TRANSITION SYSTEMS

Slides by Alessandro Artale http://www.inf.unibz.it/~artale/

Some material (text, figures) displayed in these slides is courtesy of: M. Benerecetti, A. Cimatti, M. Fisher, F. Giunchiglia, M. Pistore, M. Roveri, R.Sebastiani.

Summary of Lecture II

- Types of Systems.
- Modeling Systems as Kripke Models.
- Languages for Describing Kripke Models.
- Properties of Systems.

Concurrent Reactive Systems

We describe here Concurrent Reactive systems.

- Reactive Systems: Systems that interact with their environment and usually do not terminate (e.g. communication protocols, hardware circuits).
- Concurrent Systems consist of a set of components that execute together.
- We distinguish two types of Concurrent Systems:
 - 1. Asynchronous or Interleaved Systems. Only one component makes a step at a time;
 - 2. *Synchronous Systems*. All components make a step at the same time.

Modeling Systems

- We need to construct a *Formal Specification* of the system which abstract from irrelevant details.
 - **State**: Snapshot of the system that captures the values of the variables at a particular point in time.
 - System Transition: How the state of the system evolves as the result of some action.
 - **Computation**: Infinite sequence of states along the different transitions.

- Types of Systems.
- Modeling Systems as Kripke Models.
- Languages for Describing Kripke Models.
- Properties of Systems.

Modeling Systems with Kripke Structures

- Kripke Structures are transition diagrams that represent the dynamic behavior of a reactive system.
- Kripke Structures consist of a set of states, a set of transitions between states, and a set of properties labeling each state.
- A path in a Kripke structure represents a computation of the system.

Kripke model: definition

- \triangleright Formally, a Kripke model $\langle S, I, R, AP, L \rangle$ consists of
 - a set of states *S*;
 - a set of initial states $I \subseteq S$;
 - a set of transitions $R \subseteq S \times S$;
 - a set of atomic propositions AP;
 - a labeling function $L: S \mapsto 2^{AP}$.
- \triangleright A path in a Kripke model *M* from a state s_0 is an infinite sequence of states

$$\pi = s_0, s_1, s_2, \ldots$$

such that $(s_i, s_{i+1}) \in R$, for all $i \ge 0$.

Example: Kripke model for mutual exclusion

- We model two concurrent asynchronous processes sharing a resource ensuring they do not access it at the same time.
- Each process has *critical sections* in its code and only one process can be in its critical section at a time.
- We want to find a *protocol* for mutual exclusion which, for example, guarantee the following properties:
 Safety: Only one process is in its critical section at a time.
 - **Liveness:** Whenever any process requests to enter its critical section it will *eventually* be permitted to do so.

Non-Blocking: A process can always request to enter its critical section.



Example: a Kripke model for mutual exclusio

Each process can be in its non-critical state (N), or trying to enter its critical state (T), or in its critical state (C). The variable **turn** considers the *first* process that went into its trying state.



Composing Kripke Models

- Complex Kripke Models are tipically obtained by composition of smaller ones
- Components can be combined via
 - synchronous composition
 - asynchronous composition.

Synchronous Composition

- ▷ Components evolve in parallel.
- At each time instant, every component performs a transition.



▷ Typical example: sequential hardware circuits.



Asynchronous Composition

- Interleaving of evolution of components.
- At each time instant, one component is selected to perform a transition.



> Typical example: communication protocols.

- Types of Systems.
- Modeling Systems as Kripke Models.
- Languages for Describing Kripke Models.
- Properties of Systems.

Description languages for Kripke Model

Tipically a Kripke model is not given explicitly, rather it is usually presented in a structured language (e.g., NuSMV, SDL, PROMELA, StateCharts, VHDL, ...) Each component is presented by specifying:

- A set of system variables
- Initial values for state variables
- Instructions

Description languages for Kripke Model

The correspondence between a description language and the Kripke Model is the following:

- States: all possible assignments for system variables;
- Initial States: Initial values for system variables;
- Transitions: Instructions;
- Atomic Propositions: Propositions associated to the values of the system variables;
- Labeling: Set of atomic propositions true at a state.

The NuSMV language

- The NuSMV (New Symbolic Model Verifier) model-checking system is an Open Source product (<u>nusmv.irst.itc.it</u>).
- An SMV program consists of:
 - Type declarations of the system variables;
 - Assignments that define the valid initial states (e.g., init(b0) := 0).
 - Assignments that define the transition relation (e.g., next(b0) := !b0).

NuSMV: The modulo 4 counter with reset

```
MODULE main
VAR
         : boolean;
  b0
                                               1
                                    0
         : boolean;
  b1
  reset : boolean;
         : 0...3;
  out
ASSIGN
  init(b0) := 0;
                                               2
                                    3
  next(b0)
            := case
                reset = 1: 0;
                reset = 0:
                             !b0;
               esac;
  init(b1)
            := 0;
  next(b1)
            := case
                reset: 0;
                     : ((!b0 & b1) | (b0 & !b1));
                1
               esac;
  out := b0 + 2*b1;
```

Summary

- Types of Systems.
- Modeling Systems as Kripke Models.
- Languages for Describing Kripke Models.
- Properties of Systems.

p 17/21

Safety Properties

- Nothing Bad Ever Happens.
 - Deadlock: two processes waiting for input from each other, the system is unable to perform a transition.
 - No reachable state satisfies a "bad" condition, e.g. never two processes in critical section at the same time
- It is expressed by a temporal formula saying that "it's never the case that p".



Liveness Properties

- Something Desirable Will Eventually Happen.
 - Whenever a subroutine takes control, it will always return it (sooner or later).
- It is expressed by a temporal formula saying that "at each state it will be the case that p".
- Can be refuted by infinite behaviour (represented as a loop)



Summary of Lecture II

- Types of Systems.
- Modeling Systems as Kripke Models.
- Languages for Describing Kripke Models.
- Properties of Systems.