



Robotics 2

Hybrid Force/Motion Control

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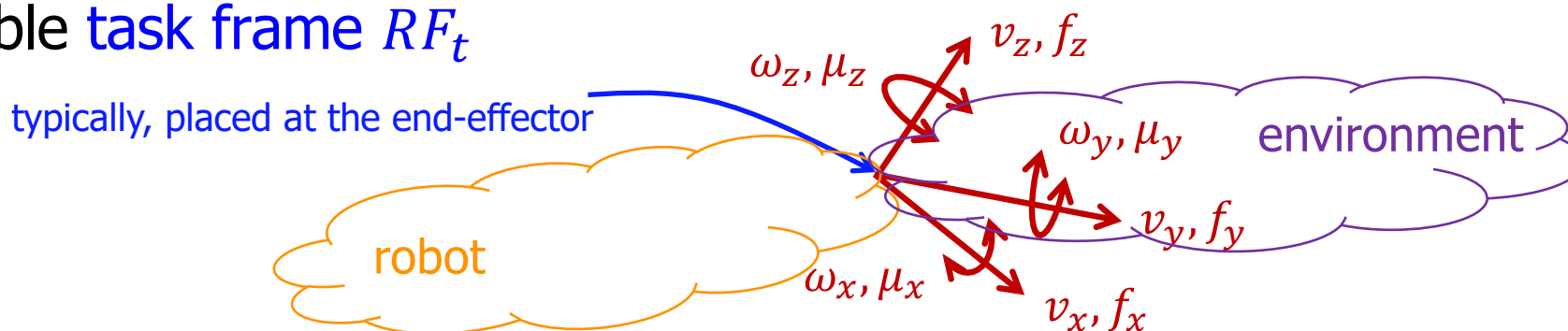
Hybrid force/motion control

- we consider **contacts/interactions** between a robot and a stiff environment that **naturally constrains** the end-effector motion
- **compared** to an approach using the constrained/reduced robot dynamics with (bilateral) **geometric constraints**, the **differences** are
 - the hybrid control law is designed in **ideal conditions**, but now unconstrained directions of motion and constrained force directions are defined in a more direct way using a **task frame formalism**
 - all **non-ideal conditions** (compliant surfaces, friction at the contact, errors in contact surface orientation) are handled explicitly in the control scheme by a **geometric filtering of the measured quantities**
 - considering only signal components that should appear in certain directions based on the nominal task model, and treating those that should not be there as **disturbances** to be rejected
- the hybrid control law avoids to introduce conflicting behaviors (force vs. motion control) in any of the task space directions!!



Natural constraints

- in **ideal conditions** (robot and environment are perfectly rigid, contact is frictionless), **two sets of generalized directions** can be defined in the **task space**
 - **end-effector motion** (v/ω) is prohibited along/around **$6 - k$ directions** (since the environment reacts there with forces/torques)
 - **reaction forces/torques** (f/μ) are absent along/around **k directions** (where the environment does not prevent end-effector motions)
- these constraints have been called the **natural constraints** on motion and force associated to the task geometry
- the two sets of directions are characterized through the axes of a suitable **task frame** RF_t



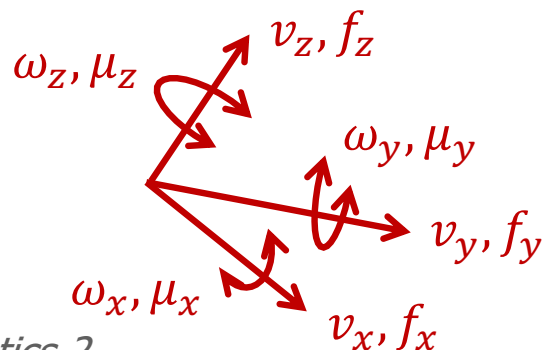


Artificial constraints

- the way **task execution** should be performed can be expressed in terms of so-called **artificial constraints** that specify the desired values (to be imposed by the control law)
 - for the **end-effector velocities** (v/ω) along/around **k directions** where feasible motions can occur
 - for the **contact forces/torques** (f/μ) along/around **$6 - k$ directions** where admissible reactions of the environment can occur
- the two sets of directions are **complementary** (they cover the 6D generalized task space) and mutually **orthogonal**, while the **task frame** can be **time-varying** ("moves with task progress")
 - directions are intended as 6D **screws**: **twists** $V = (v^T \ \omega^T)^T$ and

wrenches $F = (f^T \ \mu^T)^T$

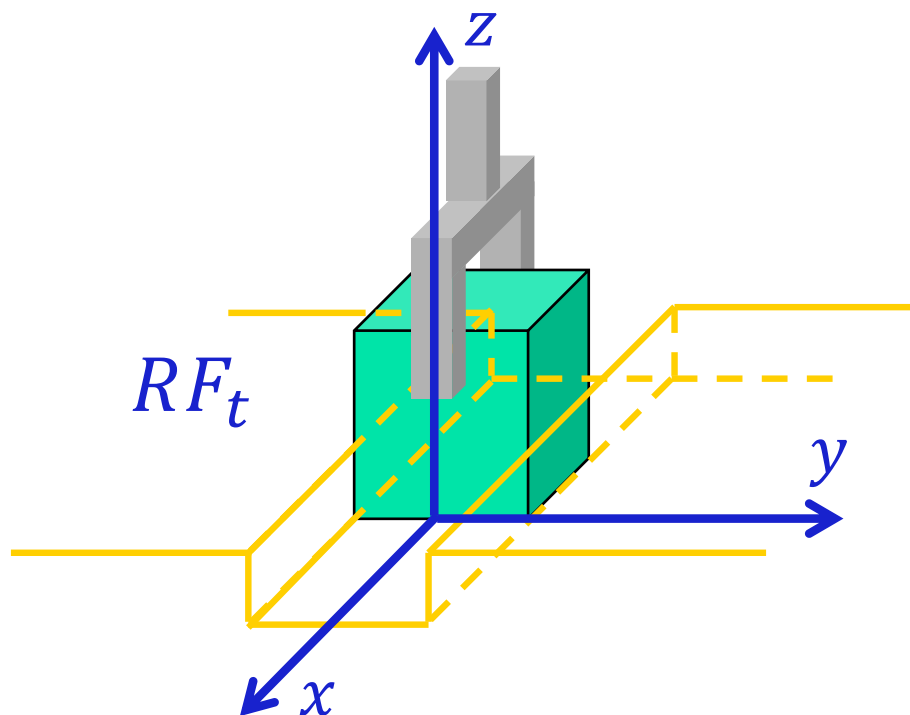
$$F^T V = 0 \Leftrightarrow \text{orthogonality}$$



but **ill-defined** (don't use it!) for $V_1^T V_2$ or $F_1^T F_2$



Task frame and constraints - example 1



task: slide the cube along a guide

natural (geometric) constraints

$$\left. \begin{array}{l} v_y = v_z = 0 \\ \omega_x = \omega_z = 0 \end{array} \right\} 6 - k = 4$$
$$\left. \begin{array}{l} f_x = \mu_y = 0 \end{array} \right\} k = 2$$

v = linear velocity
 ω = angular velocity
 f = force
 μ = torque

$6 - k = 4$ {

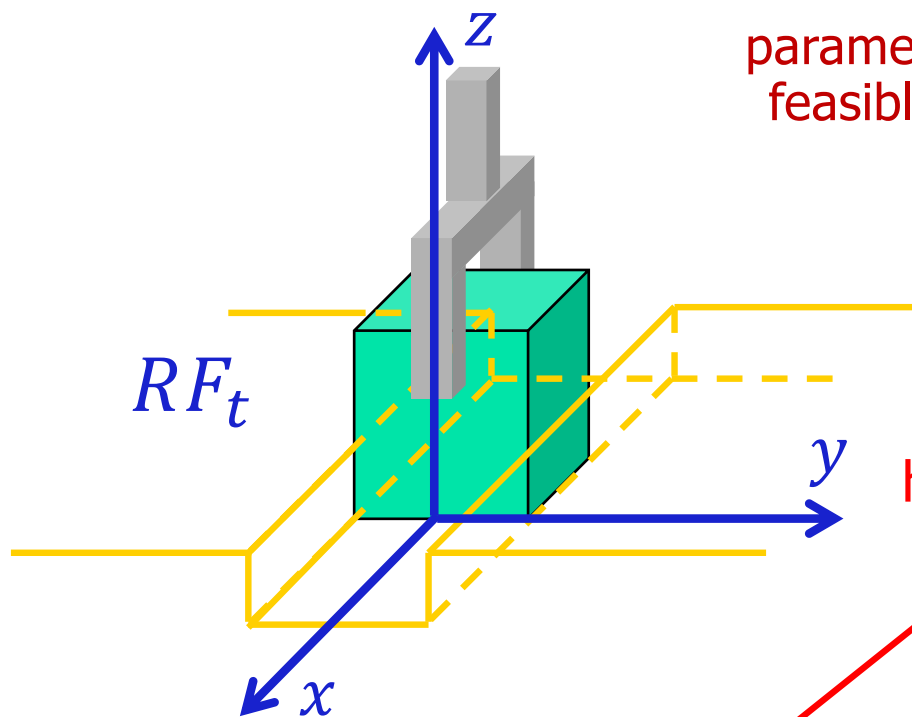
$k = 2$ {

artificial constraints
(to be imposed by the control law)

$$\left. \begin{array}{l} f_y = f_{y,des} (= 0) \text{ (to avoid internal stress)} \\ \mu_x = \mu_{x,des} (= 0), \mu_z = \mu_{z,des} (= 0) \\ f_z = f_{z,des} \text{ (to keep contact)} \end{array} \right\}$$
$$\left. \begin{array}{l} \omega_y = \omega_{y,des} = 0 \text{ (to slide and not to roll !!)} \\ v_x = v_{x,des} \end{array} \right\}$$



Selection of directions - example 1



parametrization of feasible motions

$$\begin{pmatrix} v \\ \omega \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 1 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} v_x \\ \omega_y \end{pmatrix} = T \begin{pmatrix} v_x \\ \omega_y \end{pmatrix}$$

here, constant and unitary ("selection" of columns from the 6×6 identity matrix)

parametrization of feasible reactions

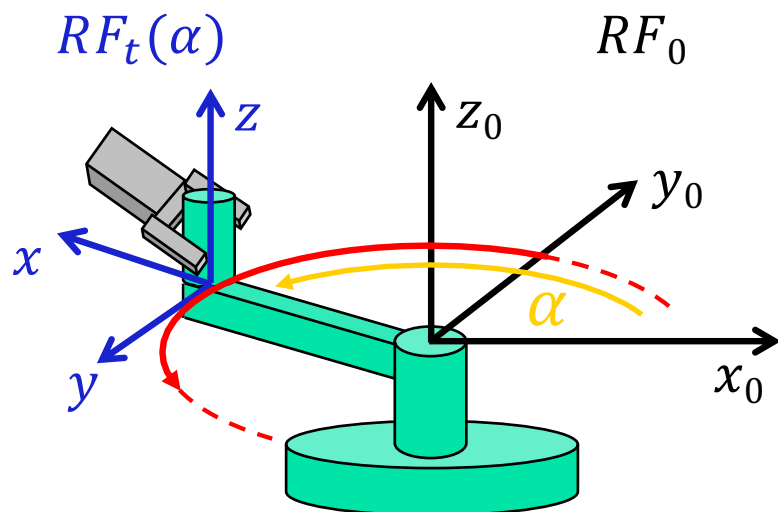
$$\begin{pmatrix} f \\ \mu \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} f_y \\ f_z \\ \mu_x \\ \mu_z \end{pmatrix} = Y \begin{pmatrix} f_y \\ f_z \\ \mu_x \\ \mu_z \end{pmatrix}$$

$$T^T Y = 0$$

reaction forces/torques do **not** perform work on feasible motions

$$\begin{pmatrix} f^T & \mu^T \end{pmatrix} \begin{pmatrix} v \\ \omega \end{pmatrix} = 0$$

Task frame and constraints - example 2



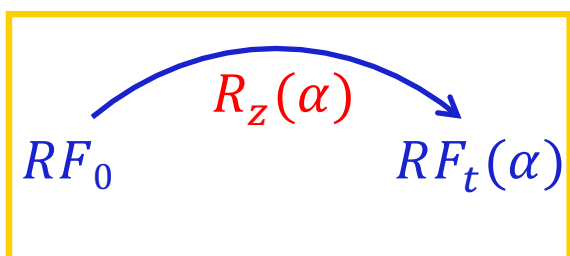
task: turning a crank
(free handle)

natural constraints

$$v_x = v_z = 0$$

$$\omega_x = \omega_y = 0$$

$$f_y = \mu_z = 0$$



artificial constraints

$$f_x = f_{x,des} (= 0), f_z = f_{z,des} (= 0)$$

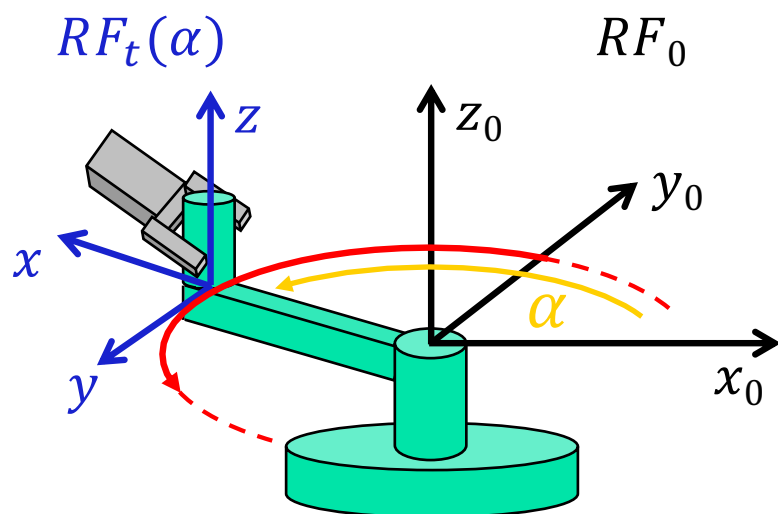
$$\mu_x = \mu_{x,des} (= 0), \mu_y = \mu_{y,des} (= 0)$$

$$v_y = v_{y,des} \text{ (the tangent speed of rotation)}$$

$$\omega_z = \omega_{z,des} (= 0 \text{ if handle should not spin})$$



Selection of directions – example 2



parametrization of feasible motions

$$\begin{pmatrix} {}^0v \\ {}^0\omega \end{pmatrix} = \begin{pmatrix} R^T(\alpha) & 0 \\ 0 & R^T(\alpha) \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} v_y \\ \omega_z \end{pmatrix} = T(\alpha) \begin{pmatrix} v_y \\ \omega_z \end{pmatrix}$$

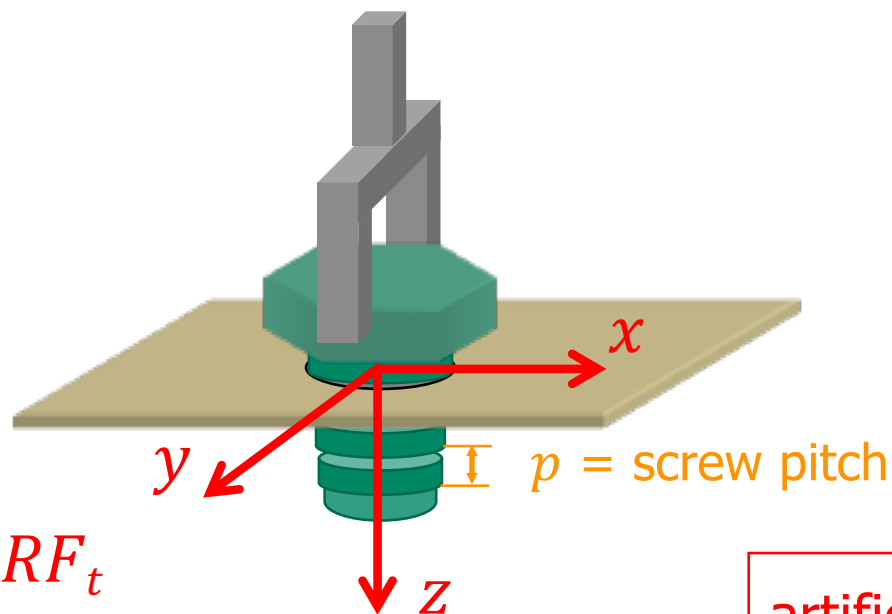
$$T^T(\alpha)Y(\alpha) = 0$$

parametrization of feasible reactions

$$\begin{pmatrix} {}^0f \\ {}^0\mu \end{pmatrix} = \begin{pmatrix} R^T(\alpha) & 0 \\ 0 & R^T(\alpha) \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} f_x \\ f_z \\ \mu_x \\ \mu_y \end{pmatrix} = Y(\alpha) \begin{pmatrix} f_x \\ f_z \\ \mu_x \\ \mu_y \end{pmatrix}$$



Task frame and constraints - example 3



task: insert a screw
in a bolt

natural constraints (partial...)

$$v_x = v_y = 0$$

$$\omega_x = \omega_y = 0$$

artificial constraints (abundant...)

$$f_x = f_{x,des} = 0, f_y = f_{y,des} = 0$$

$$\mu_x = \mu_{x,des} = 0, \mu_y = \mu_{y,des} = 0$$

$$v_z = v_{z,des}, \omega_z = \omega_{z,des} = (2\pi/p)v_{z,des}$$

$$f_z = f_{z,des}, \mu_z = \mu_{z,des} \text{ (one function of the other!)}$$

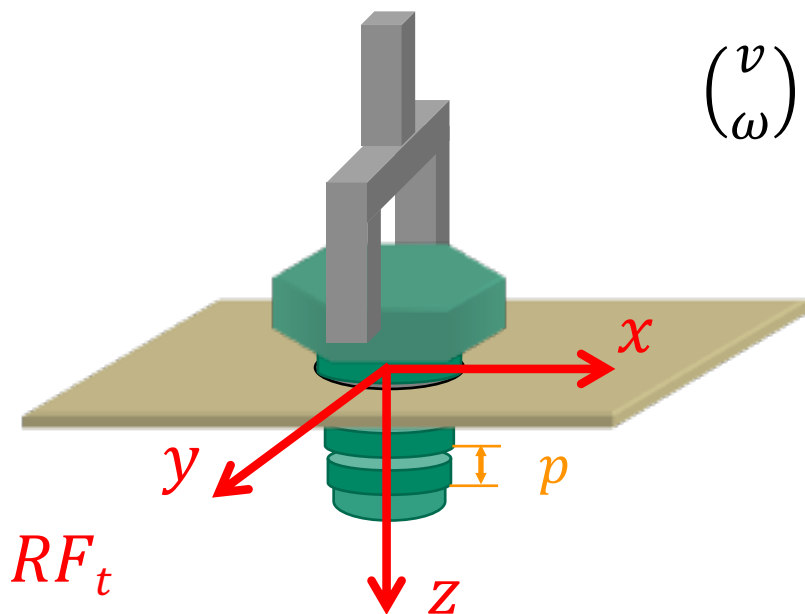
the screw proceeds **along** and **around** the **z**-axis, but **not** in an **independent** way! (1 dof)

accordingly, f_z and μ_z **cannot** be **independent**

wrench (force/torque) direction should be **orthogonal** to motion twist!



Selection of directions – example 3



$$\begin{pmatrix} v \\ \omega \end{pmatrix} = \begin{pmatrix} 0 & 0 & 1 & 0 & 0 & \frac{2\pi}{p} \end{pmatrix}^T v_z = T v_z \quad (k = 1)$$

$$\text{or } \omega_z = 2\pi \frac{v_z}{p}$$

Y : such that $T^T Y = 0$

$$f_z = -\frac{2\pi}{p} \mu_z$$

$(6 - k = 5)$

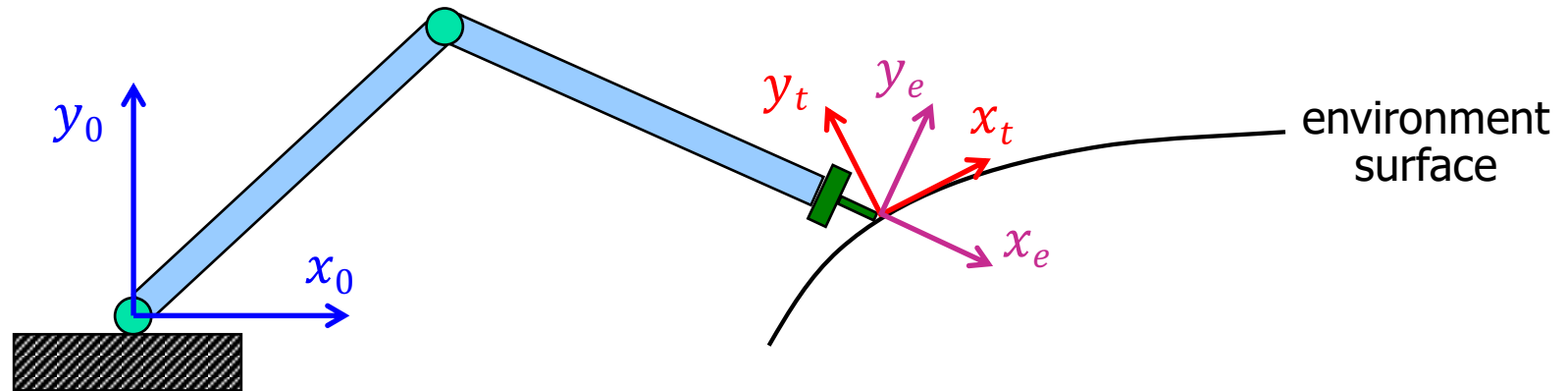
the columns of T and Y do not necessarily coincide with selected columns of the 6×6 identity matrix
 \Rightarrow generalized (screw) directions

$$\begin{pmatrix} f \\ \mu \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -2\pi/p \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} f_x \\ f_y \\ \mu_x \\ \mu_y \\ \mu_z \end{pmatrix} = Y \begin{pmatrix} f_x \\ f_y \\ \mu_x \\ \mu_y \\ \mu_z \end{pmatrix}$$



Frames of interest – example 4

planar motion of a 2R robot ($n = 2$) in pointwise contact with a surface (task dimension $m = 2$)



- **task frame RF_t** used for an independent definition of the hybrid **reference values** (here: ${}^t v_{x,des}$ [$k = 1$] and ${}^t f_{y,des}$ [$m - k = 1$]) and for computing the errors that drive the **feedback control** law
- **sensor frame RF_e** (here: RF_2) where the **force** ${}^e f = ({}^e f_x, {}^e f_y)$ is measured
- **base frame RF_0** in which the end-effector **velocity** is expressed (here: ${}^0 v = ({}^0 v_x, {}^0 v_y)$ of O_2), computed using robot Jacobian and joint velocities

all quantities (and errors!) should be expressed ("rotated")
in the **same** reference frame \Rightarrow the **task frame!**



General parametrization of hybrid tasks

a "description" of robot-environment contact type: it implicitly defines the task frame

$$\begin{cases} \begin{pmatrix} v \\ \omega \end{pmatrix} = T(s)\dot{s} & s \in \mathbb{R}^k \\ & \text{parametrizes robot E-E free motion} \\ \begin{pmatrix} f \\ \mu \end{pmatrix} = Y(s)\lambda & \lambda \in \mathbb{R}^{m-k} \\ & \text{parametrizes reaction forces/torques} \end{cases}$$

reaction forces/torques do not perform work on E-E displacements



$$T^T(s)Y(s) = 0$$



axes directions of **task frame** depend in general on s (i.e., on robot E-E pose in the environment)

in general, it is $m = 6$ (as in most of the previous examples)

+

robot dynamics

$$M(q)\ddot{q} + S(q, \dot{q})\dot{q} + g(q) = u + J^T(q) \begin{pmatrix} f \\ \mu \end{pmatrix}$$

robot kinematics

$$\begin{pmatrix} v \\ \omega \end{pmatrix} = J(q)\dot{q}$$



Hybrid force/velocity control

- **control objective:** to impose desired task evolutions to the parameters s of **motion** and to the parameters λ of **force**

$$s \rightarrow s_d(t) \quad \lambda \rightarrow \lambda_d(t)$$

- the control law is designed in **two steps**
 1. exact **linearization and decoupling** in the **task frame** by feedback

$$\boxed{\text{closed-loop model}} \rightarrow \begin{pmatrix} \ddot{s} \\ \lambda \end{pmatrix} = \begin{pmatrix} a_s \\ a_\lambda \end{pmatrix}$$

2. (**linear**) design of a_s and a_λ so as to impose the desired dynamic behavior to the errors $e_s = s_d - s$ and $e_\lambda = \lambda_d - \lambda$

- **assumptions:** $n = m$ ($= 6$ usually), $J(q)$ out of singularity

Note: in “simple” cases, \dot{s} and λ drive single components of v or ω and of f or μ ; accordingly, T and Y are just columns of **0/1 selection matrices**



Feedback linearization in task space

$$J(q)\dot{q} = \begin{pmatrix} v \\ \omega \end{pmatrix} = T(s)\dot{s} \rightarrow J\ddot{q} + \dot{J}\dot{q} = T\ddot{s} + \dot{T}\dot{s} \rightarrow \ddot{q} = J^{-1}(T\ddot{s} + \dot{T}\dot{s} - \dot{J}\dot{q})$$

$$M(q)\ddot{q} + S(q, \dot{q})\dot{q} + g(q) = u + J^T(q) \begin{pmatrix} f \\ \mu \end{pmatrix} = u + J^T(q)Y(s)\lambda$$

$$\left(M(q)J^{-1}(q)T(s) \quad ; \quad -J^T(q)Y(s) \right) \begin{pmatrix} \ddot{s} \\ \lambda \end{pmatrix}$$

nonsingular $n \times n$ matrix
(under the assumptions made)

$$+ M(q)J^{-1}(q)(\dot{T}(s)\dot{s} - \dot{J}(q)\dot{q}) + S(q, \dot{q})\dot{q} + g(q) = u$$

$$u = (MJ^{-1}T \quad ; \quad -J^TY) \begin{pmatrix} a_s \\ a_\lambda \end{pmatrix} + MJ^{-1}(\dot{T}\dot{s} - \dot{J}\dot{q}) + S\dot{q} + g$$

linearizing and
decoupling
control law

$$\rightarrow \begin{pmatrix} \ddot{s} \\ \lambda \end{pmatrix} = \begin{pmatrix} a_s \\ a_\lambda \end{pmatrix} \left. \begin{array}{l} \} k \\ \} m - k \end{array} \right\}$$

s has "relative degree" = 2

λ has "relative degree" = 0



Stabilization with a_s and a_λ

as usual, it is sufficient to apply **linear** control techniques for the exponential stabilization of tracking errors (on each single, input-output decoupled channel)

$$a_s = \ddot{s}_d + K_D(\dot{s}_d - \dot{s}) + K_P(s_d - s)$$

$K_P, K_D > 0$
and diagonal

$$\rightarrow \ddot{e}_s + K_D \dot{e}_s + K_P e_s = 0 \rightarrow e_s = s_d - s \rightarrow 0$$

$K_I \geq 0$
diagonal

$$a_\lambda = \lambda_d + K_I \int (\lambda_d - \lambda) dt$$

$a_\lambda = \lambda_d$ would be enough,
but adding an integral
with the **force error**
gives more robustness
to (constant) disturbances

$$\rightarrow e_\lambda + K_I \int e_\lambda dt = 0 \rightarrow e_\lambda = \lambda_d - \lambda \rightarrow 0$$

we need "values" for s , \dot{s} and λ to be extracted from actual **measurements** !



“Filtering” position and force measures

- ➔ s and \dot{s} are obtained from measures of q and \dot{q} , equating the descriptions of the end-effector pose and velocity “from the robot side” (direct and differential kinematics) and “from the environment side” (function of s, \dot{s})

example

$${}^0r = {}^0f(q) = \begin{pmatrix} L \cos s \\ L \sin s \\ 0 \end{pmatrix} \Rightarrow s = \text{atan2}\{ {}^0f_y(q), {}^0f_x(q) \}$$

$$J(q)\dot{q} = T(s)\dot{s} \Rightarrow \dot{s} = T^\#(s)J(q)\dot{q}$$

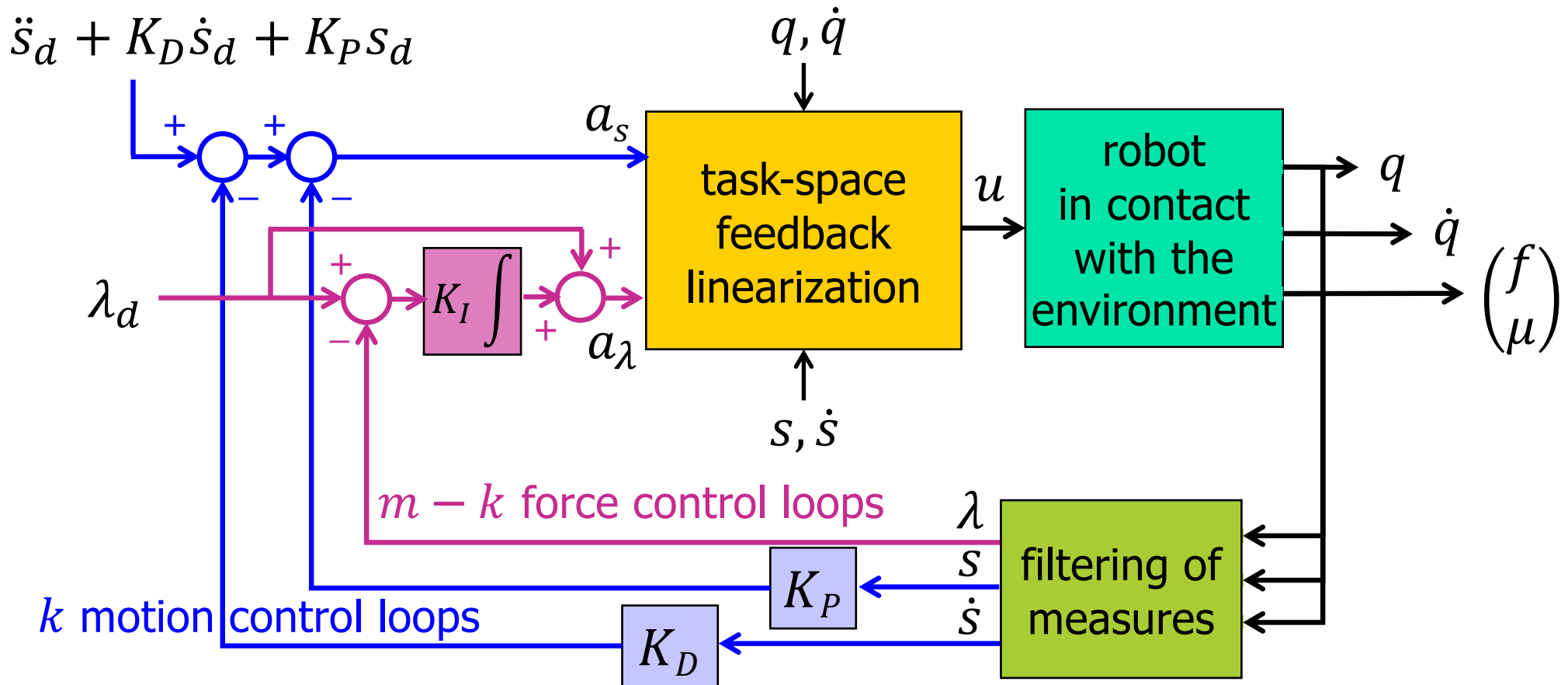
- ➔ λ is obtained from force/torque measures at end-effector

$$\begin{pmatrix} f \\ m \end{pmatrix} = Y(s)\lambda \Rightarrow \lambda = Y^\#(s) \begin{pmatrix} f \\ m \end{pmatrix}$$

pseudoinverses of “tall” matrices having full column rank, e.g.,
 $T^\# = (T^T T)^{-1} T^T$
 (or weighted)



Block diagram of hybrid control



usually $m = 6$ (complete 3D space)

limit cases $k = m$: no force control loops, only motion (free motion)

$k = 0$: no motion control loops, only force ("frozen" robot end-effector)



Block diagram of hybrid control

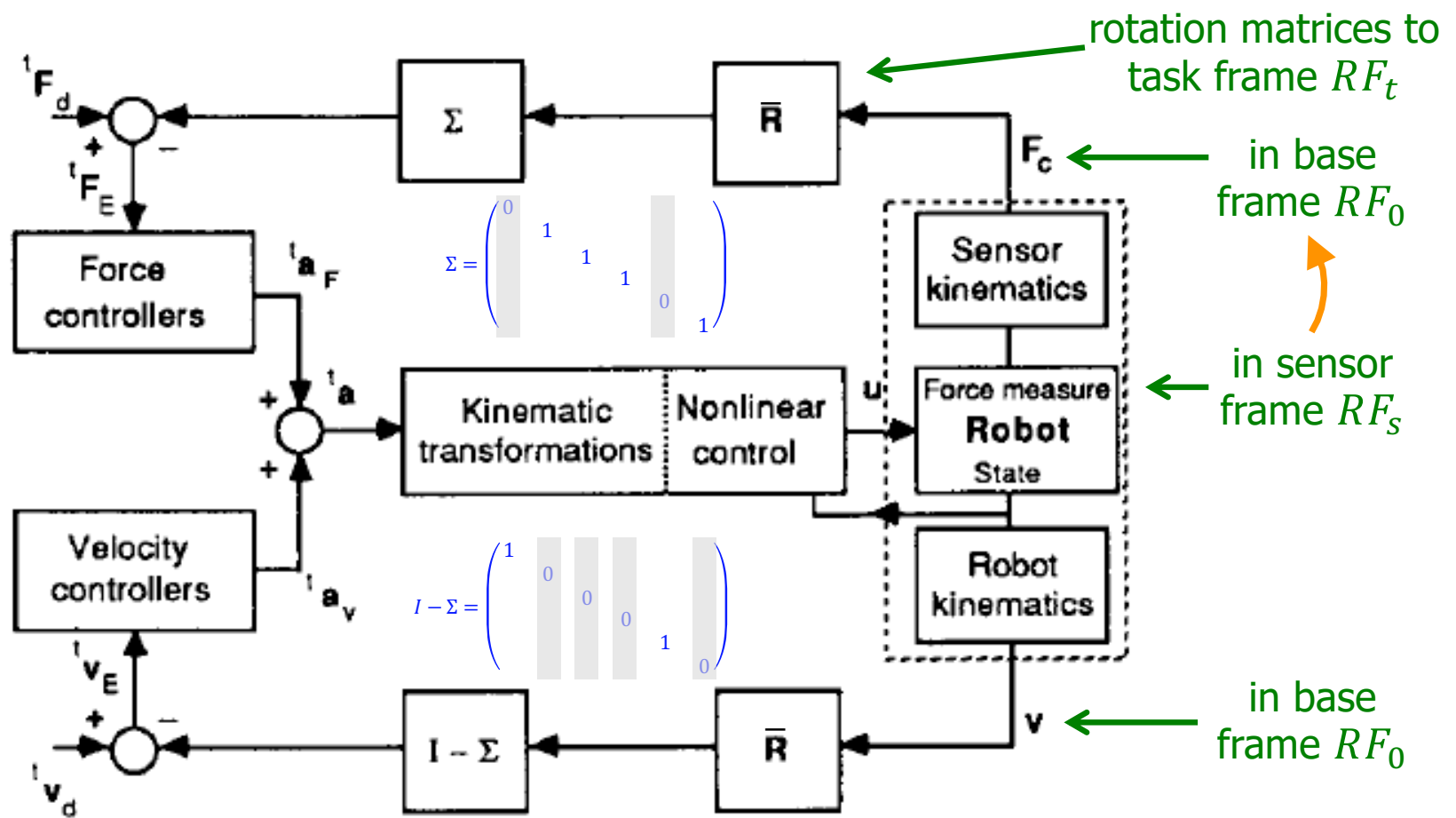
simpler case of 0/1 selection matrices

compact notation in this slide

$$F = \begin{pmatrix} f \\ \mu \end{pmatrix}$$

$$V = \begin{pmatrix} v \\ \omega \end{pmatrix}$$

$$\bar{R} = \begin{pmatrix} R & 0 \\ 0 & R \end{pmatrix}$$



λ and \dot{s} are just single components of f (or μ) and v (or ω)
 Y and T are replaced by 0/1 selection matrices: Σ and $I - \Sigma$

illustrated here for example 1, slide #5 (discarding 0 columns to get Y and T)

Force control via an impedance model



- in a force-controlled direction of the hybrid task space, when the **contact stiffness is limited** (i.e., far from infinite, as assumed in the ideal case), one may use **impedance model ideas** to explicitly **control the contact force**
 - let x be the position of the robot along such a direction, x_d the (constant) contact point, $k_s > 0$ the contact (viz., sensor) stiffness, and $f_d > 0$ the desired contact force
- the impedance model is chosen then as

$$m_m \ddot{x} + d_m \dot{x} + k_s (x - x_d) = f_d$$

where the **force sensor** measures $f_s = k_s (x - x_d)$, and only $m_m > 0$ and $d_m > 0$ are free model parameters

- after feedback linearization ($\ddot{x} = a_x$), the command a_x is designed as

$$a_x = (1/m_m) [(f_d - f_s) - d_m \dot{x}]$$

which is a **P-regulator** of the desired force, **with velocity damping**

- the **same** control law works also before the contact ($f_s = 0$), guaranteeing a steady-state speed $\dot{x}_{ss} = f_d/d_m > 0$ in the **approaching phase**



First experiments with hybrid control

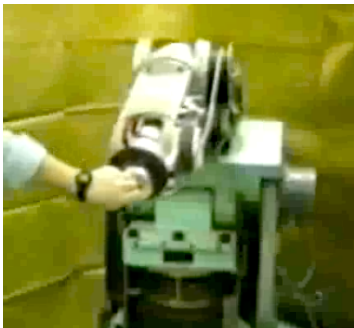
First Experiments with Hybrid Force/Velocity Control

Università di Roma "La Sapienza"
DIS, LabRob
February 1991

First Experiments with Hybrid Force/Velocity Control

(part II)

Università di Roma "La Sapienza"
DIS, LabRob
February 1991



video



video

MIMO-CRF robot
(DIS, Laboratorio di Robotica, 1991)

Sources of inconsistency in force and velocity measurements



1. presence of **friction** at the contact

- a reaction force component appears that opposes motion in a “free” motion direction (in case of Coulomb friction, the tangent force intensity depends also on the applied normal force ...)

2. **compliance** in the robot structure and/or at the contact

- a (small) displacement may be present also along directions that are nominally “constrained” by the environment

NOTE: if the environment geometry at the contact is perfectly known, the task inconsistencies due to 1. and 2. on parameters s and λ are already **filtered out** by the pseudo-inversion of matrices T and Y

3. uncertainty on **environment geometry** at the contact

- can be reduced/eliminated by real-time **estimation processes** driven by external sensors (e.g., vision –but also force!)

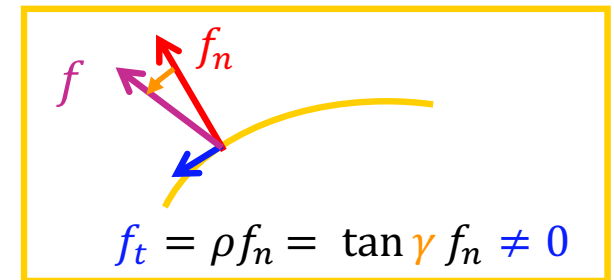


Estimation of an unknown surface

how difficult is to **estimate** the unknown profile of the environment surface, using information from velocity and force measurements at the contact?

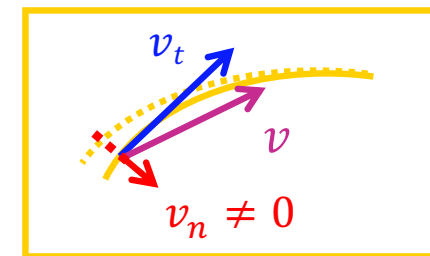
1. **normal** = nominal direction of measured **force**

... in the presence of contact motion with friction, the **measured** force f is slightly rotated from the actual normal by an (unknown) angle γ



2. **tangent** = nominal direction of measured **velocity**

... compliance in the robot structure (joints) and/or at the contact may lead to a **computed** velocity v having a small component along the actual normal to the surface



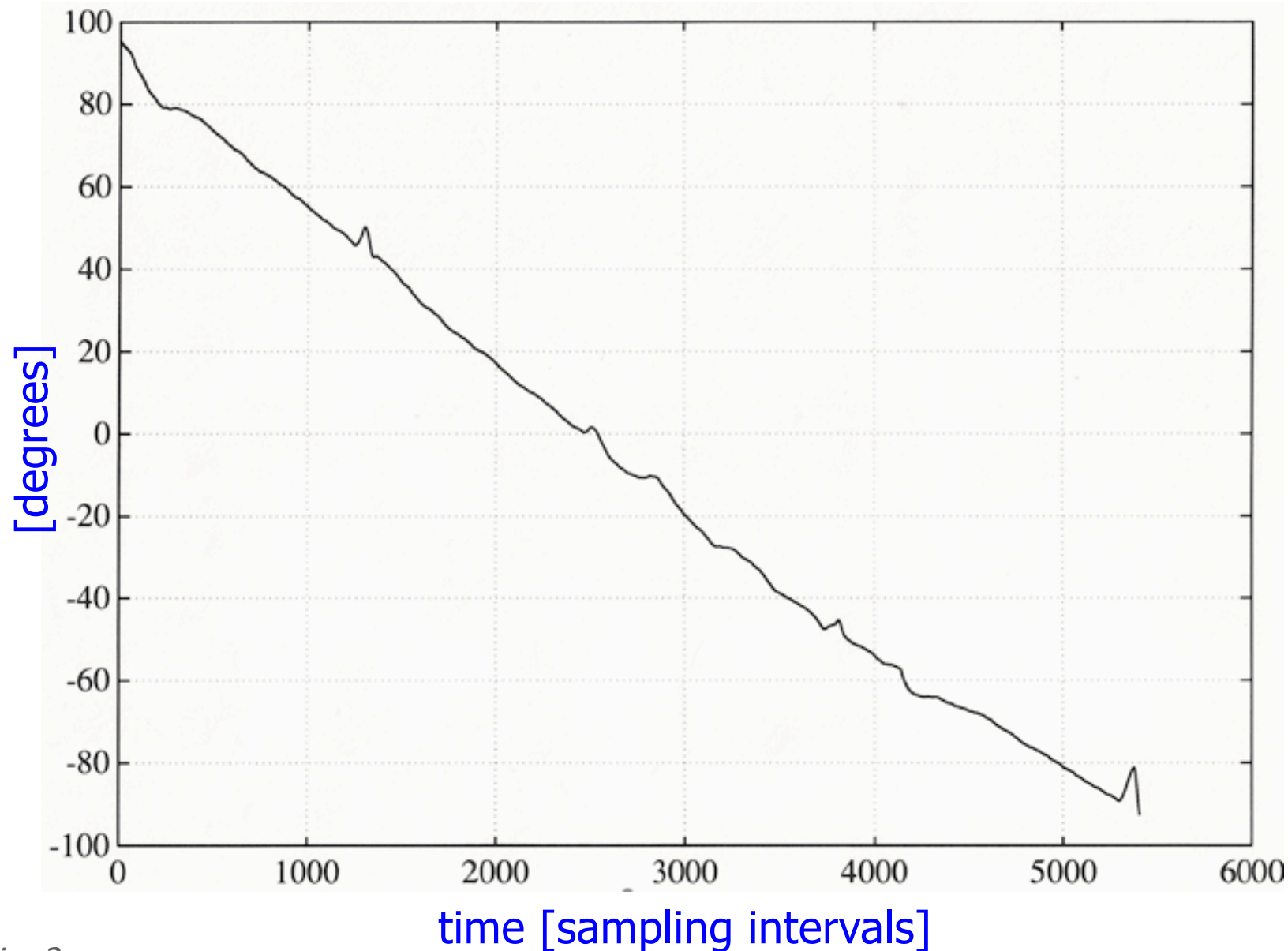
3. mixed method (**sensor fusion**) with RLS

- tangent direction is estimated by a **recursive least squares** method from position measurements
- friction angle is estimated by a **recursive least squares** method, using the current estimate of the tangent direction and from force measurements

to approach an unknown surface or to recover contact (in case of loss), the robot uses simple exploratory moves

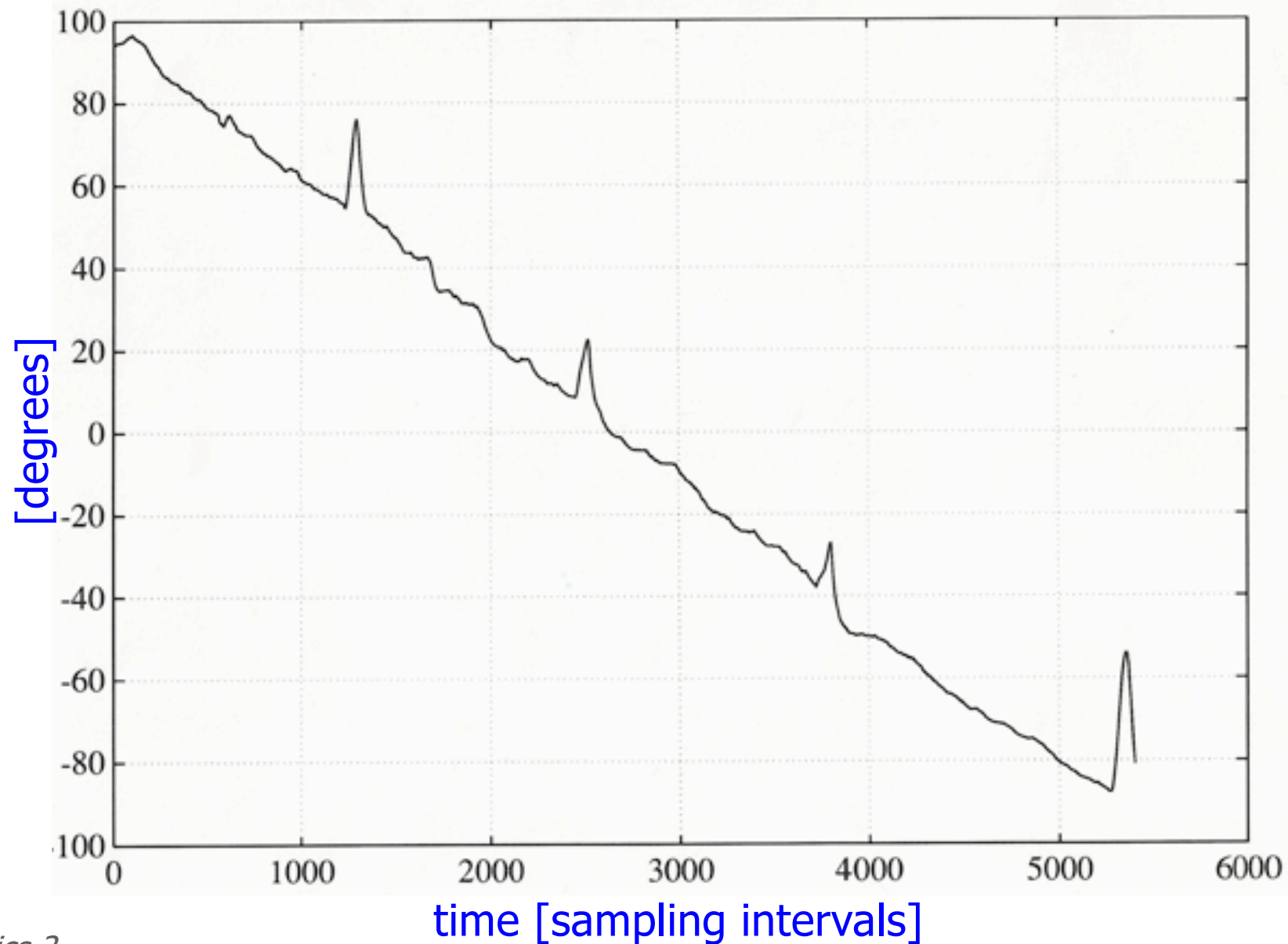
Position-based estimation of the tangent

(for a **circular** surface traced at constant speed)



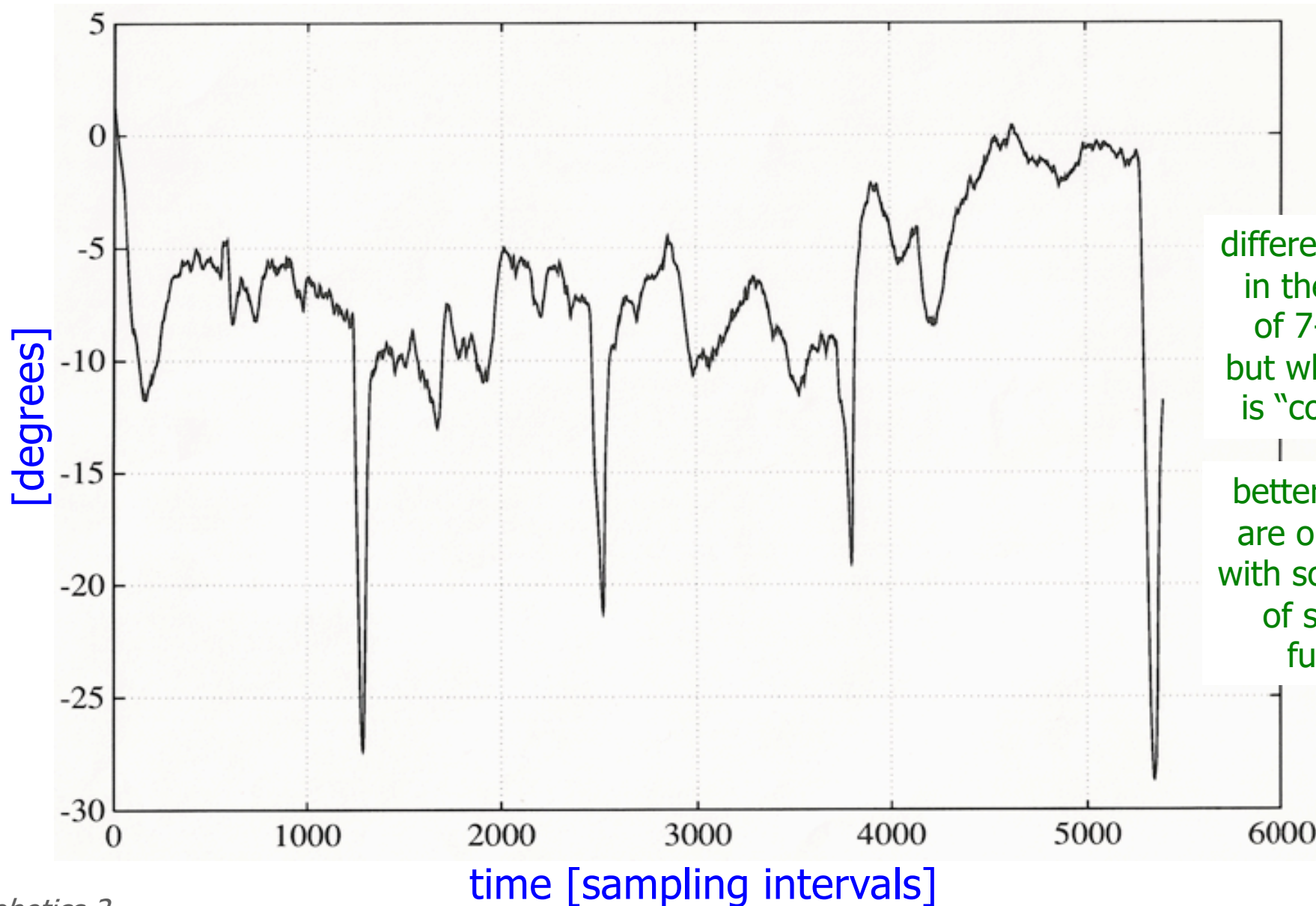
Force-based estimation of the tangent

(for the same **circular** surface traced at constant speed)





Difference between estimated tangents



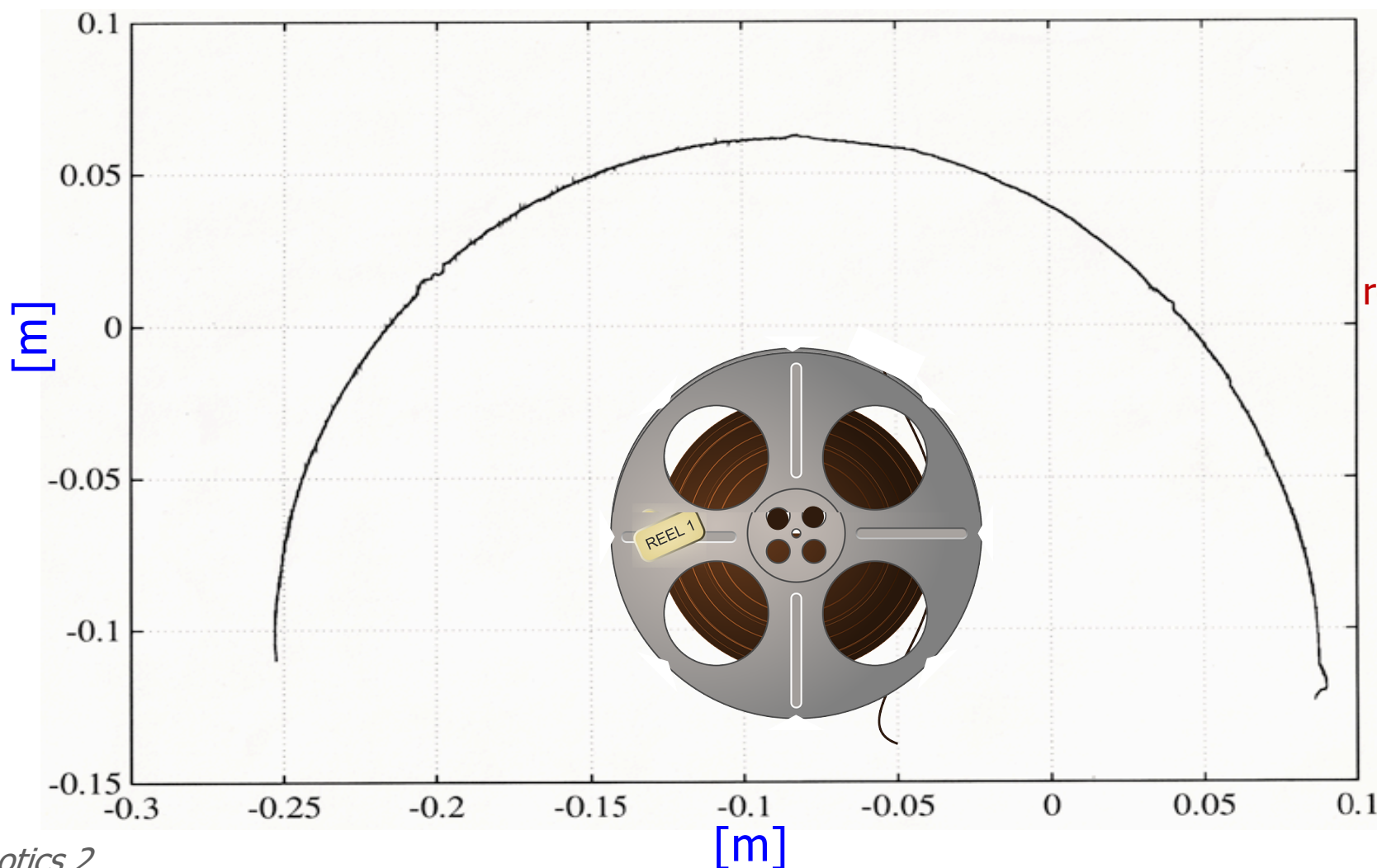
differences are
in the order
of 7-8° ...
but which one
is "correct"?

better results
are obtained
with some kind
of sensor
fusion



Reconstructed surface profile

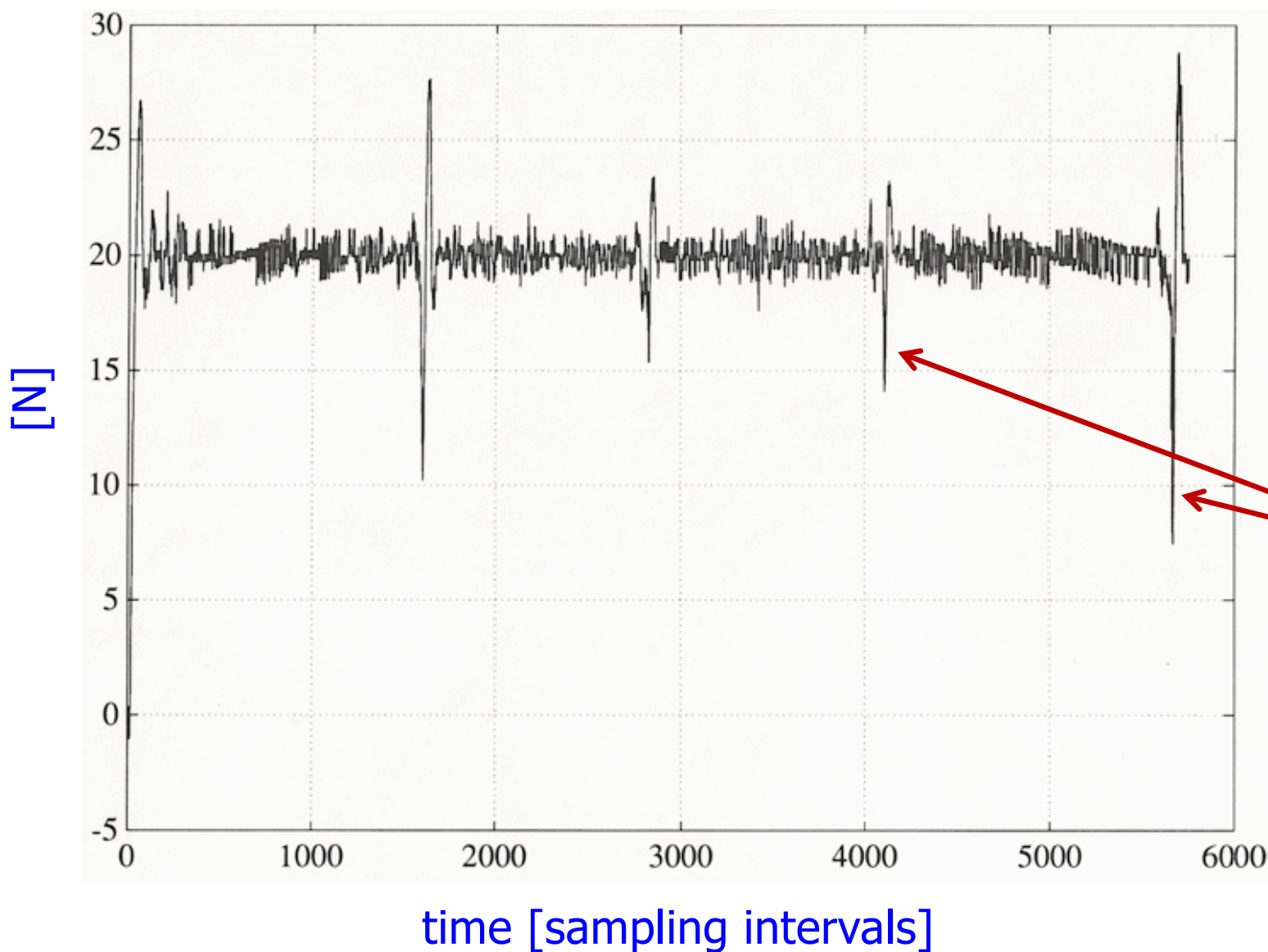
estimation by a RLS (Recursive Least Squares) method: we continuously update the coefficients of two quadratic polynomials that fit locally the unknown contour, using data fusion from both force and position/velocity measurements



this is the reconstructed contour of a cinema "film reel" (of radius = 17 cm)



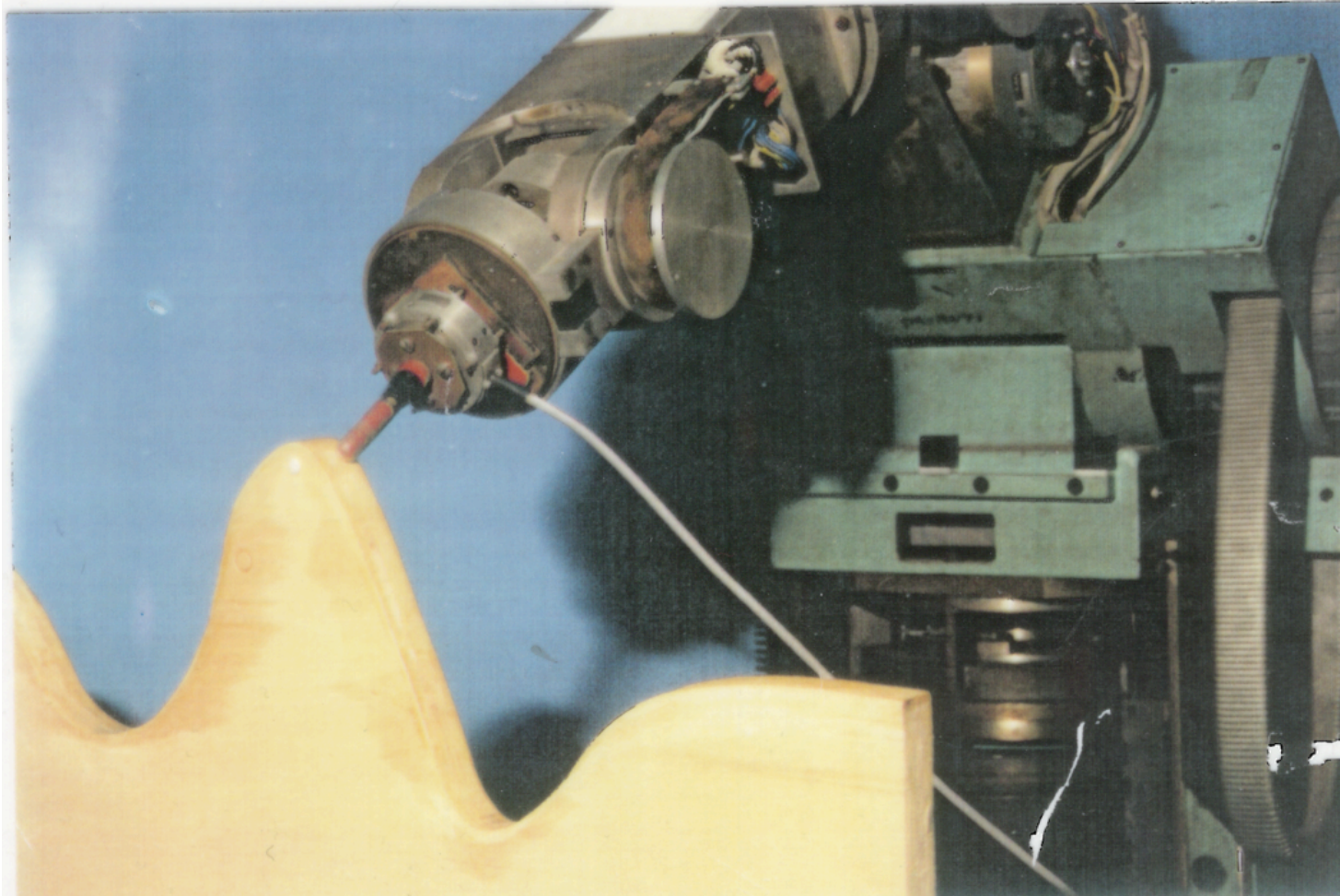
Normal force



regulated
to 20 N
during
simultaneous
motion and
estimation

force peaks
correspond
to the grooves
on the surface
contour

Contour estimation and hybrid control performed simultaneously



MIMO-CRF robot (DIS, Laboratorio di Robotica, 1992)

Contour estimation and hybrid control



Hybrid Force/Velocity Control and Identification of Surfaces

**Università di Roma "La Sapienza"
DIS, LabRob
September 1992**



video

Robotized deburring of car windshields

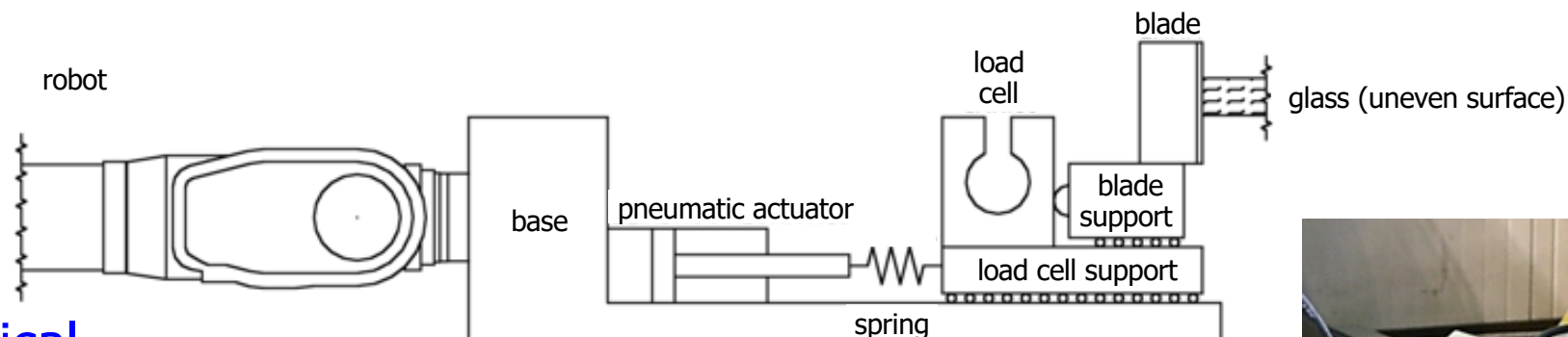


- car windshield with **sharp edges** and fabrication tolerances, with **excess of material** (PVB = Polyvinyl butyral for gluing glass layers) on the contour
- robot end-effector follows the pre-programmed path, despite the small errors w.r.t. the nominal windshield profile, thanks to the **compliance** of the deburring tool
- contact force between tool blades and workpiece can be independently controlled by a **pneumatic actuator** in the tool

the robotic deburring tool contains in particular

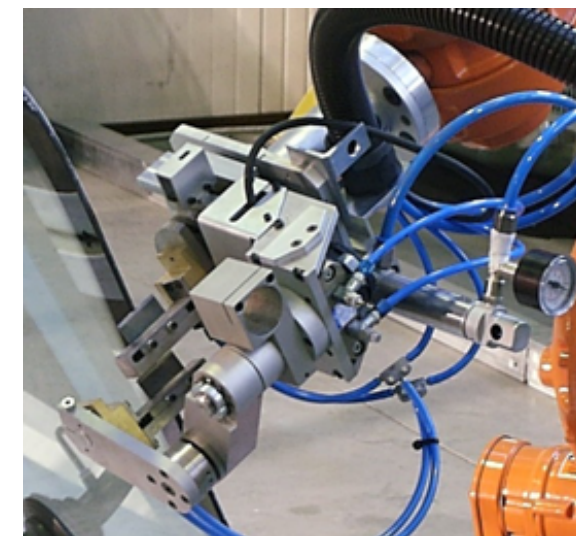
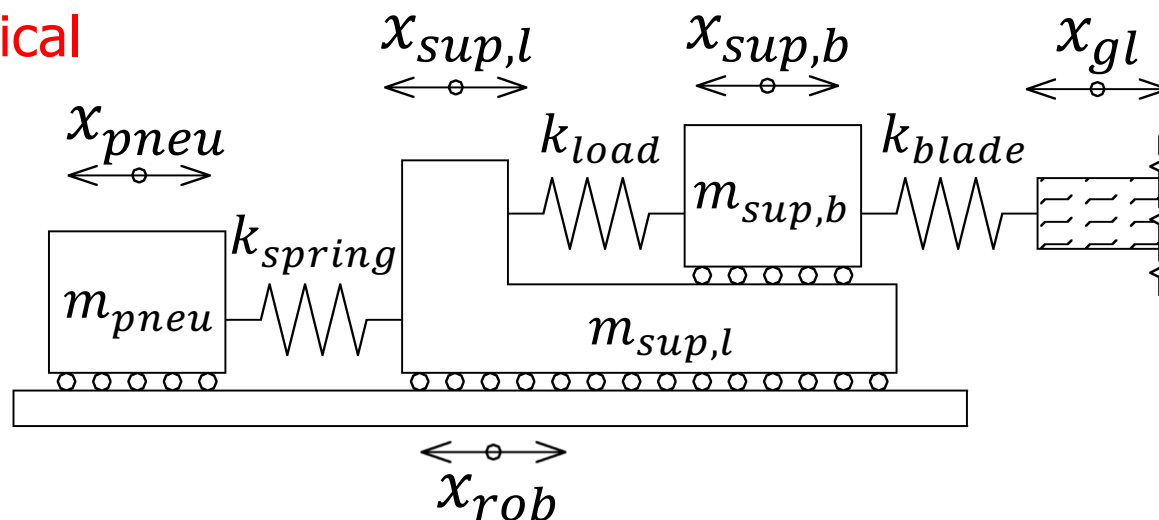
- **two blades** for cutting the exceeding plastic material (PVB), the first one actuated, the second passively pushed against the surface by a spring
- a **load cell** for measuring the 1D applied normal force at the contact
- on-board **control system**, exchanging data with the ABB robot controller

Model of the deburring work tool



physical

mathematical



for a stability analysis (based on linear models and root locus techniques) of force control in a single direction and in presence of multiple masses/springs, see again Eppinger & Seering, IEEE CSM, 1987 (material in the course web site)

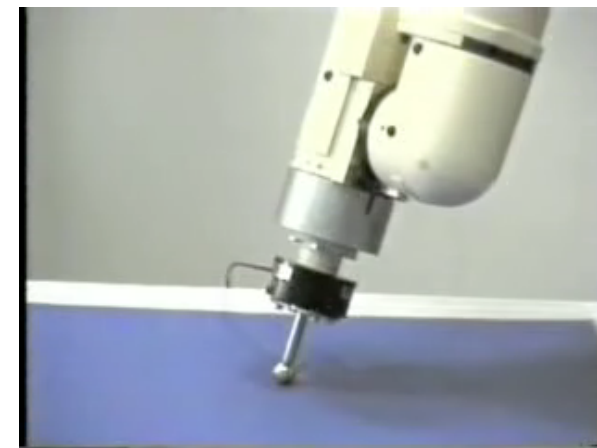
Summary through video segments



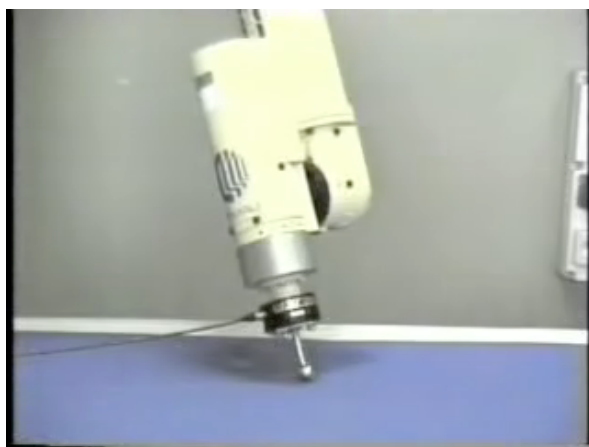
compliance control
(active Cartesian stiffness control **without** F/T sensor)



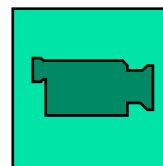
impedance control
(with F/T sensor)



force control
(realized as external loop providing the reference to an internal position loop
-see Appendix)



hybrid force/position control



COMAU Smart robot
c/o Università di Napoli, 1994
(full video on course web site)



Appendix

- force control can also be realized as an external loop providing reference values to an internal motion loop (see video in slide #32)
- inner-outer (or cascaded) control scheme
 - angular position quantities (E-E orientation, errors, commands) can be expressed in different ways (Euler angles ϕ , rotation matrices R , ...)

