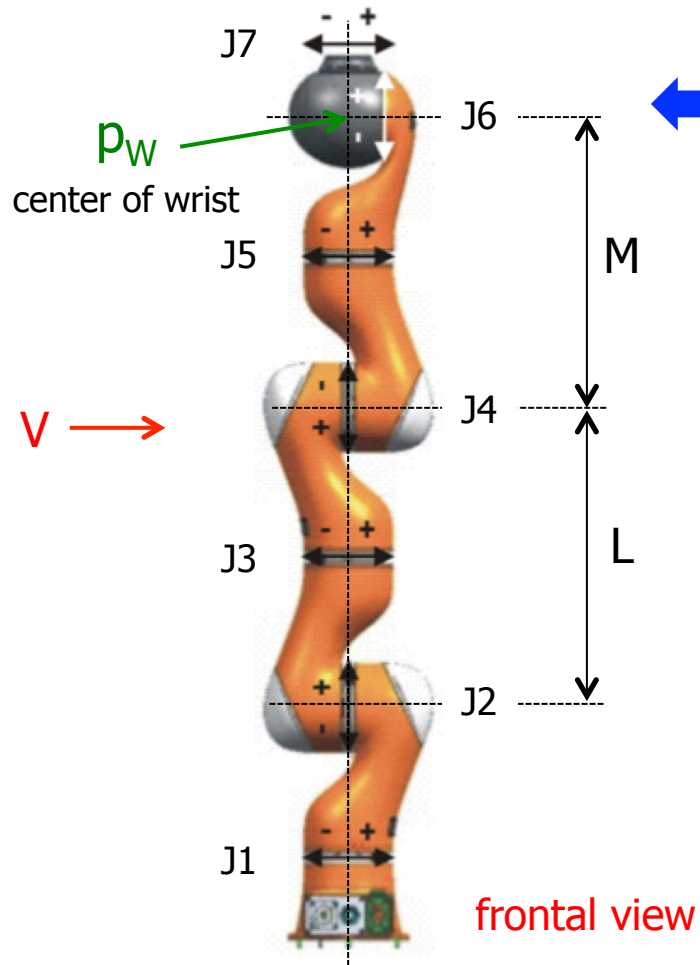
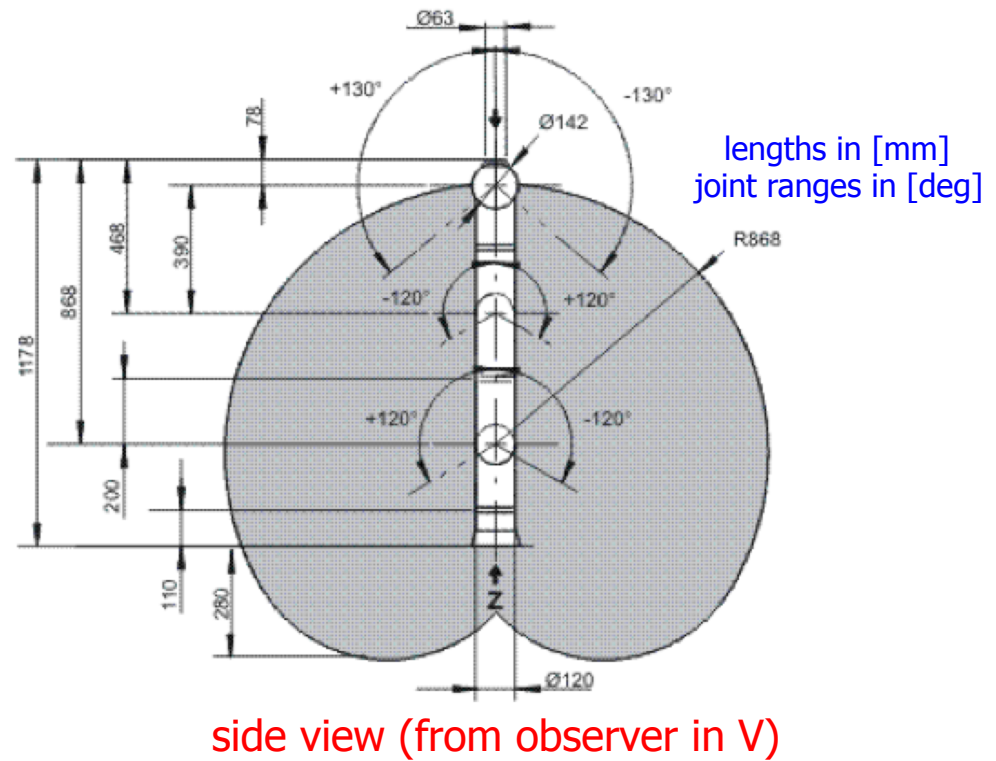


KUKA LWR-IV

- 7R manipulator: spherical shoulder (3R), elbow joint (1R), spherical wrist (3R)



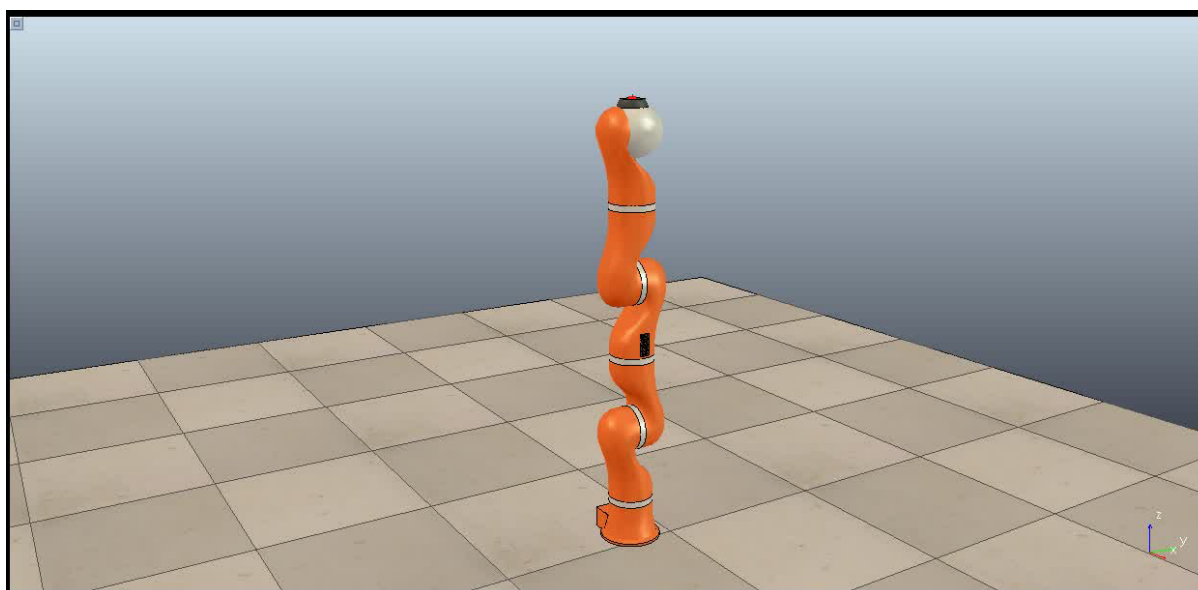
- the robot is shown in its **zero** configuration ($\mathbf{q}=\mathbf{0}$)
- positive directions of joint rotations are indicated



KUKA LWR-IV in motion



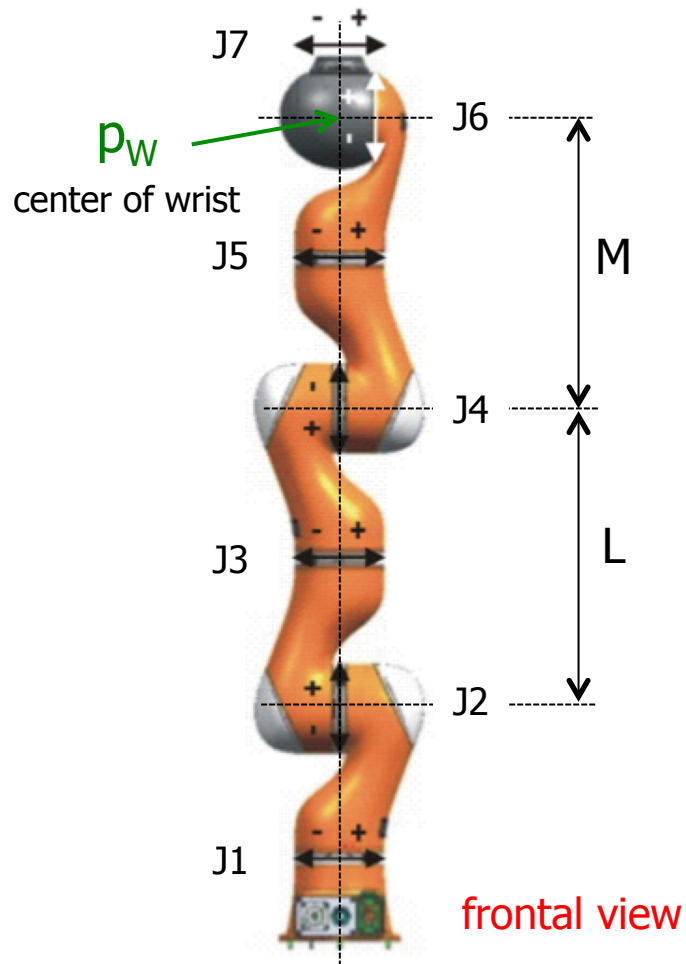
↑
side view from
observer in V



↖
videos at DIAG
Robotics Lab

VREP video

KUKA LWR-IV



- determine

- frames and table of D-H parameters
 - be consistent with positive rotations indicated by KUKA
 - only the two kinematic lengths L and M should be needed
- homogeneous transformation matrices
- direct kinematics of the center of wrist p_W in **symbolic** form
- **numerically**, in the configuration

$$q = (0, \pi/2, \pi/2, -\pi/2, 0, \pi/2, 0) \quad [\text{rad}]$$

the position 0p_d in frame 0 of a **tool point** P_d whose coordinates in frame 7 are given by

$${}^7p_d = (0, 0.05, 0.1) \quad [\text{m}]$$

Assignment of D-H frames

steps!

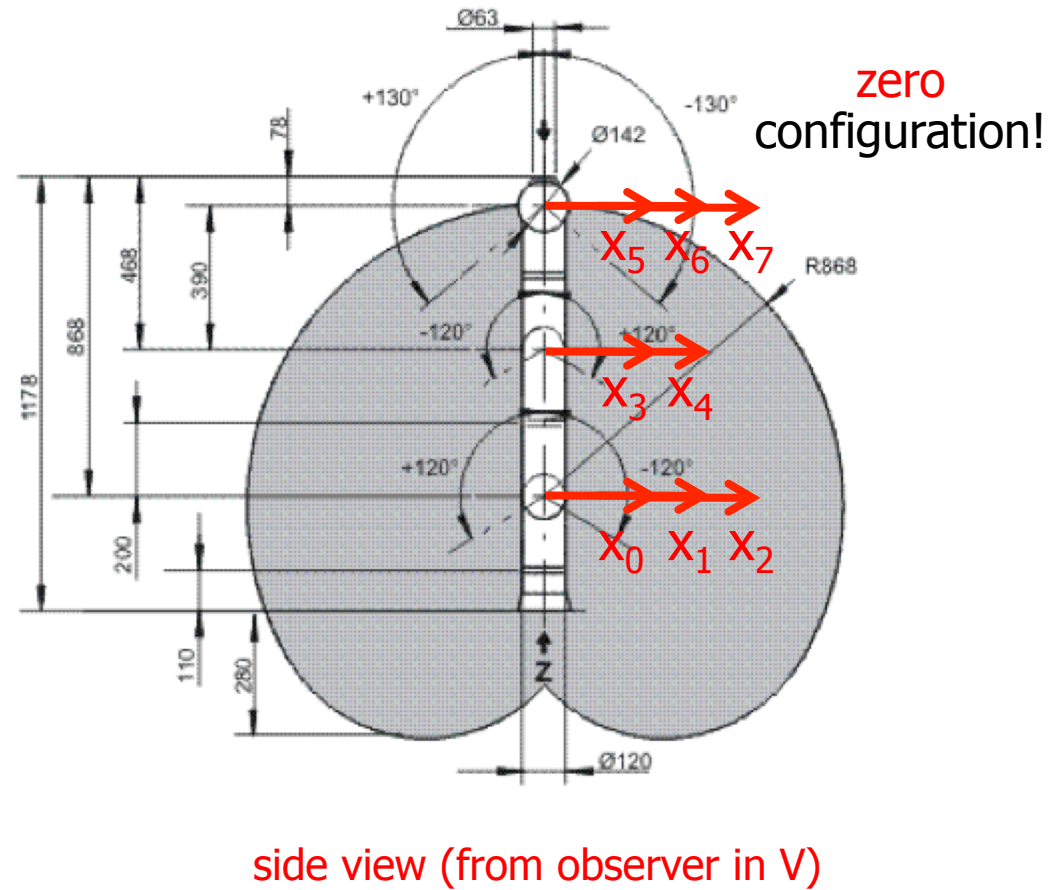
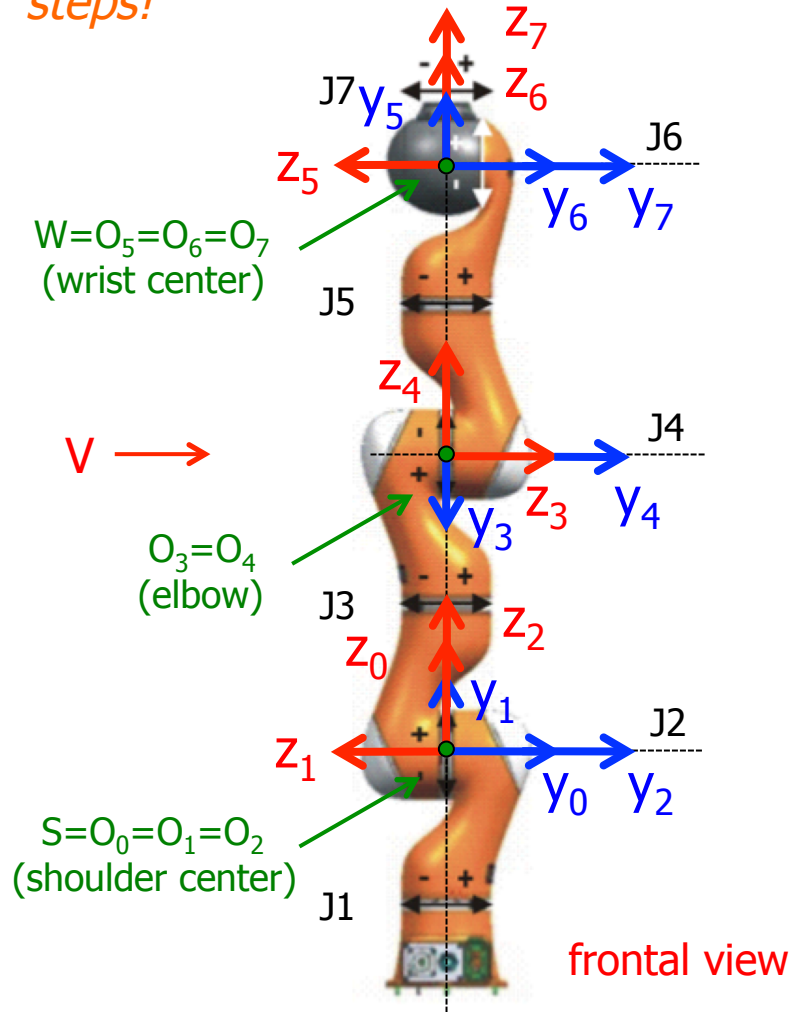
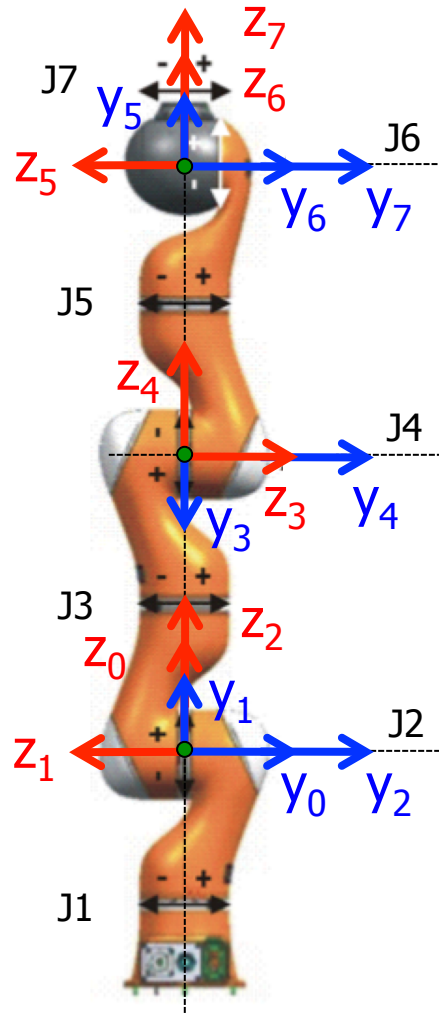


Table of D-H parameters



i	α_i	d_i	a_i	θ_i
1	$\pi/2$	0	0	$q_1=0$
2	$-\pi/2$	0	0	$q_2=0$
3	$-\pi/2$	L	0	$q_3=0$
4	$\pi/2$	0	0	$q_4=0$
5	$\pi/2$	M	0	$q_5=0$
6	$-\pi/2$	0	0	$q_6=0$
7	0	0	0	$q_7=0$

in the shown configuration

with

$$d_3 = L = 0.40, \quad d_5 = M = 0.39 \quad [\text{m}]$$

D-H homogeneous matrices

output from Matlab (**symbolic**) program

```
A1 =  
[ cos(q1), 0, sin(q1), 0]  
[ sin(q1), 0, -cos(q1), 0]  
[ 0, 1, 0, 0]  
[ 0, 0, 0, 1]  
  
A2 =  
[ cos(q2), 0, -sin(q2), 0]  
[ sin(q2), 0, cos(q2), 0]  
[ 0, -1, 0, 0]  
[ 0, 0, 0, 1]  
  
A3 =  
[ cos(q3), 0, -sin(q3), 0]  
[ sin(q3), 0, cos(q3), 0]  
[ 0, -1, 0, L]  
[ 0, 0, 0, 1]  
  
A4 =  
[ cos(q4), 0, sin(q4), 0]  
[ sin(q4), 0, -cos(q4), 0]  
[ 0, 1, 0, 0]  
[ 0, 0, 0, 1]
```

```
A5 =  
[ cos(q5), 0, sin(q5), 0]  
[ sin(q5), 0, -cos(q5), 0]  
[ 0, 1, 0, M]  
[ 0, 0, 0, 1]  
  
A6 =  
[ cos(q6), 0, -sin(q6), 0]  
[ sin(q6), 0, cos(q6), 0]  
[ 0, -1, 0, 0]  
[ 0, 0, 0, 1]  
  
A7 =  
[ cos(q7), -sin(q7), 0, 0]  
[ sin(q7), cos(q7), 0, 0]  
[ 0, 0, 1, 0]  
[ 0, 0, 0, 1]
```

Direct kinematics of the wrist center

output from Matlab (**symbolic**) program

$$p_{W,hom} = A_1(q_1)A_2(q_2)A_3(q_3)A_4(q_4)A_5(q_5)A_6(q_6)A_7(q_7) \cdot [0 \ 0 \ 0 \ 1]^T$$

these can be replaced (by inspection) with $[0 \ 0 \ M \ 1]^T$

$$= A_1(q_1)A_2(q_2)A_3(q_3)A_4(q_4) \cdot [0 \ 0 \ M \ 1]^T$$

the last three (spherical) joints do **not** move W

faster (symbolic) recursive position transformations
(matrix · vector products, in homogenous coordinates)

`pW =`

```
- cos(q1)*(sin(q2)*(L + M*cos(q4)) - M*cos(q2)*cos(q3)*sin(q4)) - M*sin(q1)*sin(q3)*sin(q4)
M*cos(q1)*sin(q3)*sin(q4) - sin(q1)*(sin(q2)*(L + M*cos(q4)) - M*cos(q2)*cos(q3)*sin(q4))
cos(q2)*(L + M*cos(q4)) + M*cos(q3)*sin(q2)*sin(q4)
```

Tool position evaluation

output from Matlab ([numerical](#)) program

- in the given configuration $q = (0, \pi/2, \pi/2, -\pi/2, 0, \pi/2, 0)$ [rad]
for the **tool point** P_d of coordinates (in frame 7) ${}^7p_d = (0, 0.05, 0.1)$ [m]

$${}^0p_{d,hom} = A_1(q_1)A_2(q_2)A_3(q_3)A_4(q_4)A_5(q_5)A_6(q_6)A_7(q_7) {}^7p_{d,hom}$$

etc.

again, (numerical) recursive position transformations (matrix · vector products)

```
Anum{1}=subs(A1,{q1},{0});
Anum{2}=subs(A2,{q2},{pi/2});
Anum{3}=subs(A3,{q3,L},{pi/2,0.4});
Anum{4}=subs(A4,{q4},{-pi/2});
Anum{5}=subs(A5,{q5,M},{0,0.39});
Anum{6}=subs(A6,{q6},{pi/2});
Anum{7}=subs(A7,{q7},{0});
```

numerical evaluation
of symbolic quantities

```
pd = [0 0.05 0.1 1]';
```

```
for i=N:-1:1
    pd = Anum{i}*pd;
end
```

7p_d in homogeneous coordinates

```
pd=pd(1:3)
```

```
pd =
-0.3000
-0.3900
-0.0500
```

