

# Implicitly Coordinated Multi-Agent Path Finding under Destination Uncertainty

## The Dancing Robots

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- A central problem in many applications is the coordinated movement of agents/robots/vehicles in a given environment.



Motivation

MAPF

Going  
Beyond:  
MAPF/DU

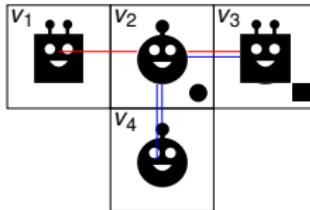
Implicitly  
Coordinated  
Branching  
Plans

Joint  
Execution

Results

An abstraction of this problem is the **Multi-Agent Path Finding** (MAPF) problem:

- Given a set of **agents**  $A$ , a (perhaps directed) **graph**  $G = (V, E)$ , an **initial state** modelled by an injective function  $\alpha_0 : A \rightarrow V$  and a **goal state** modelled by another injective function  $\alpha_*$ , can  $\alpha_0$  be **transformed** into  $\alpha_*$  by movements of single agents without collisions?



- Can we find a (central) plan to move the square robot  $S$  to  $v_3$  and the circle robot  $C$  to  $v_2$ ?

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## MAPF with **destination uncertainty** (MAPF/DU):

- All agents know their own destinations, but these are **not common knowledge** any longer.
- For each agent, there exists a **set of possible destinations**, which do not overlap with possible destinations of other agents. These possible destinations are **common knowledge**.
- All agents plan and re-plan **without communicating** with their peers.
- A **success announcement action** becomes necessary, which the agents can use to announce that they have reached their destination (and after that they are not allowed to move anymore).

→ Models multi-robot interactions without communication

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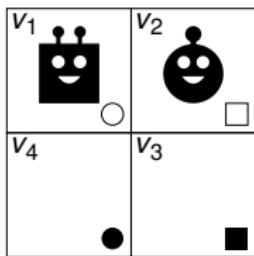
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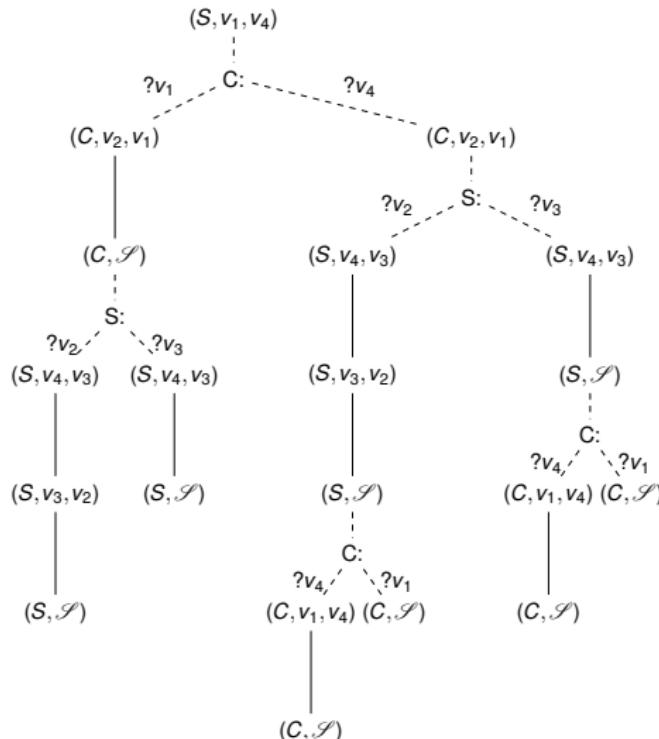
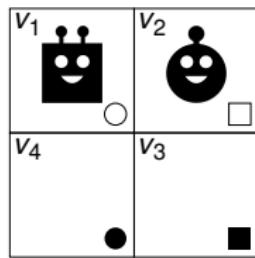
- We need a **solution concept** for the agents: **implicitly coordinated branching plans**.
- We need to define what the **joint execution** of such plans means.
- We need to find **conditions** that guarantee **success** of such joint executions.
- We have to determine the **computational complexity** for finding plans and deciding solvability.

→ Since MAPF/DU is a special case of **epistemic planning** (initial state uncertainty which is monotonically decreasing), we can use concepts and results from this area.



- Square agent  $S$  **wants to go to  $v_3$**  and **knows** that circle agent  $C$  wants to go to  $v_1$  or  $v_4$ .
- $C$  **wants to go to  $v_4$**  and **knows** that  $S$  wants to go to  $v_2$  or  $v_3$ .
- Let us assume  $S$  forms a plan in which it moves in order to **empower**  $C$  to reach their common goal.
- $S$  needs **shifting its perspective** in order to plan for all possible destinations of  $C$  (**branching on destinations**).
- Planning for  $C$ ,  $S$  must **forget** about its own destination.

# Branching plan: Example



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- Let us assume, all agents have planned and a subset of them came up with a **family of plans** ( $\pi_i$ ) $_{i \in A}$ .
- Among the agents that have a plan with their **own action as the next action to execute**, one is chosen.
- The action of the chosen agent is **executed**.
- Agents, which have anticipated the action, **track** that in their plans.
- All other agents have to **replan** from the new state.
- Since all plans branch over all possible destinations and result in goal states, no acting agent will ever execute an action that leads to a **dead end**.
- However, agents might wait for each other **infinitely long** or undo each others action leading to **execution cycles**.

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- Provided all agents plan in a particular way, we can guarantee success with **polynomial executions**.
- They have to plan
  - **optimally**, i.e., generate (worst-case) shortest plans;
  - **conservatively**, i.e., replan from the initial state using the executed actions as a prefix;
  - **eagerly**, i.e., always plan to act when they can act (respecting optimality and conservativity).
- Deciding whether an implicitly coordinated plan exists is **PSPACE-complete** (same for eager plans with depth  $k$ ).

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Preprint: <http://tr.informatik.uni-freiburg.de/2018/>  
Talk on Epistemic Planning: **Friday, 2pm**