



Robotics 1

Robot components: Introduction, Actuators, Transmissions

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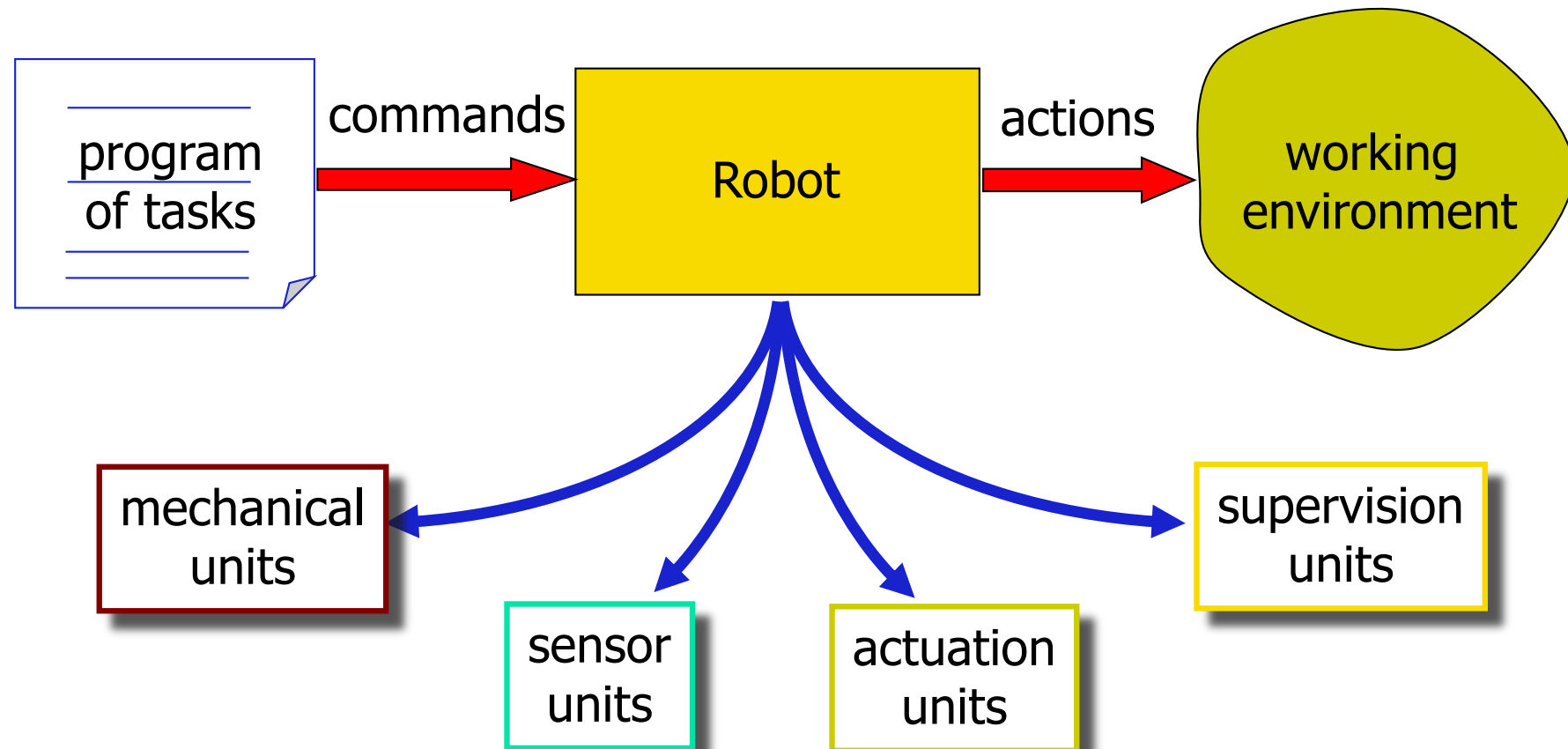
DIPARTIMENTO DI INGEGNERIA INFORMATICA
AUTOMATICA E GESTIONALE ANTONIO RUBERTI



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Robot as a system





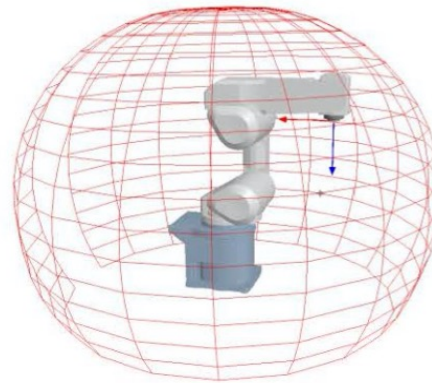
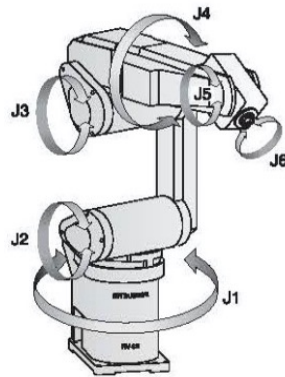
Functional units of a robot

- mechanical units (robot arms)
 - serial manipulators: rigid links connected via **rotational** or **prismatic** joints (each giving 1 degree of freedom = DOF, **R** or **P** type)
 - **supporting structure** (mobility), **wrist** (dexterity), **end-effector** (for task execution, e.g., manipulation)
- actuation units
 - motors (**electrical**, **hydraulic**, **pneumatic**) and transmissions
 - motion control algorithms
- sensor units
 - **proprioceptive** (internal robot state: position and velocity of the joints)
 - **exteroceptive** (external world: force and proximity, vision, ...)
- supervision units
 - task **planning** and **control**
 - artificial intelligence and reasoning

Arrangement of mechanical links

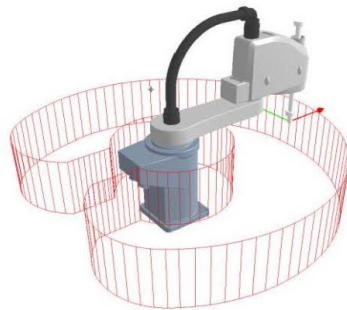
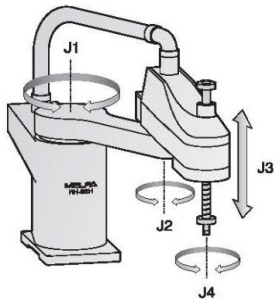
4, 5, or 6
joints
(DOFs)

Articulated Robot

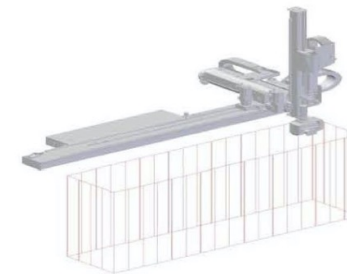
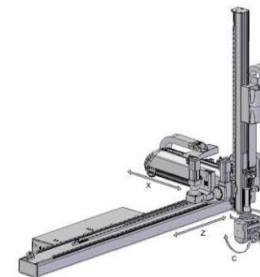


different
kinematic
types of
robot arms

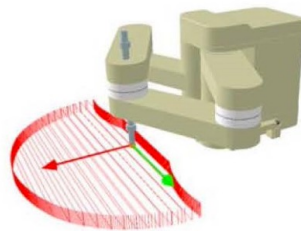
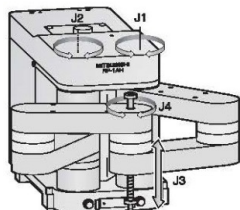
SCARA Robot



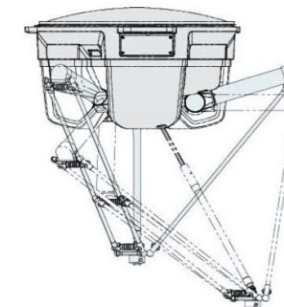
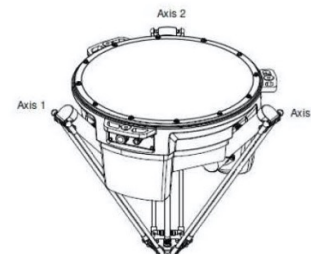
Cartesian Robot



SCARA Robot



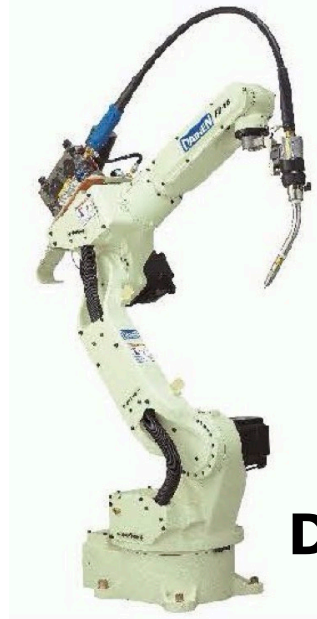
Parallel/Delta Robot



Examples of industrial robots with brands



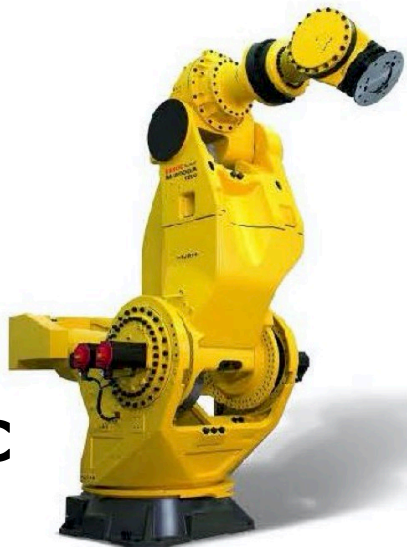
ABB



DAIHEN



EPSON



FANUC



KUKA



NAICHI

Bi-manual industrial robots

with brands

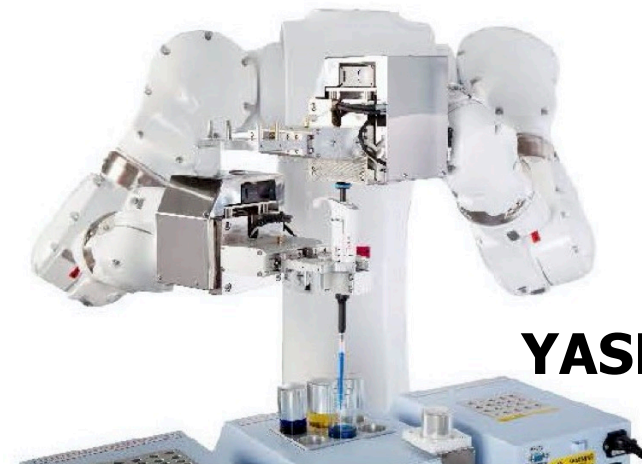


ABB



COMAU

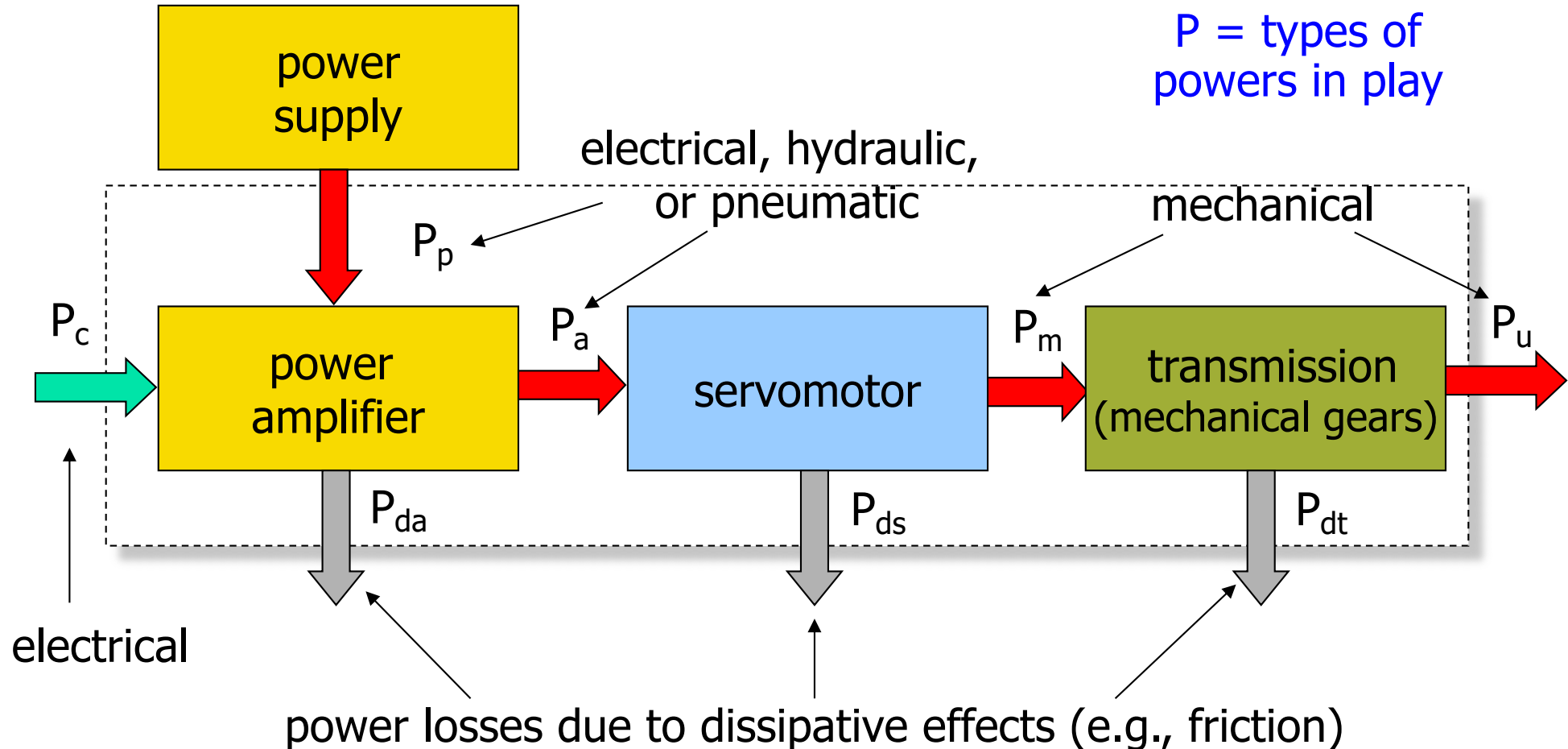
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ROBOTS**



YASHKAWA



Actuation systems



power = voltage · current = pressure · flow rate = force · speed = torque · angular speed [W, Nm/s]

efficiency = power out/power in [%] **energy** ~ **work** = power · time [kWh, Nm, J]

Desired characteristics for robot servomotors



- low inertia
- high power-to-weight ratio
- high acceleration capabilities
 - variable motion regime, with several stops and inversions
- large range of operational velocities
 - 1 to 2000 rpm (round per min)
- high accuracy in positioning
 - at least 1/1000 of a turn
- low torque ripple
 - continuous rotation at low speed
- power: 10 W to 10 kW
 - max 80W for HRI applications

examples of computations (with reduction ratio):

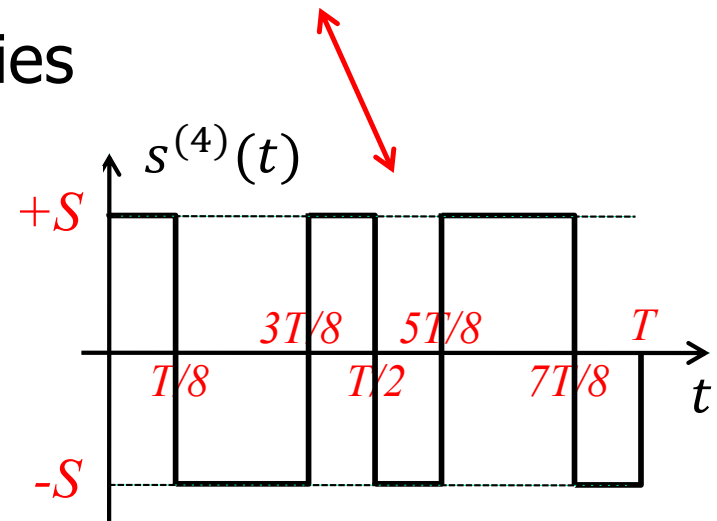
2000 rpm ~ 12500 rad/min = 210 rad/s $\rightarrow$

reduction ratio $n_r = 50 \rightarrow$

~ 4 rad/s = 240 deg/s on link side

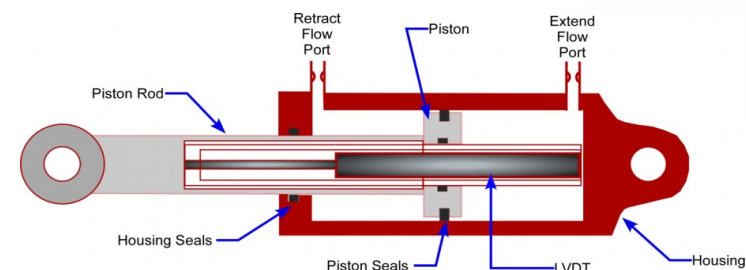
1/1000 turn ~ 6 mrad = 0.36 deg $\rightarrow$

reduction ratio $n_r = 50 \rightarrow 7.2$ mdeg on link side



Servomotors

- **pneumatic:** pneumatic energy (compressor) → pistons or chambers → mechanical energy
 - difficult to control accurately (change of fluid compressibility) → no trajectory control
 - used for opening/closing grippers
 - ... or as artificial muscles (McKibben actuators)
- **hydraulic:** hydraulic energy (accumulation tank) pumps/valves → mechanical energy
 - **advantages:** no static overheating, self-lubricated, inherently safe (no sparks), excellent power-to-weight ratio, large torques at low velocity (w/o reduction)
 - **disadvantages:** needs hydraulic supply, large size, linear motion only, low power conversion efficiency, high cost, increased maintenance (oil leaking)



Electrical servomotors

■ advantages

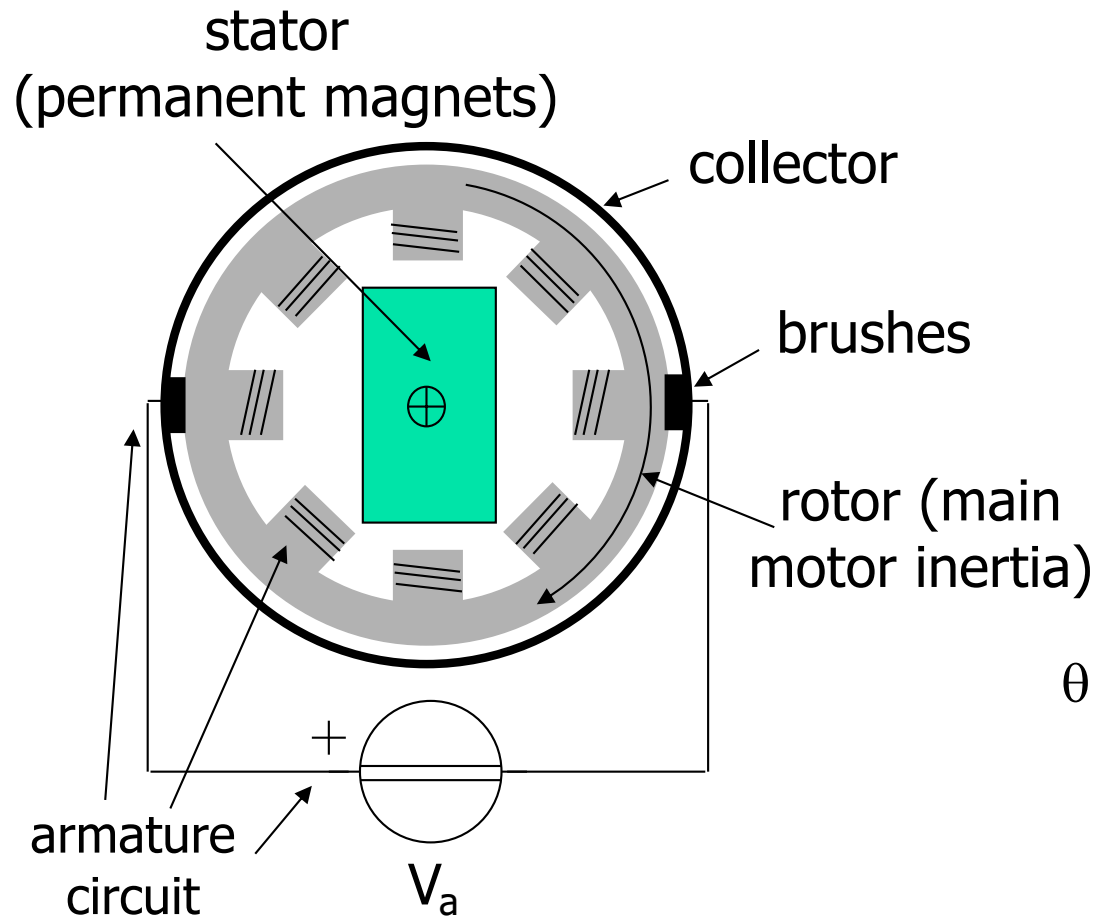
- power supply available everywhere
- low cost
- large variety of products
- high power conversion efficiency
- easy maintenance
- no pollution in working environment

■ disadvantages

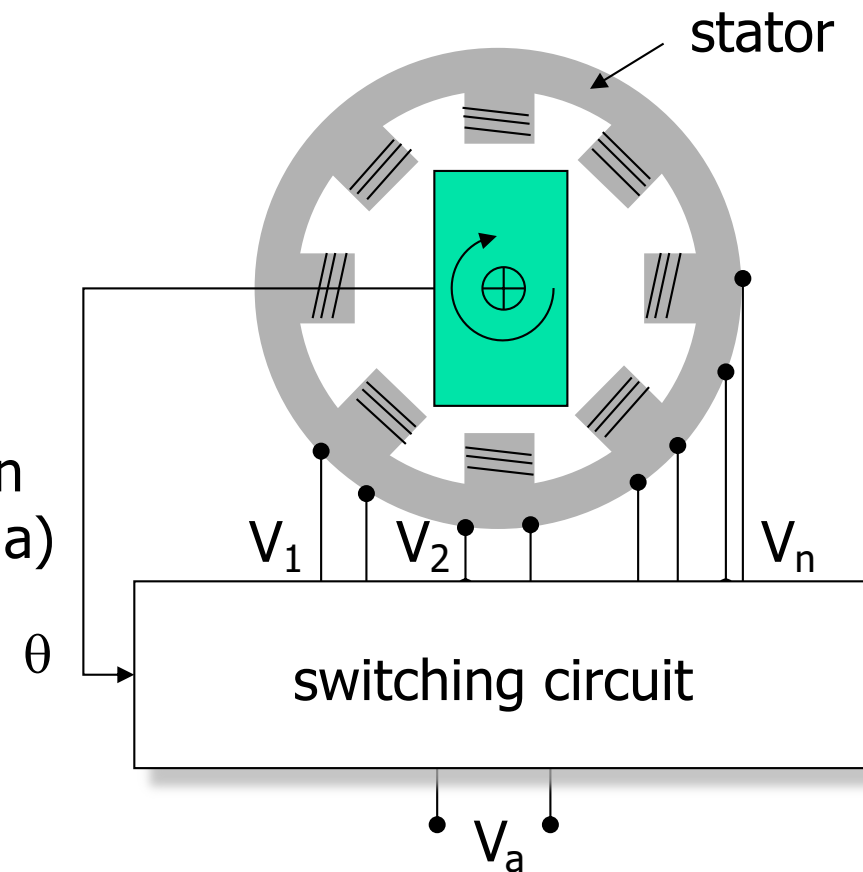
- overheating in static conditions (in the presence of gravity)
 - use of (emergency) brakes
- need special protection in flammable environments
- some advanced models require more complex control laws



Electrical servomotors for robots



direct current (DC) motor



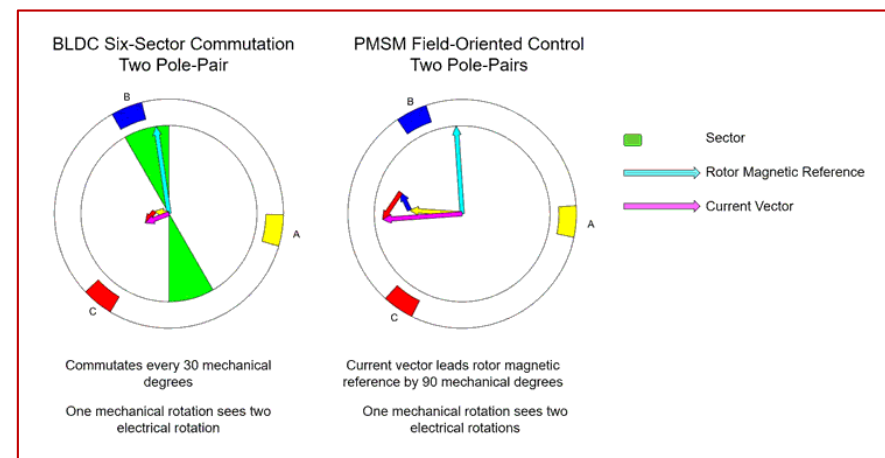
with electronic switches (brushless)

Advantages of brushless motors

- reduced losses, both electrical (due to tension drops at the collector-brushes contacts) and mechanical (friction)
- reduced maintenance (no substitution of brushes)
- easier heat dissipation
- more compact rotor (less inertia and smaller dimensions)

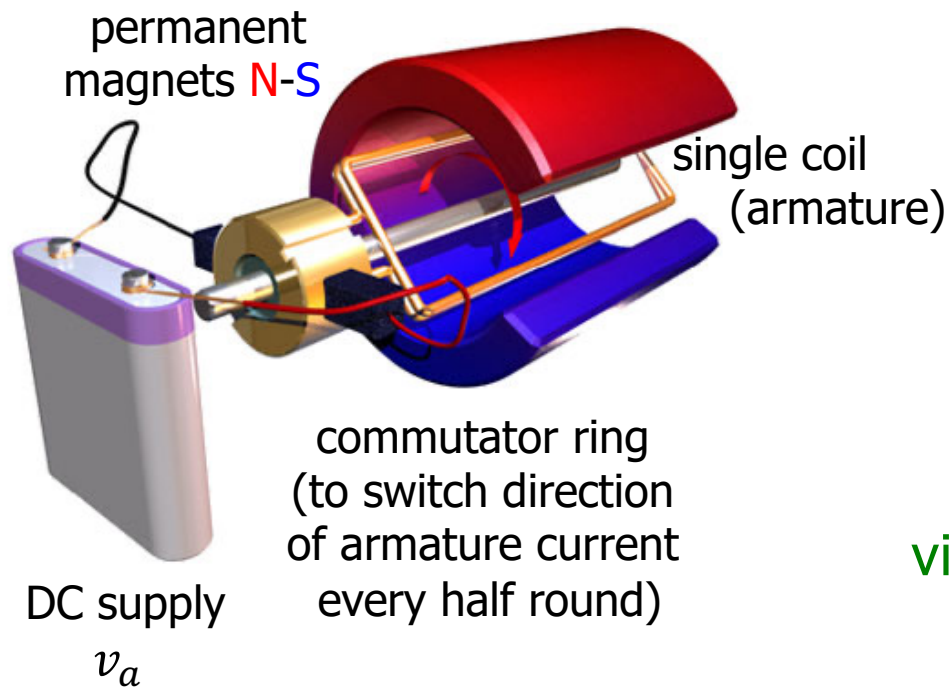
... but, indeed a higher cost!

BLDC = BrushLess DC motors

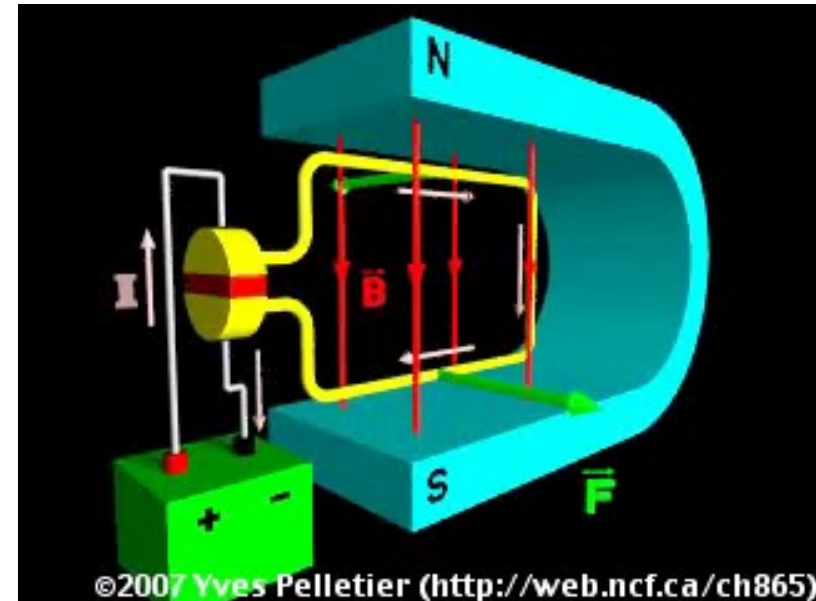


MATLAB animation

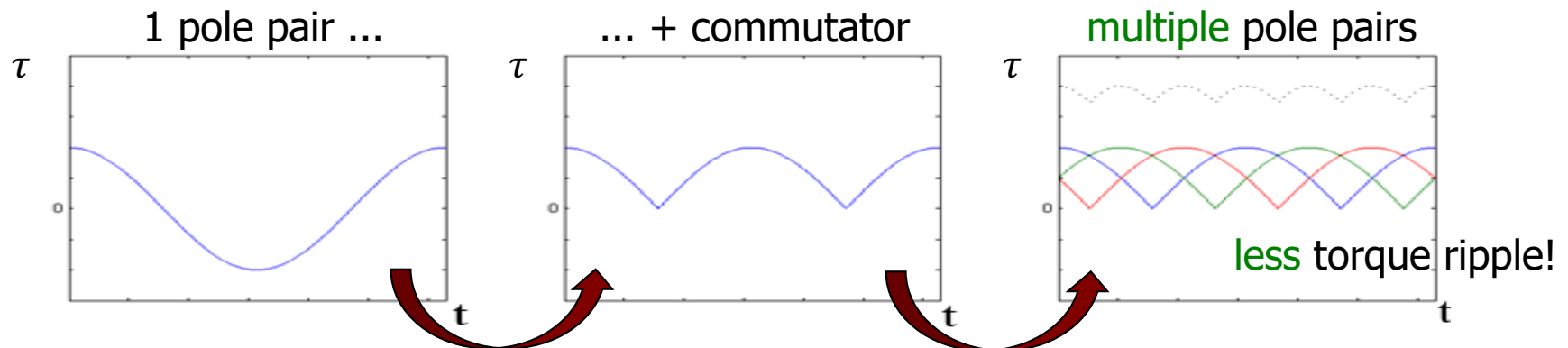
Principle of operation of a DC motor



video



$$\vec{F} = L(\vec{i} \times \vec{B}) \quad \tau = d|\vec{F}|$$





DC electrical motor

mathematical model (in the time domain)

electrical balance
(on the equivalent armature circuit)

$$v_a(t) = R_a i_a(t) + L_a \frac{di_a(t)}{dt} + v_{emf}(t)$$

$$v_{emf}(t) = k_v \omega(t)$$

(back emf)

mechanical balance
(Newton law on torques)

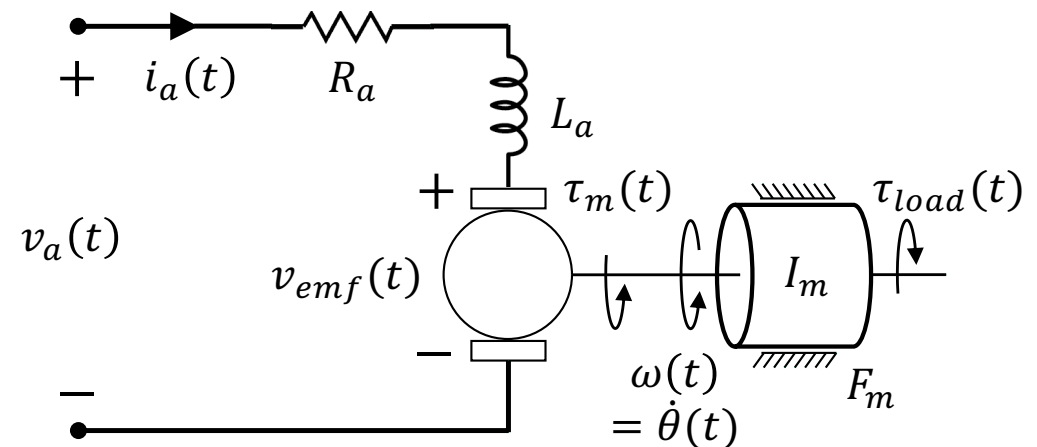
$$\tau_m(t) = I_m \frac{d\omega(t)}{dt} + F_m \omega(t) + \tau_{load}(t)$$

$$\tau_m(t) = k_t i_a(t)$$

(motor torque)

in the absence of losses, **conservation of power** holds in energy transformations

$$P_{elec} = v_{emf} i_a = \tau_m \omega = P_{mecc}$$
$$\Rightarrow k_v = k_t \quad (\text{in SI units})$$



using Laplace transform, differential equations become **algebraic relations!**

$$X(s) = \mathcal{L}[x(t)] = \int_0^{\infty} x(t) e^{-st} dt$$



DC electrical motor

mathematical model for command and control

electrical balance

$$V_a = (R_a + sL_a) I_a + V_{emf}$$

$$V_{emf} = k_v \Omega$$

Laplace domain (transfer functions)

time constants

$$\tau_{elec} = \frac{L_a}{R_a} \ll \frac{I_m}{F_m} = \tau_{mecc}$$

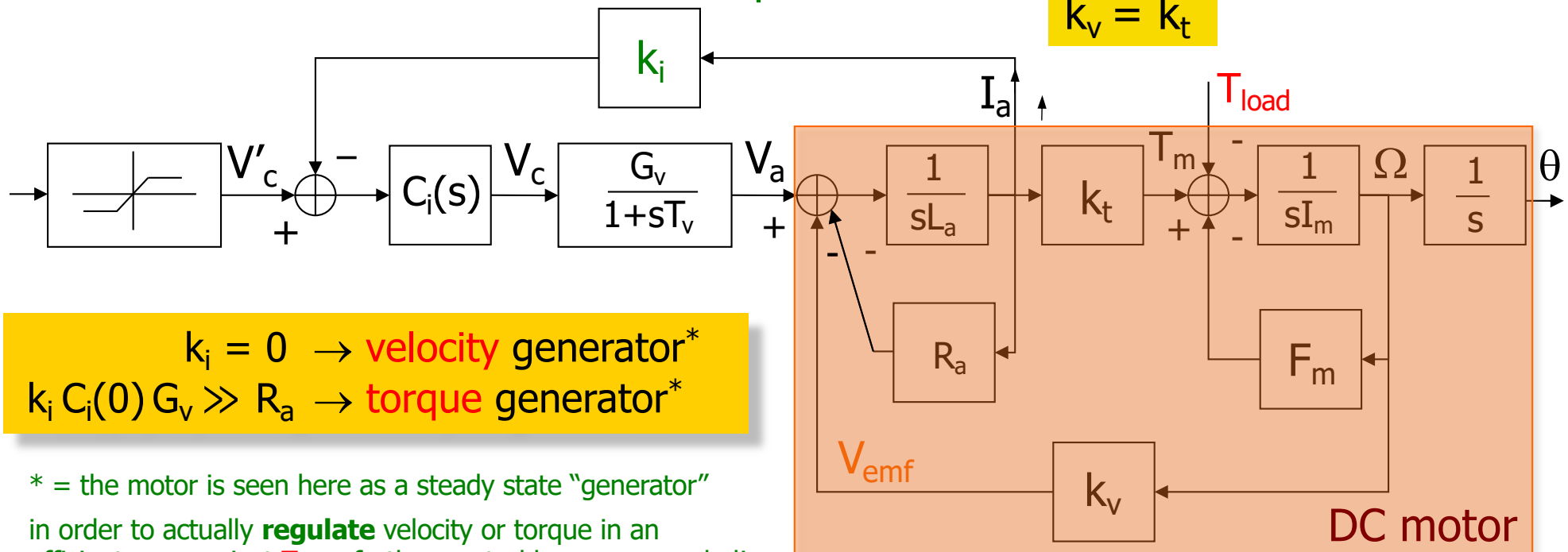
mechanical balance

$$T_m = (sI_m + F_m) \Omega + T_{load}$$

$$T_m = k_t I_a$$

$$k_v = k_t$$

current loop



$k_i = 0 \rightarrow$ **velocity** generator*

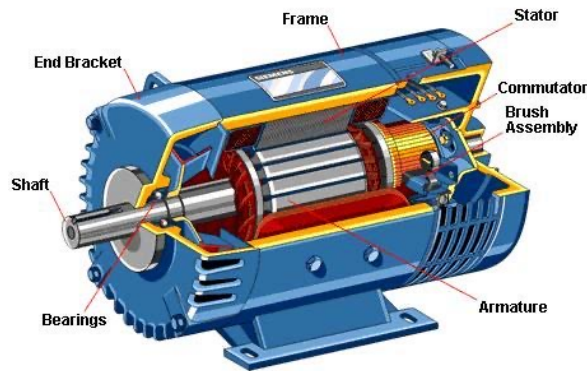
$k_i C_i(0) G_v \gg R_a \rightarrow$ **torque** generator*

* = the motor is seen here as a steady state "generator"
in order to actually **regulate** velocity or torque in an efficient way against T_{load} , further control loops are needed!

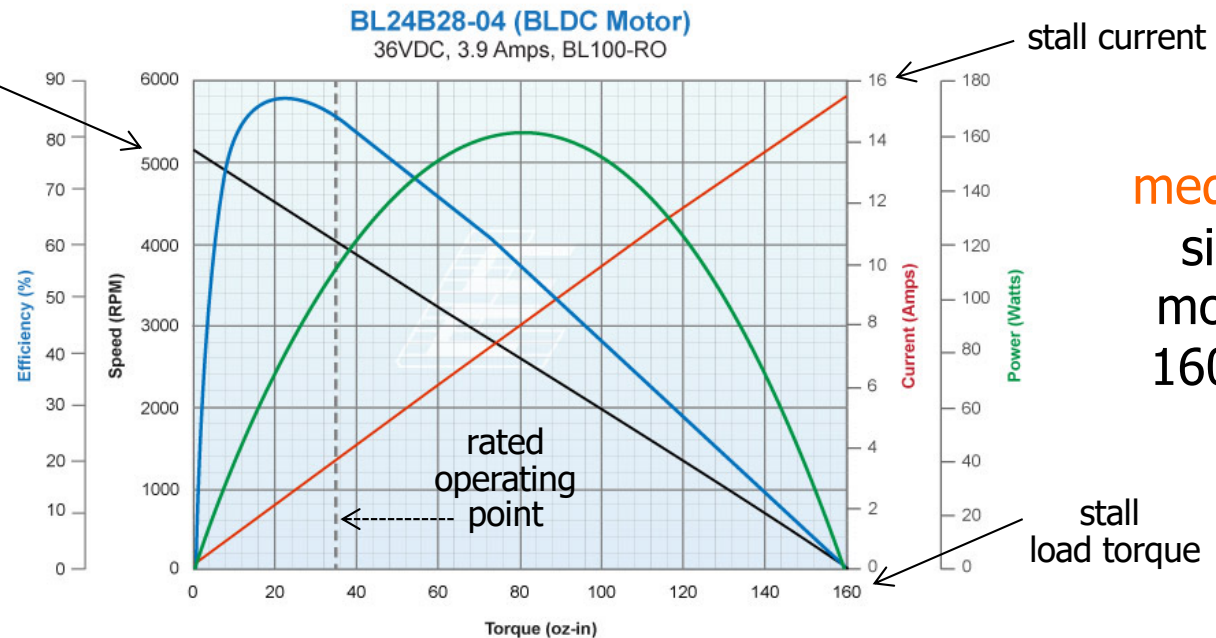


Characteristic curves of a DC motor

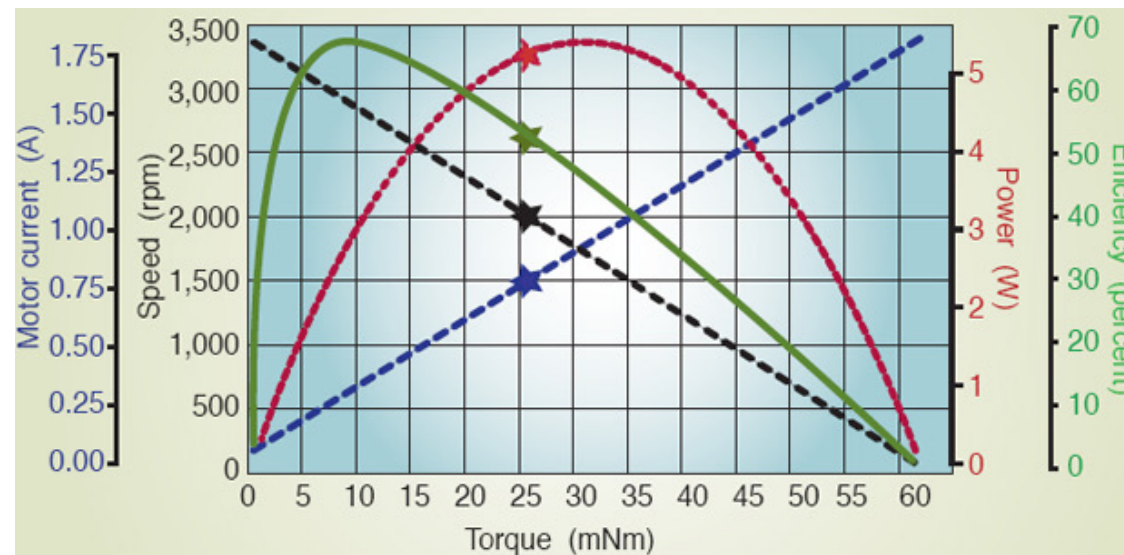
at steady-state,
for **constant**
applied tension v_a



no-load
max speed



conversion SI $\Leftrightarrow$ US
unit systems (!!)
1 Nm = 141.61 oz-in
100 oz-in = 0.70 Nm



Data sheet electrical motors

- DC drives



Model of actuator		RHS-14		RHS-17		RHS-20/RFS-20				RHS-25/RFS-25				RHS-32/RFS-32			
		6003	3003	6006	3006	6007	3007	6012	3012	6012	3012	6018	3018	6018	3018	6030	3030
Rated Torque	Inlb	48	69	87	177	106	212	177	266	177	354	266	531	266	531	443	885
	Nm	5.4	7.8	9.8	20	12	24	20	30	20	40	30	60	30	60	50	100
Rated Speed of Rotation	rpm	60	30	60	30	60	30	60	30	60	30	60	30	60	30	60	30
Max. Instant. Torque	Inlb	159	248	301	478	504	743	504	743	885	1416	885	1416	1947	3009	1947	3009
	Nm	18	28	34	54	57	84	57	84	100	160	100	160	220	340	220	340
Max.Speed of Rotation	rpm	100	50	80	40	80	40	80	40	80	40	80	40	80	40	80	40

nominal/peak torques and speeds

Data sheet electrical motors

■ AC drives



	unit	HKM-20-60	HKM-20-30	HKM-25-60	HKM-25-30
Rated Power	Watts	100		200	
Rated Torque	in-lb	115	223	233	440
	N-m	13	26	26	50
Maximum Torque	in-lb	345	700	830	1330
	N-m	39	79	94	150
Rated Speed	r/min	60	30	60	30
Maximum Speed	r/min	80	40	80	40
Current Rated	A	1.8	1.4	4.8	3
Current Max	A	5	4	14	9
Thermal Time Constant	min.				
Gear Reduction Ratio	R:1	50	100	50	100
Output Resolution	P/rev	50,000	100,000	75,000	150,000
	arc sec	26	13	17	9
Absolute Accuracy	+/- arc sec	75	40	60	40

- for applications requiring a rapid and accurate response (in robotics!)
- induction motors driven by alternate current (AC)
- small diameter rotors, with low inertia for fast starts, stops, and reversals



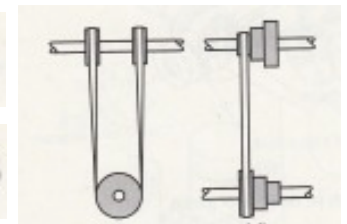
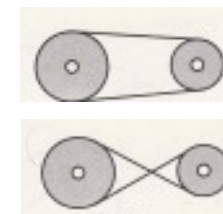
Motion transmission gears

- optimize the transfer of mechanical torque from actuating motors to driven links
- quantitative transformation (from **low torque/high velocity** to **high torque/low velocity**)
- qualitative transformation (e.g., from **rotational** motion of an electrical motor to a **linear** motion of a link along the axis of a prismatic joint)
- allow improvement of static and dynamic performance by reducing the weight of the actual robot structure in motion (locating the motors remotely, closer to the robot base)



Transmissions in robotics

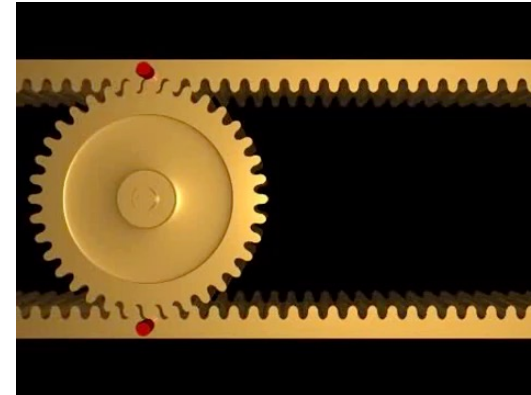
- **spur/bevel gears:** modify direction and/or translate axis of motor displacement
 - problems: **deformations, backlash**
- **lead screws, worm gearing:** convert rotational into translational motion (prismatic joints)
 - problems: **friction, elasticity, backlash**
- **toothed belts and chains:** dislocate the motor w.r.t. the joint axis
 - problems: **compliance** (belts) or **vibrations** induced by larger mass at high speed (chains)
- **harmonic drives:** compact, in-line, power efficient, with high reduction ratio (up to 150-200:1)
 - problems: **elasticity**
- **transmission shafts:** long, inside the links, with flexible couplings for alignment





Transmission gears in motion

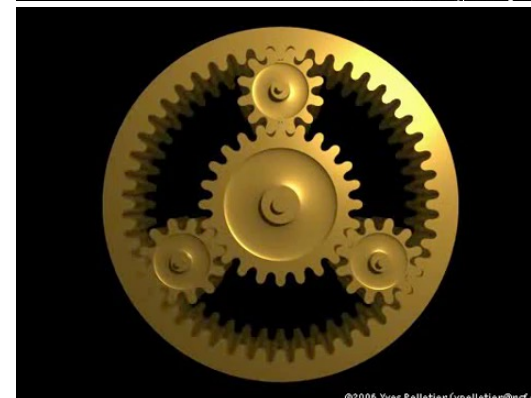
- racks and pinion
 - one rack moving (or both)
- epi-cycloidal gear train
 - or hypo-cycloidal (small gear inside)
- planetary gear set
 - one of three components is locked: sun gear, planet carrier, ring gear



video



video

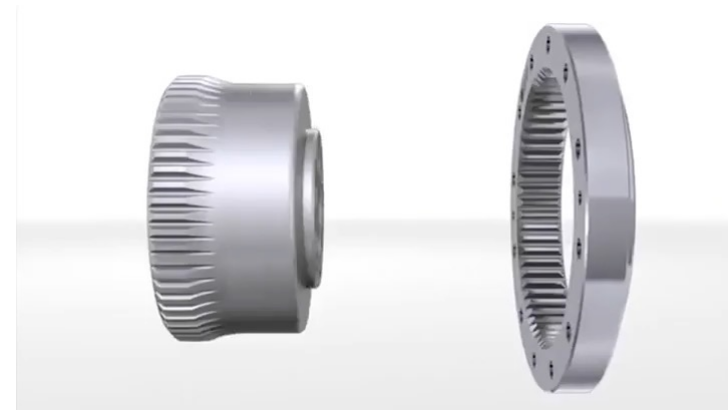
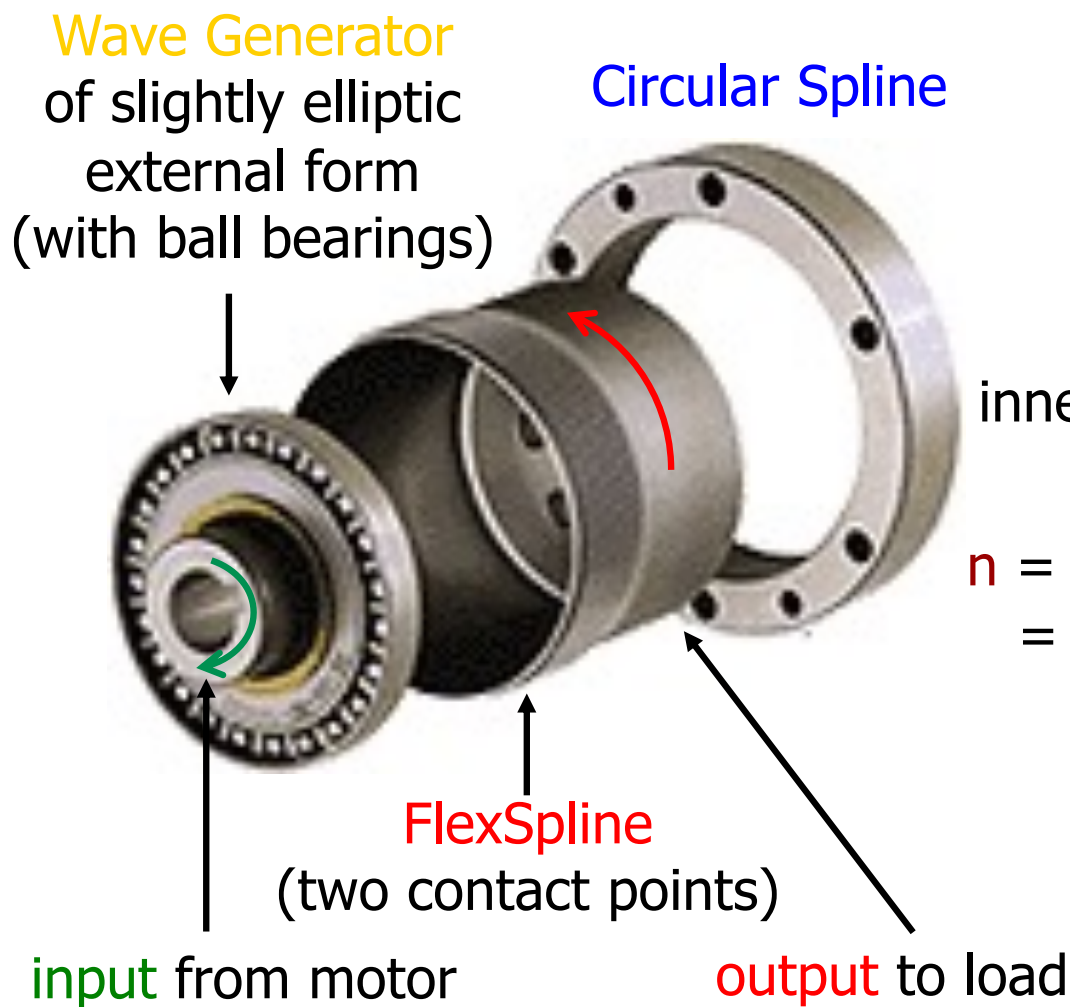


video



Harmonic drives

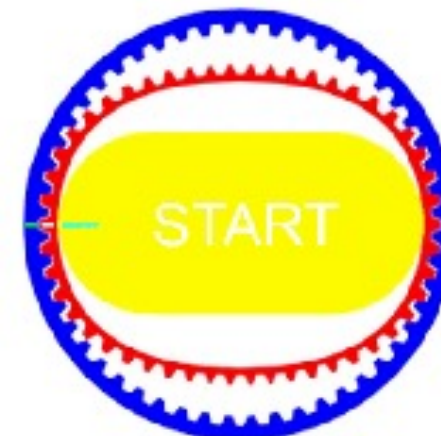
video



$$\text{inner \#teeth CS} = \text{outer \#teeth FS} + 2$$

reduction ratio

$$n = \frac{\text{\#teeth FS}}{(\text{\#teeth CS} - \text{\#teeth FS})}$$
$$= \frac{\text{\#teeth FS}}{2}$$



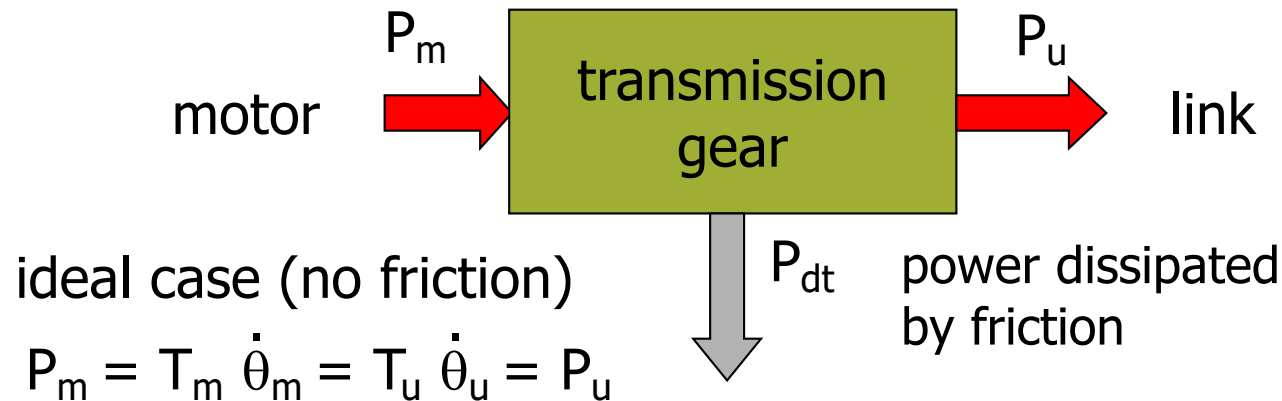


Operation of a harmonic drive

Harmonic Drive Gearing
PRINCIPLE of
OPERATION

commercial **video** by Harmonic Drives AG
(<https://www.youtube.com/watch?v=bzRh672peNk>)

Optimal choice of reduction ratio



$n = \text{reduction ratio } (>> 1) \quad \dot{\theta}_m = n \dot{\theta}_u \quad \Rightarrow \quad T_u = n T_m$

to have $\ddot{\theta}_u = a$ (thus $\ddot{\theta}_m = n a$), the motor should provide a torque

$$T_m = J_m \ddot{\theta}_m + 1/n (J_u \ddot{\theta}_u) = (J_m n + J_u/n) a$$

inertia × angular acceleration

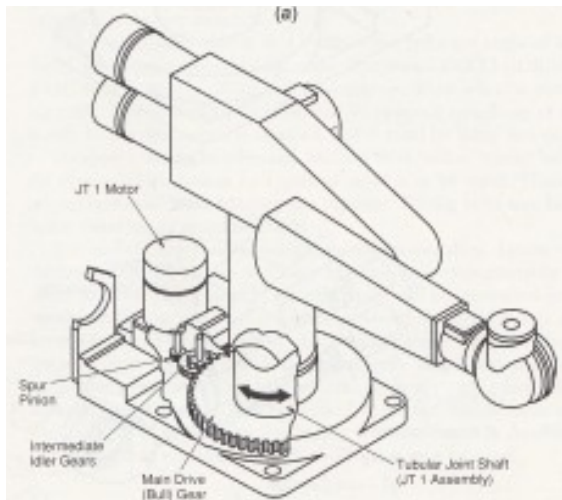
for minimizing T_m , we set: $\frac{\partial T_m}{\partial n} = (J_m - J_u/n^2) a = 0$

→ $n = (J_u / J_m)^{1/2}$ “matching” condition between inertias

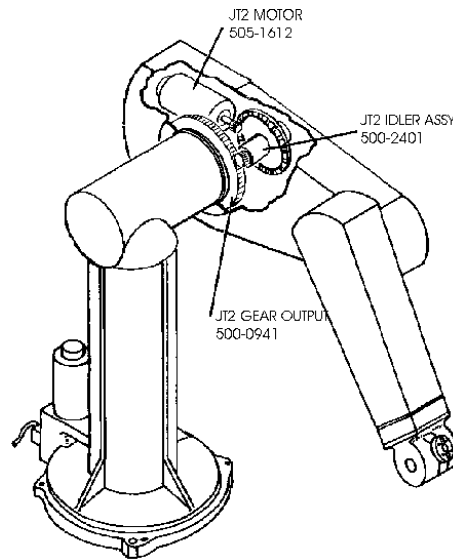
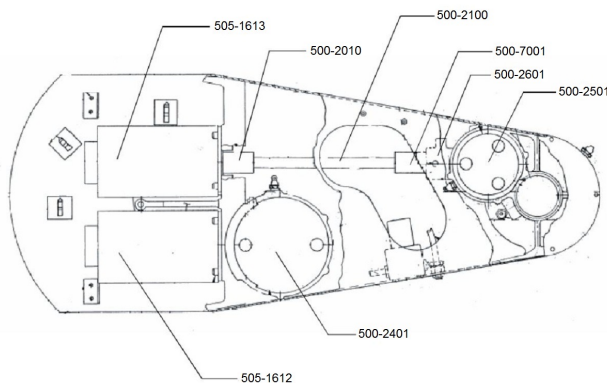


Transmissions in industrial robots

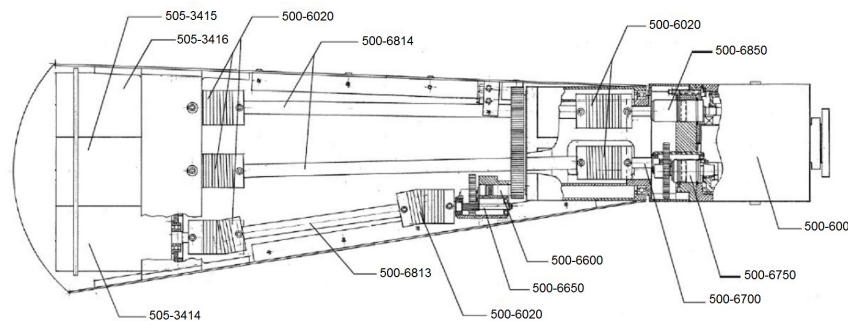
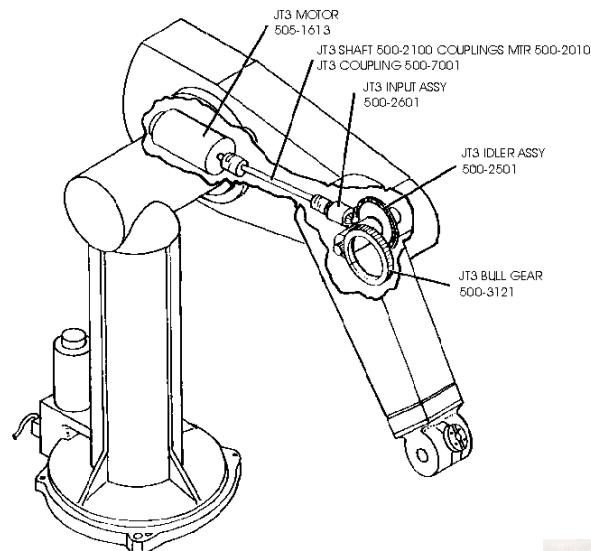
- transmissions used (inside) 6-dof Unimation industrial robots with serial kinematics



PUMA 260: 1st axis

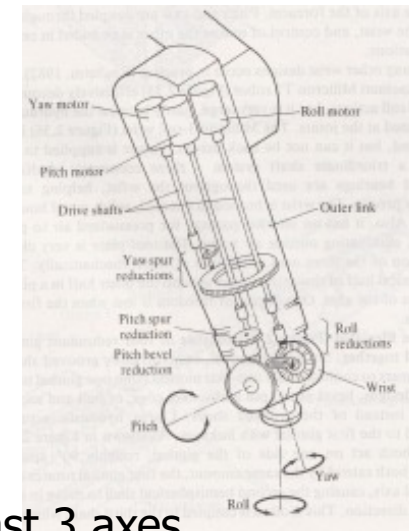


PUMA 560: 2nd and 3rd axes



PUMA 560: inner and outer links

PUMA 560



PUMA 560: last 3 axes

Inside views on joint axes 4, 5 & 6 of an industrial KUKA robot



- looking inside the forearm to see the transmissions of the spherical wrist
- motor rotation seen from the encoder side (small couplings exist)

<https://youtu.be/iRKDfknqtbC>



Differential drive at wrist

two motors + transmissions for moving joints 5 & 6



video

both motors
are rotating
in the **same**
direction
(same speed)



only joint 5
moves

video

the motors
are rotating
in **opposite**
directions
(same speed)

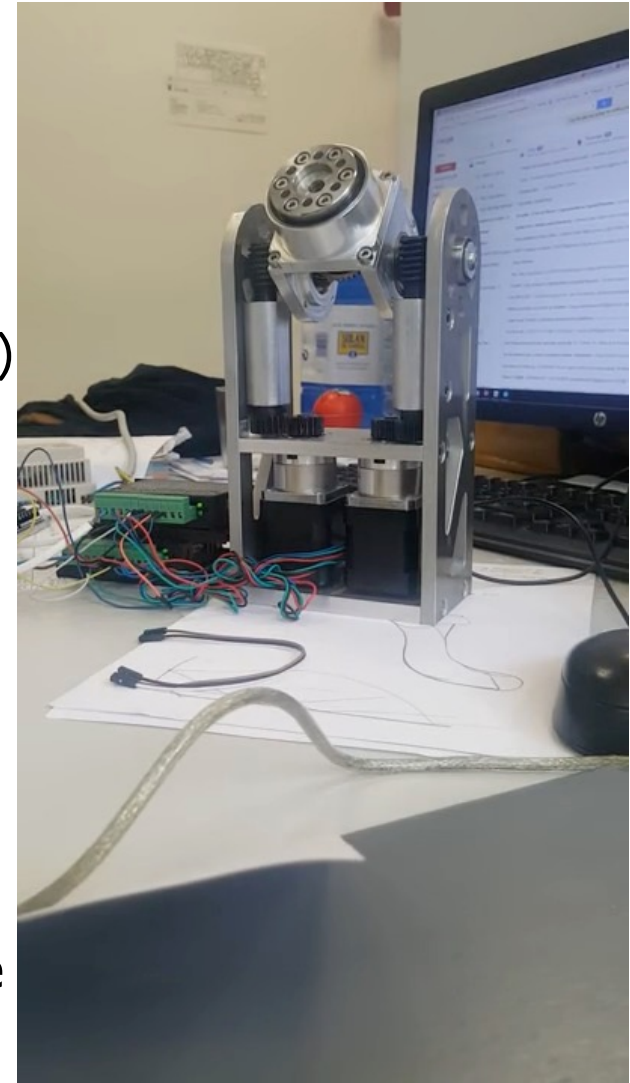


only joint 6
moves

any other
combination of
motor velocities



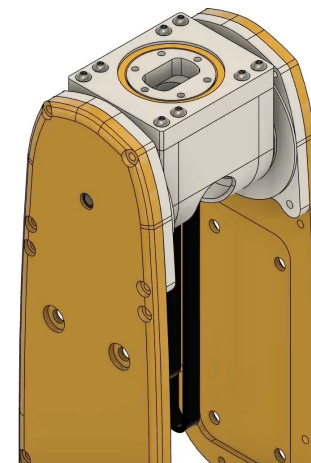
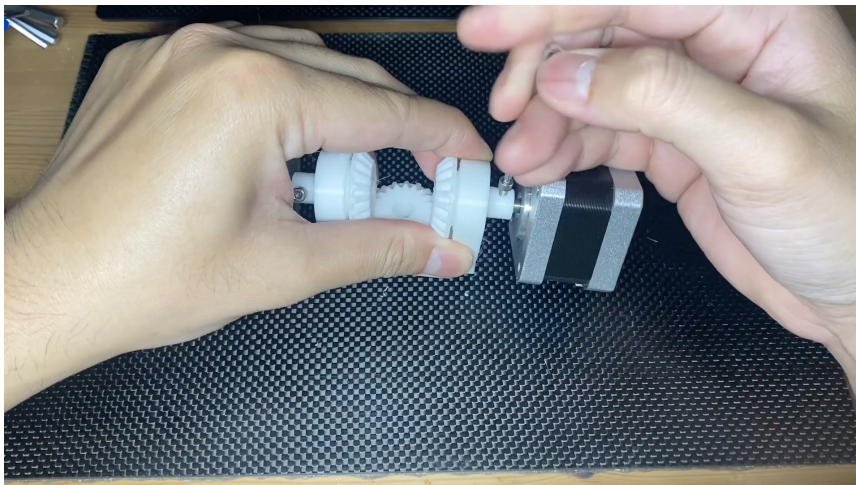
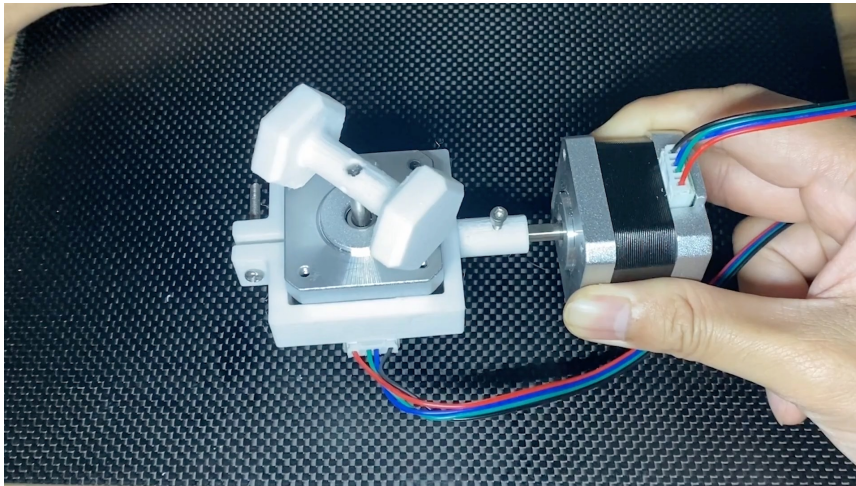
both joints move
simultaneously



Trivia on differential drive at wrist to achieve pitch and roll motion

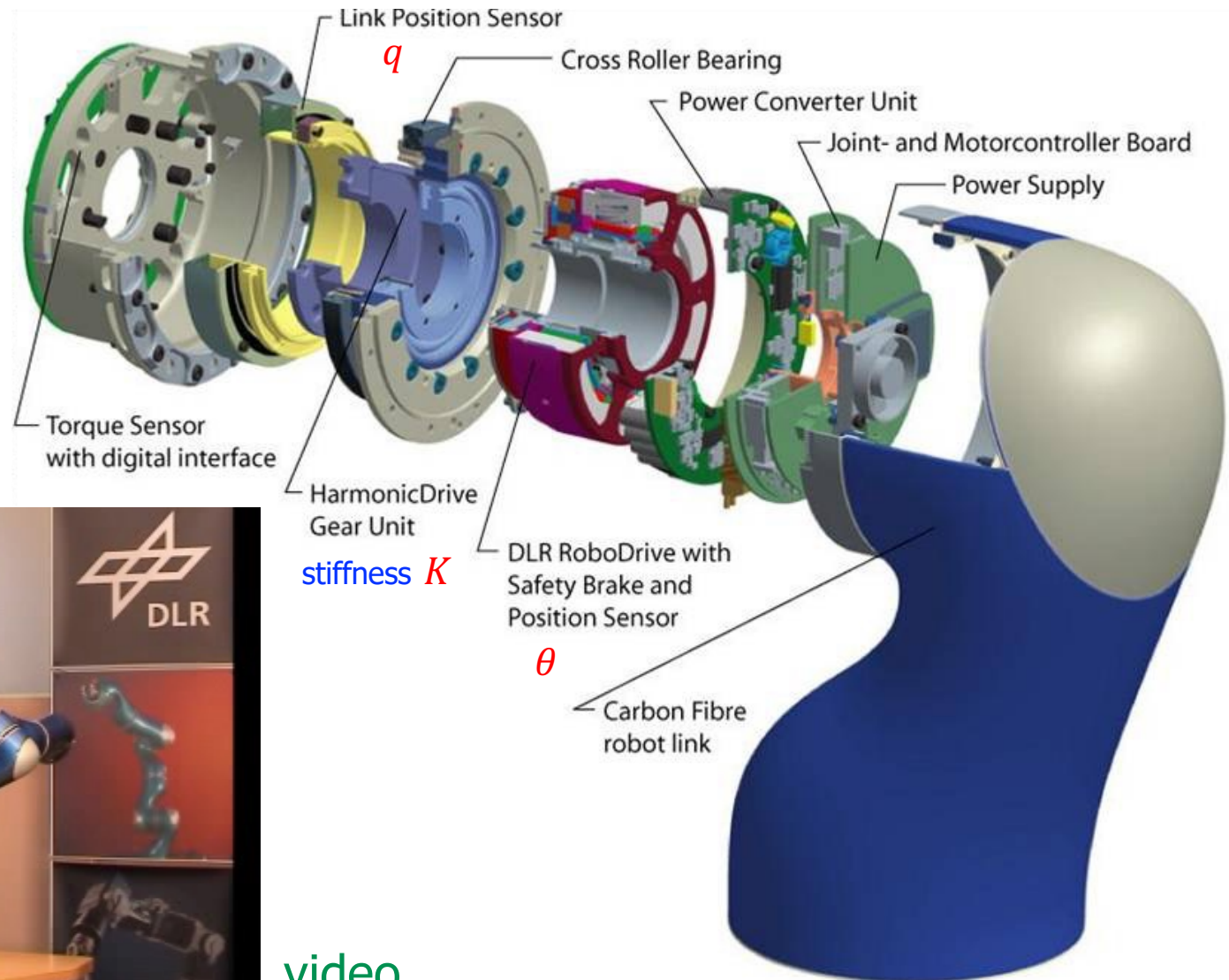


4 clips from 1 video <https://youtu.be/lr-Zh8kpTuo>



Exploded view of a joint in the DLR-III robot

joint torque
 $\tau_j = K(\theta - q)$



video