

# Autonomous and Mobile Robotics

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## Wheeled Mobile Robots 3

# Path/Trajectory Planning

companion slides for the blackboard lecture

DIPARTIMENTO DI INGEGNERIA INFORMATICA  
AUTOMATICA E GESTIONALE ANTONIO RUBERTI

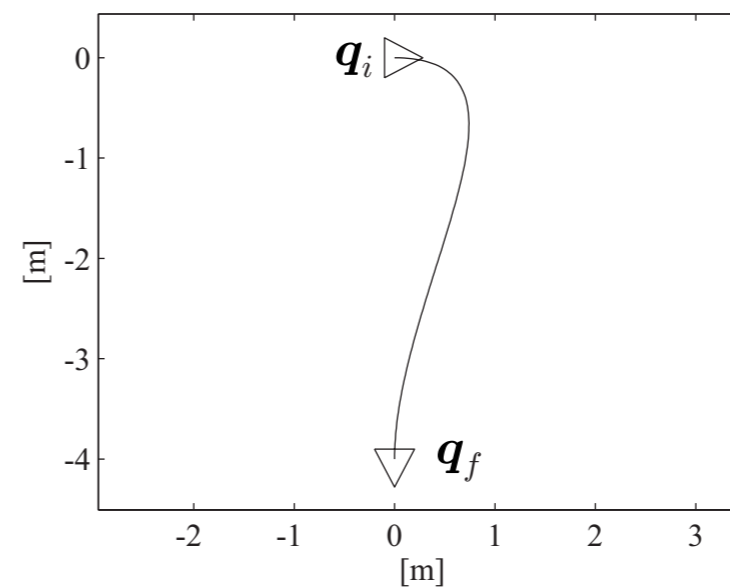
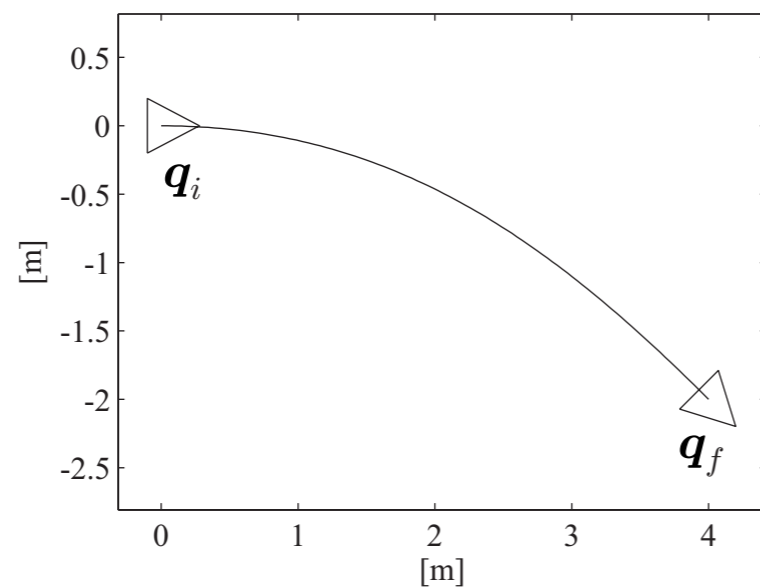


SAPIENZA  
UNIVERSITÀ DI ROMA

# parking a unicycle: numerical results

## I. forward parking

cubic polynomials for cartesian coords  $x, y$  (flat outputs)

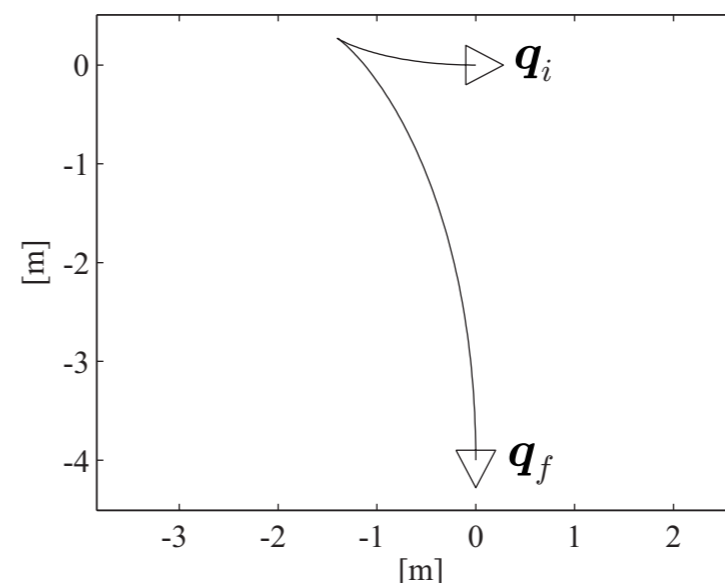
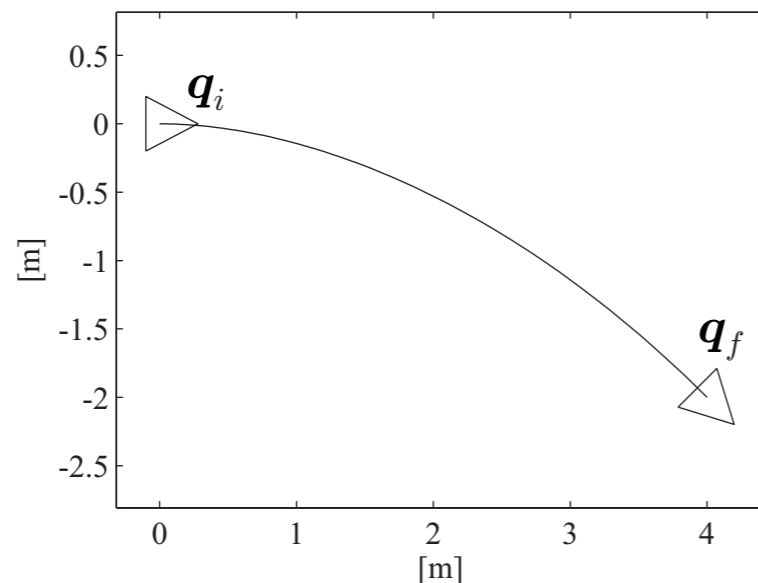


- $k=5 > 0$ , hence forward motion
- no motion inversions

# parking a unicycle: numerical results

## I. forward parking

parameterized inputs on chained form

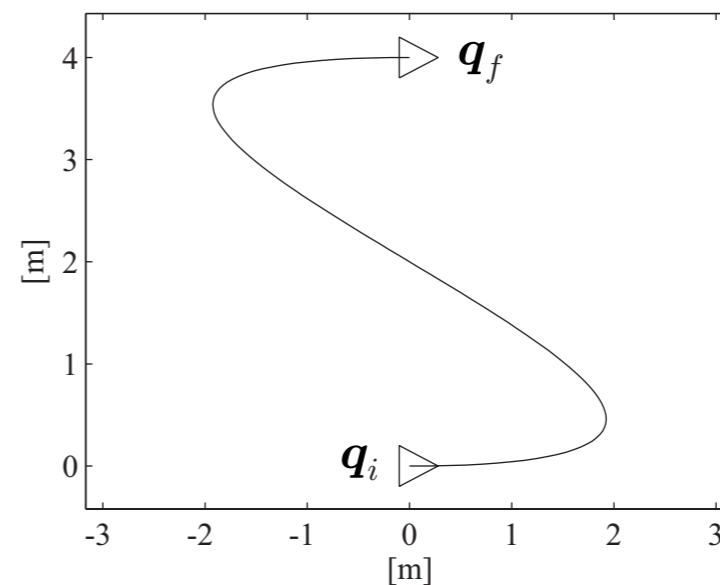
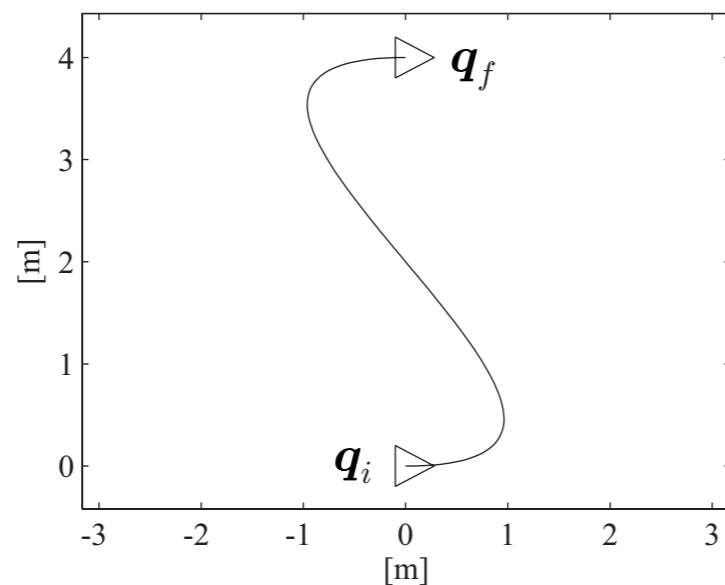


- first maneuver is similar
- a motion inversion (cusp) in the second

# parking a unicycle: numerical results

## 2. parallel parking

cubic polynomials for cartesian coords  $x, y$  (flat outputs)

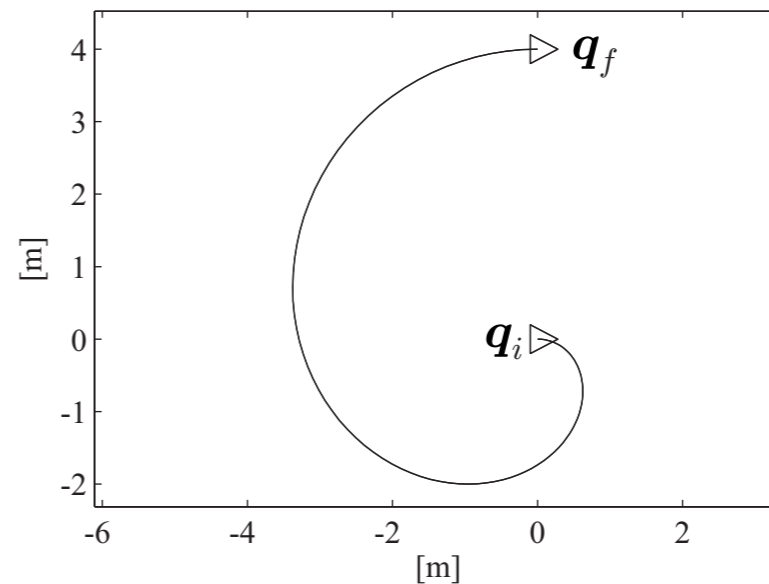
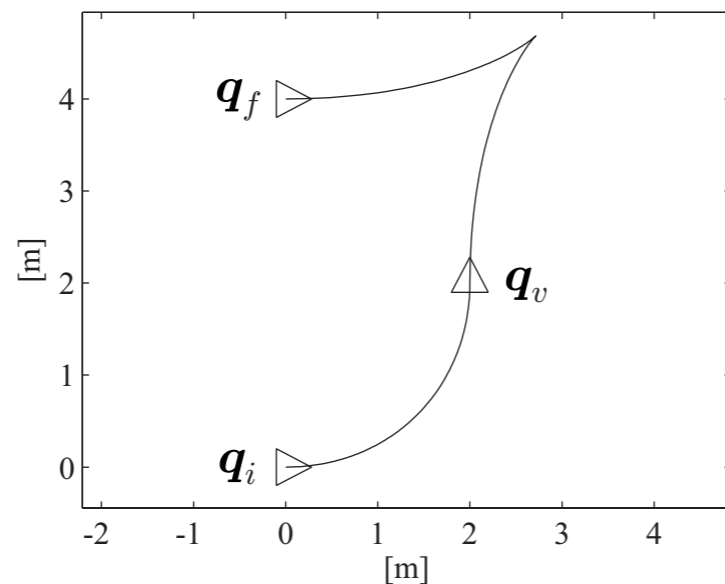


- left:  $k=10$ , right:  $k=20$
- no motion inversions

# parking a unicycle: numerical results

## 2. parallel parking

parameterized inputs on chained form

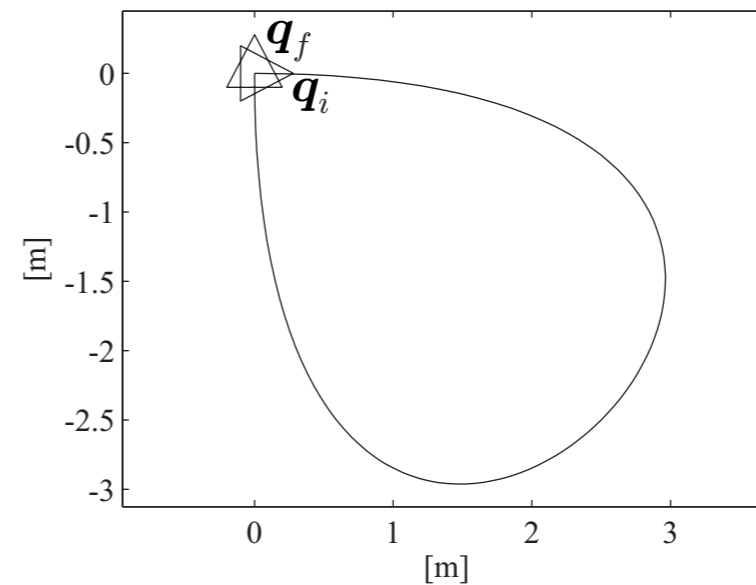
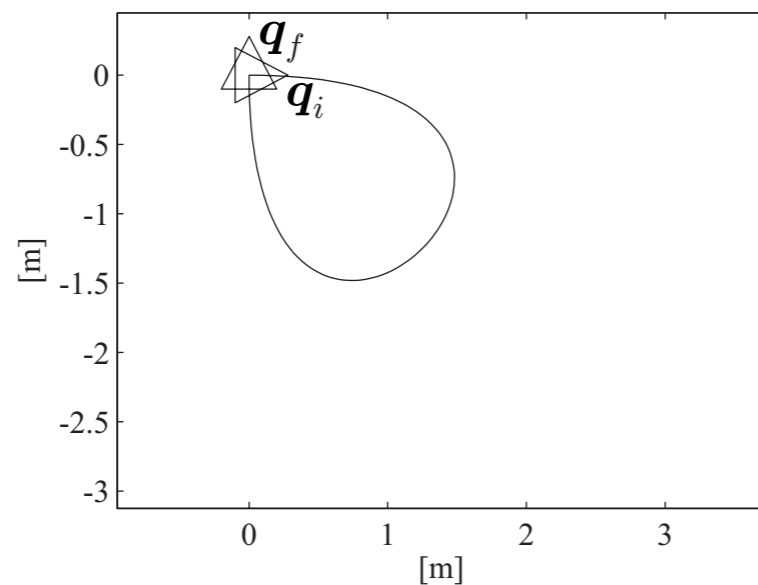


- left: with a via point
- right: requiring a full rotation

# parking a unicycle: numerical results

## 3. pure reorientation

cubic polynomials for cartesian coords  $x, y$  (flat outputs)

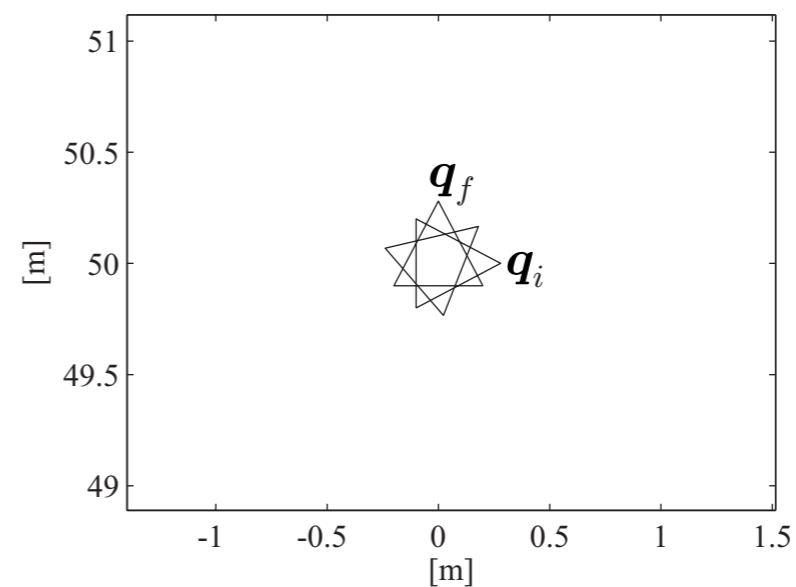
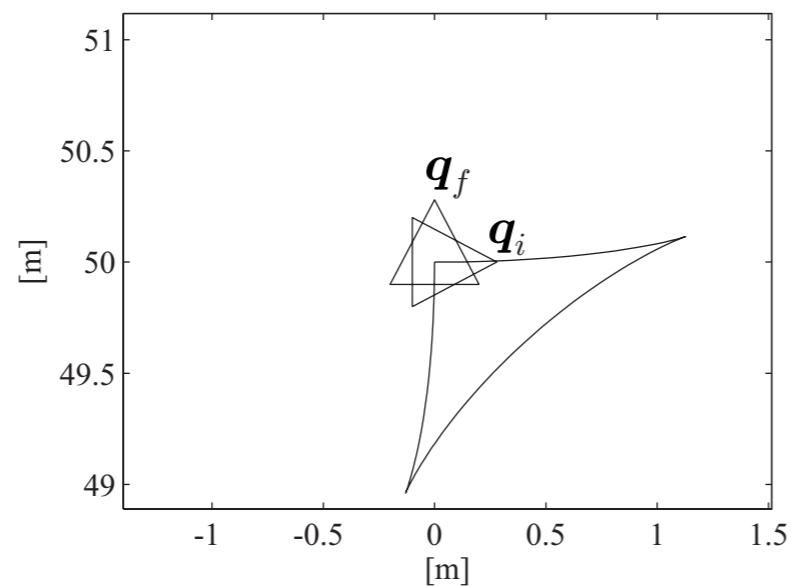


- left:  $k=10$ , right:  $k=20$
- need to move the cartesian coordinates!

# parking a unicycle: numerical results

## 3. pure reorientation

parameterized inputs on chained form



- left: straightforward
- right: placing the origin of  $z_2, z_3$  at  $q_i$