Part 2 Consider the following domain:



• Exercise 2.1: Synthesize a strategy (a plan) for realizing the LTLf formula $\Diamond(\neg SelfAtA \land \Diamond(SelfAtA \land \bullet false))$, by considering that the corresponding DFA is the one below:



Part 3 Check whether the Hoare triple below is correct, by using $(x \ge 0 \land y \ge 0 \land x + y = 23)$ as invariant:

$${x = 23 \land y = 0}$$
 while(x>0) do (x=x-1; y:= y+1) ${y = 23}$