

#### **Robotics 1**

#### **Kinematic control**

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#### Robot motion control



- need to "actually" realize a desired robot motion task ...
  - regulation of pose/configuration (constant reference)
  - trajectory following/tracking (time-varying reference)
- ... despite the presence of
  - external disturbances and/or unmodeled dynamic effects
  - initial errors (or arising later due to disturbances) w.r.t. desired task
  - discrete-time implementation, uncertain robot parameters, ...
- we use a general control scheme based on
  - feedback (from robot state measures, to impose asymptotic stability)
  - feedforward (nominal commands generated in the planning phase)
- the error driving the feedback part of the control law can be defined either in Cartesian or in joint space
  - control action always occurs at the joint level (where actuators drive the robot), but performance has to be evaluated at the task level

#### Kinematic control of robots

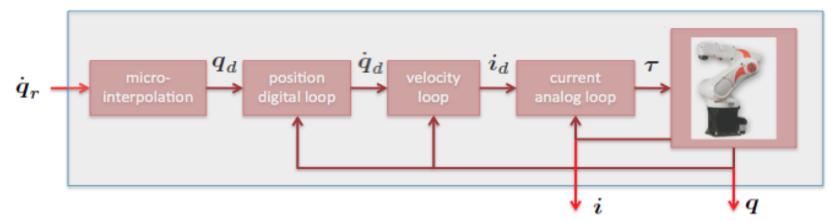


- a robot is an electro-mechanical system driven by actuating torques produced by the motors
- it is possible, however, to consider a kinematic command (most often, a velocity) as control input to the system...
- ...thanks to the presence of low-level feedback control at the robot joints that allows imposing commanded reference velocities (at least, in the "ideal case")
- these feedback loops are present in industrial robots within a "closed" control architecture, where users can only specify reference commands of the kinematic type
- in this way, performance can be very satisfactory, provided the desired motion is not too fast and/or does not require large accelerations

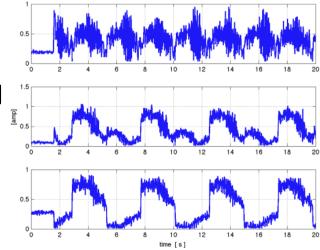
#### Closed control architecture



KUKA KR5 Sixx R650 robot



- low-level motor control laws are not known nor accessible by the user
- user programs, based also on other exteroceptive sensors (vision, Kinect, F/T sensor) can be implemented on an external PC via the RSI (RobotSensorInterface), communicating with the KUKA controller every 12 ms
- available robots measures: joint positions (by encoders)
   and (absolute value of) applied motor currents
- controller reference is given as a velocity or a position in joint space (also Cartesian commands are accepted)

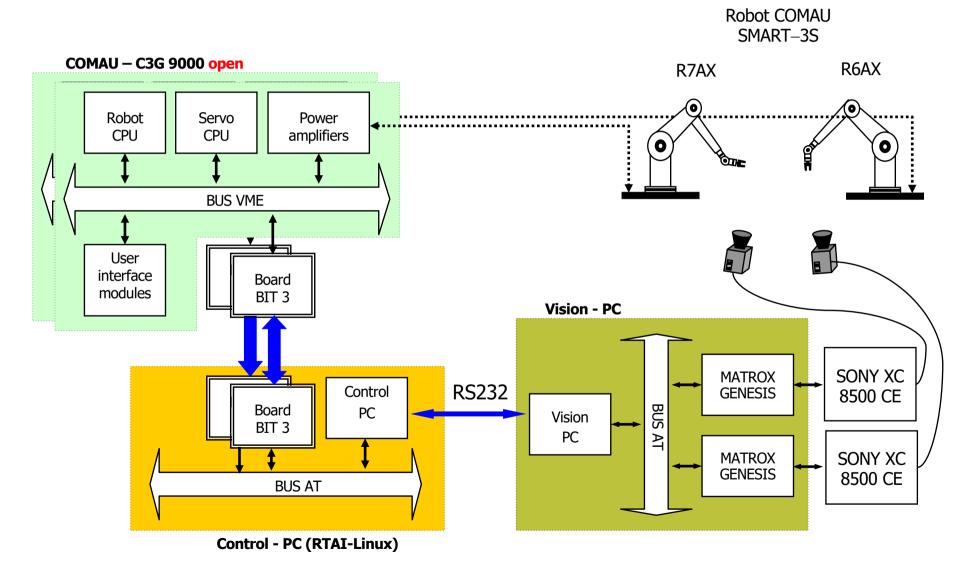


typical motor currents on first three joints

#### Hardware architecture

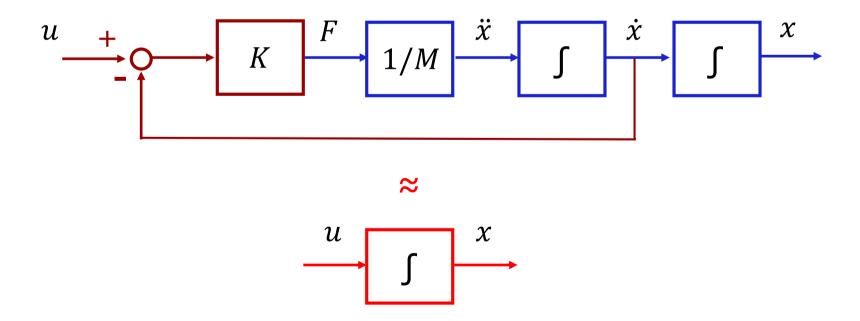


Example including vision in an open controller





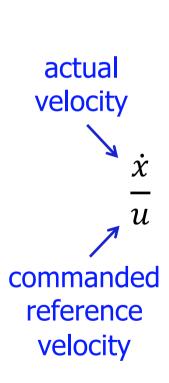
- An introductory example
- a mass M in linear motion:  $M\ddot{x} = F$
- low-level feedback:  $F = K(u \dot{x})$ , with u = reference velocity
- equivalent scheme for  $K \to \infty$ :  $\dot{x} \approx u$
- in practice, valid in a limited frequency "bandwidth"  $\omega \leq K/M$

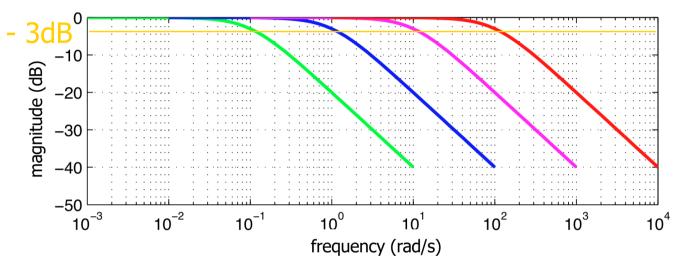


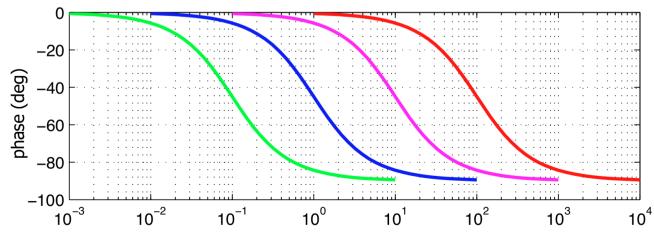
# Frequency response of the closed-loop system



■ Bode diagrams of 
$$P(s) = \frac{v(s)}{u(s)} = \frac{sx(s)}{u(s)}$$
 for  $K/M = 0.1, 1, 10, 100$ 



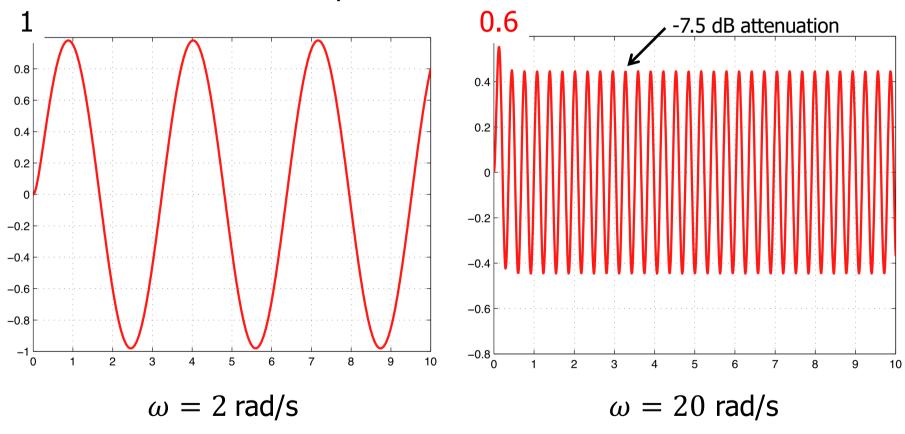






# Time response

setting K/M=10 (bandwidth), we show two possible time responses to unit sinusoidal velocity reference commands at different  $\omega$ 



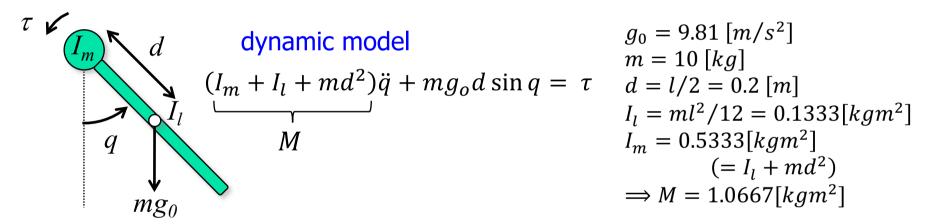
actually realized velocities

## A more detailed example



#### including nonlinear dynamics

• single link (a thin rod) of mass m, center of mass at d from joint axis, inertia M (motor + link) at the joint, rotating in a vertical plane (the gravity torque at the joint is configuration dependent)



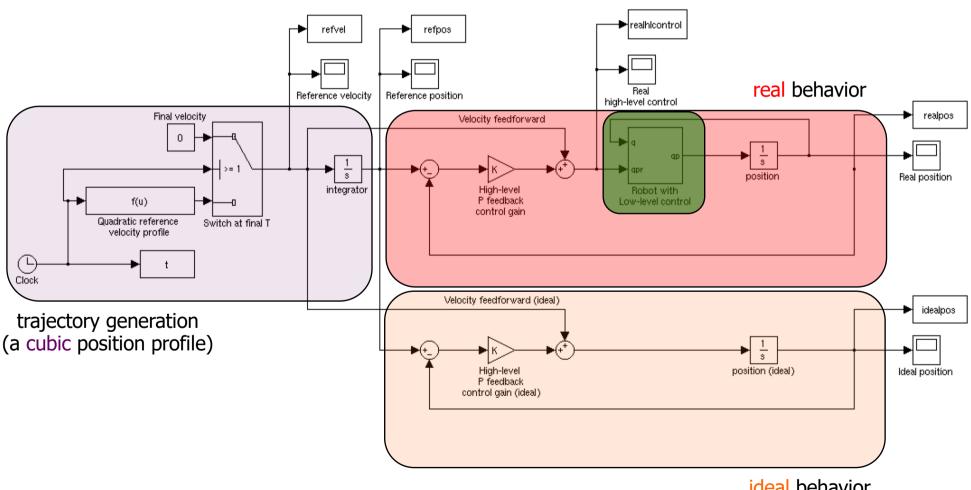
- fast low-level feedback control loop based on a PI action on the velocity error + an approximate acceleration feedforward
- kinematic control loop based on a P feedback action on the position error + feedforward of the velocity reference at the joint level
- evaluation of tracking performance for rest-to-rest motion tasks with "increasing dynamics" = higher accelerations

# A more detailed example





#### Simulink scheme



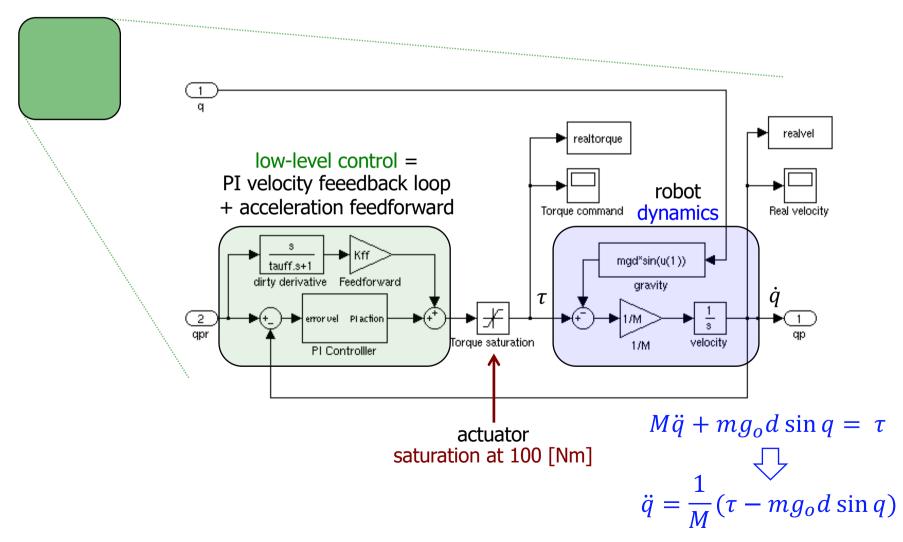
ideal behavior

# A more detailed example





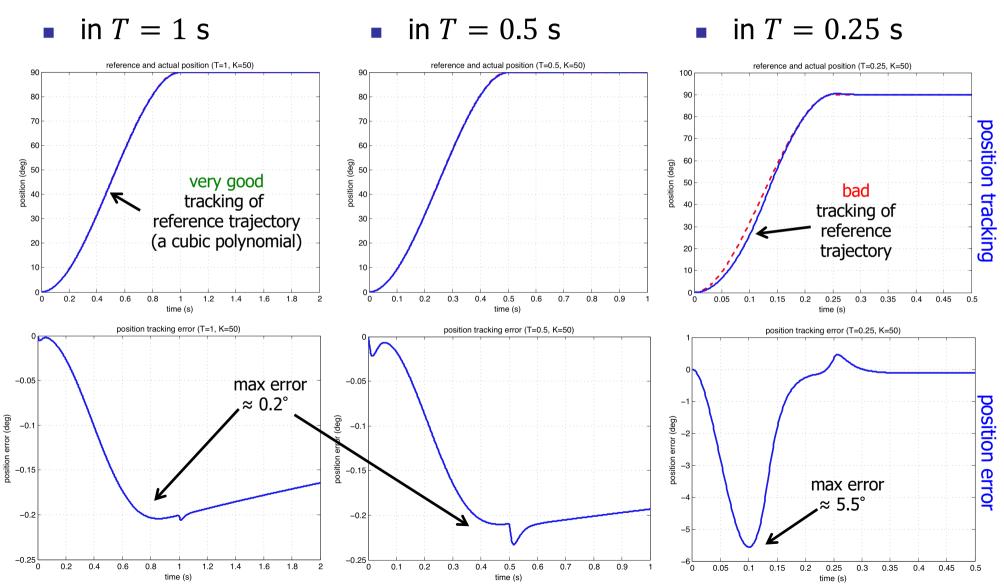
#### Simulink scheme



#### Simulation results



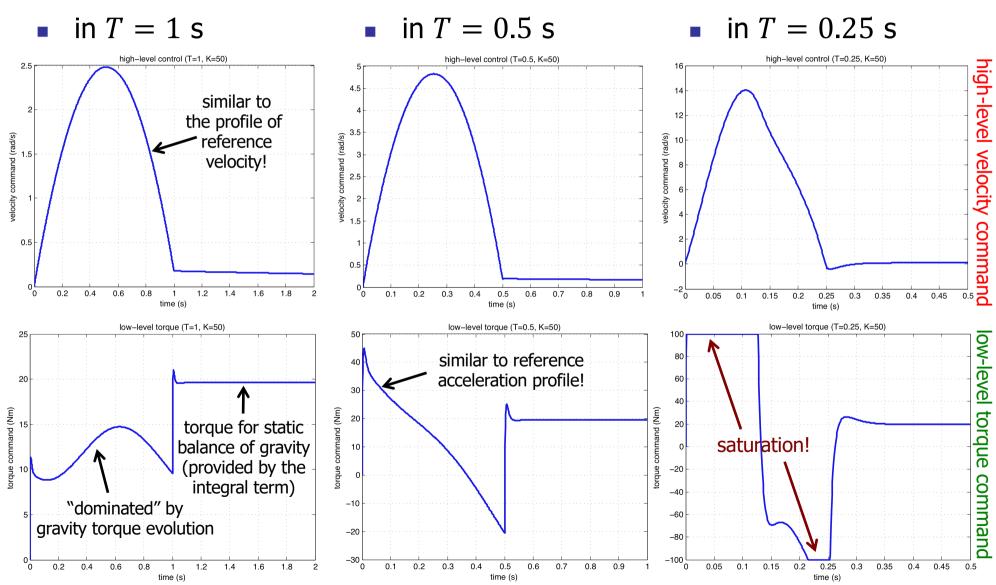
rest-to-rest motion from downward to horizontal position



#### Simulation results



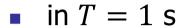
#### rest-to-rest motion from downward to horizontal position



#### Simulation results

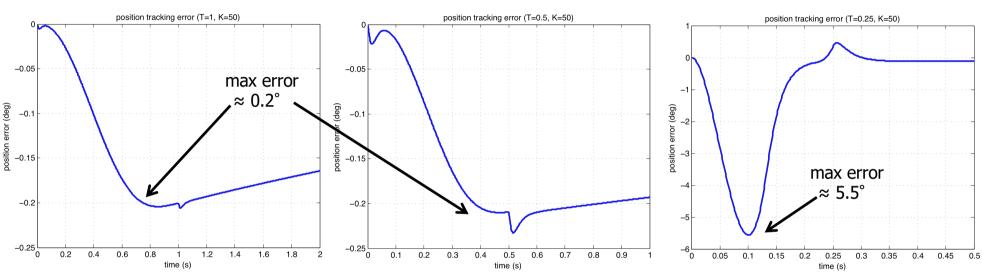


#### rest-to-rest motion from downward to horizontal position



• in 
$$T = 0.5 \text{ s}$$

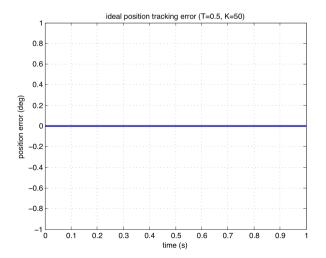
• in 
$$T = 0.25 \text{ s}$$



real position errors increase when reducing too much motion time

(⇒ too high accelerations)

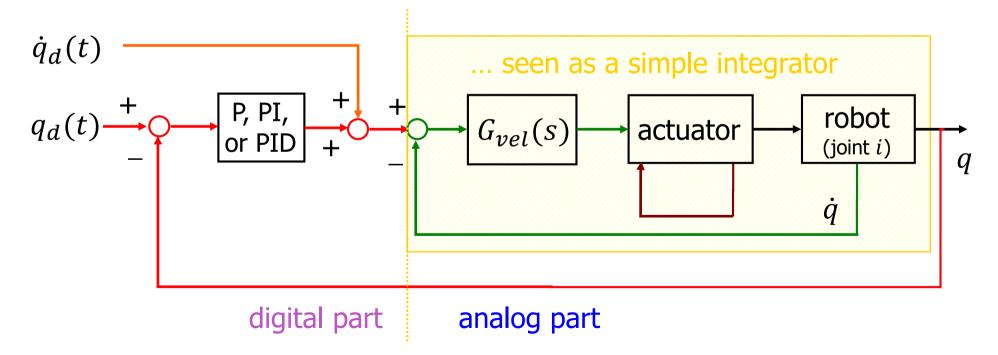
while ideal position errors
(based only on kinematics)
remain always the same!!
here = 0, thanks to the initial matching
between robot and reference trajectory





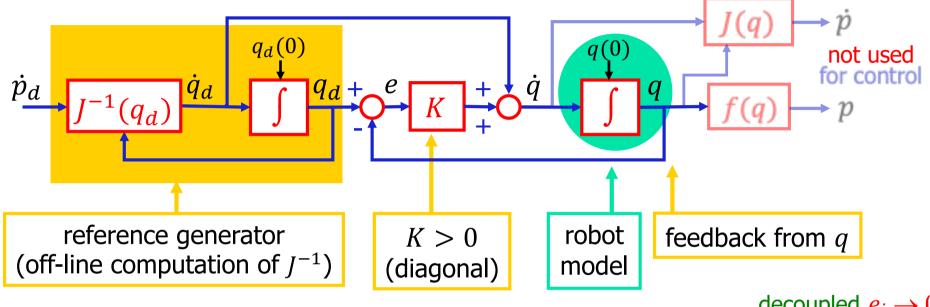
# Control loops in industrial robots

- analog loop on velocity  $(G_{vel}(s), \text{ typically a PI})$
- digital feedback loop on position, with velocity feedforward
- this scheme is local to each joint (decentralized control)





# Kinematic control of joint motion

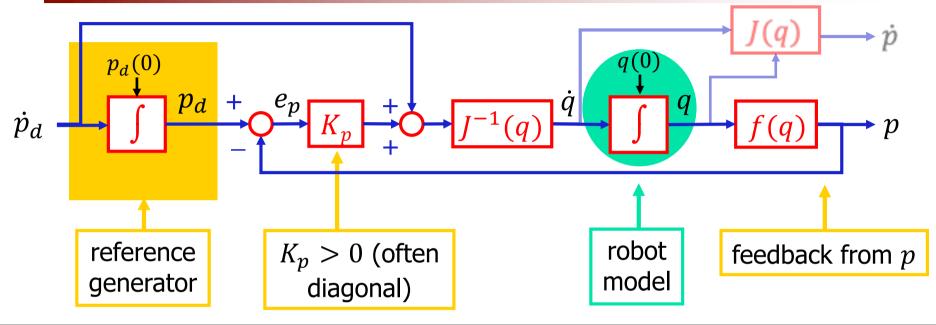


$$e = q_d - q \implies \dot{e} = \dot{q}_d - \dot{q} = \dot{q}_d - (\dot{q}_d + K(q_d - q)) = -Ke$$

decoupled  $e_i \rightarrow 0$   $(i = 1, \dots, n)$ exponentially,  $\forall e(0)$ 







$$e_p = p_d - p \implies \dot{e}_p = \dot{p}_d - \dot{p} = \dot{p}_d - J(q)J^{-1}(q)\left(\dot{p}_d + K_p(p_d - p)\right) = -K_p e_p$$

- decoupled  $e_{p,i} \to 0$   $(i = 1, \dots, m)$  exponentially,  $\forall e_p(0)$
- needs on-line computation of the inverse<sup>(\*)</sup>  $J^{-1}(q)$
- real-time + singularities issues

 $^{(*)}$  or pseudoinverse if m < n

#### **Simulation**





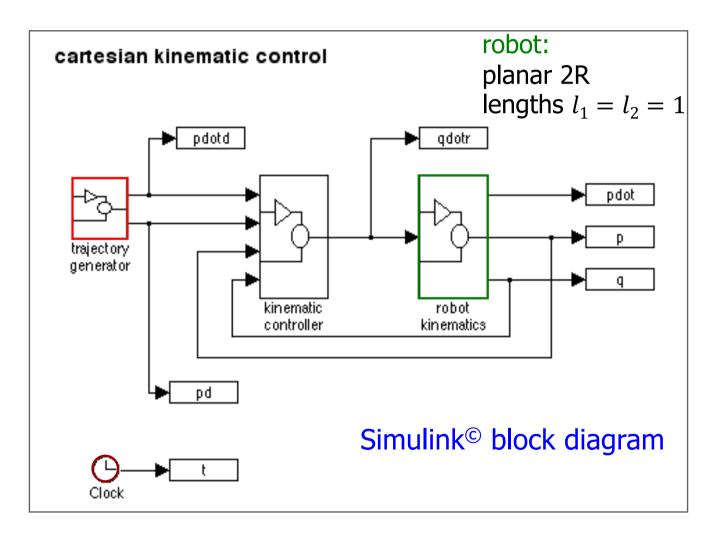
# desired reference trajectory:

two types of tasks

- 1. straight line
- 2. circular path both with constant speed

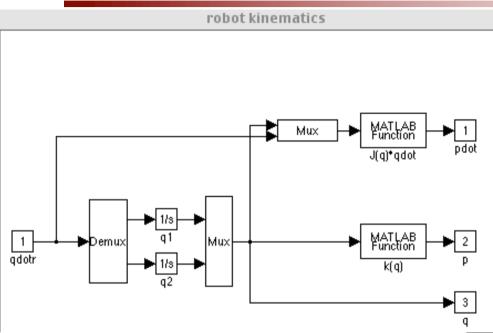
# numerical integration method:

fixed step Runge-Kutta at 1 msec



#### Simulink blocks





calls to Matlab functions

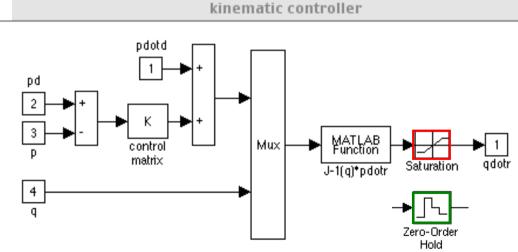
k(q)=dirkin (user)

J(q)=jac (user)

J-1(q)=inv(jac) (library)

- a saturation (for task 1.)
   or a sample and hold (for task 2.)
   added on joint velocity commands
- system initialization of kinematics data, desired trajectory, initial state, and control parameters (in init.m file)

never put "numbers" inside the block's !



#### Matlab functions



```
dirkin.m

function [p] = dirkin(q)

global l1 l2

px=l1*cos(q(1))+l2*cos(q(1)+q(2));
py=l1*sin(q(1))+l2*sin(q(1)+q(2));
```

```
jac.m

function [J] = jac(q)

global l1 l2

J(1,1)=-l1*sin(q(1))-l2*sin(q(1)+q(2))
J(1,2)=-l2*sin(q(1)+q(2));
J(2,1)=l1*cos(q(1))+l2*cos(q(1)+q(2));
J(2,2)=l2*cos(q(1)+q(2));
```

```
init.m
% controllo cartesiano di un robot 2R
% initialization
clear all: close all
alobal 11 12
% lunghezze bracci robot 2R
11=1: 12=1:
% velocità cartesiana desiderata (costante)
vxd=0; vyd=0.5;
% tempo totale
                                                      init_m
T=2;
                                                      script
% configurazione desiderata iniziale
                                                  (for task 1.)
q1d0=-45*pi/180; q2d0=135*pi/180;
pd0=dirkin([q1d0 q2d0]");
pxd0=pd0(1); pyd0=pd0(2);
% configurazione attuale del robot
q10=-45*pi/180; q20=90*pi/180;
p0=dirkin([a10 a20]");
% matrice dei guadagni cartesiani
K=[20 \ 20]; K=diag(K);
%saturazioni di velocità ai giunti (input in deg/sec, convertito in rad/sec)
vmax1=120*pi/180; vmax2=90*pi/180;
```



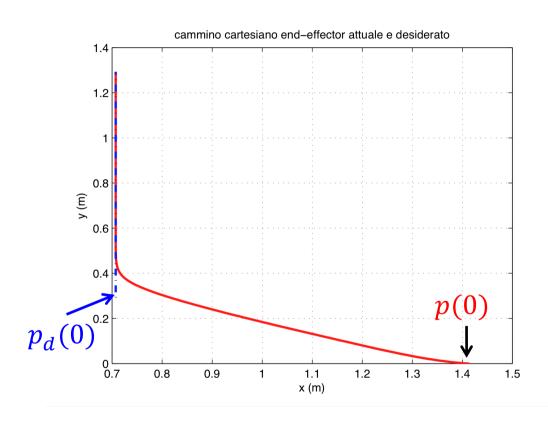
#### Simulation data for task 1

- straight line path with constant velocity
  - $x_d(0) = 0.7 \text{ m}, y_d(0) = 0.3 \text{ m}; v_{d,y} = 0.5 \text{ m/s, for } T = 2 \text{ s}$
- large initial error on end-effector position
  - $q(0) = (-45^{\circ}, 90^{\circ}) \Rightarrow e_{p}(0) = (-0.7, 0.3) \text{ m}$
- Cartesian control gains
  - $K_p = \text{diag}\{20, 20\}$
- (a) without joint velocity command saturation
- (b) with saturation ...
  - $v_{max,1} = 120^{\circ}/\text{s}, v_{max,2} = 90^{\circ}/\text{s}$

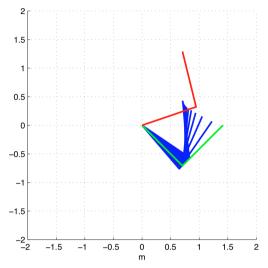
#### Results for task 1a





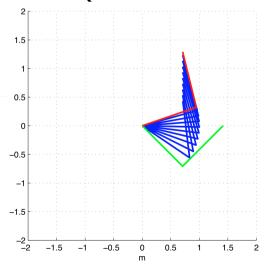


path executed by the robot end-effector (actual and desired)



initial transient phase (about 0.2 s)

stroboscopic view of motion (start and end configurations)

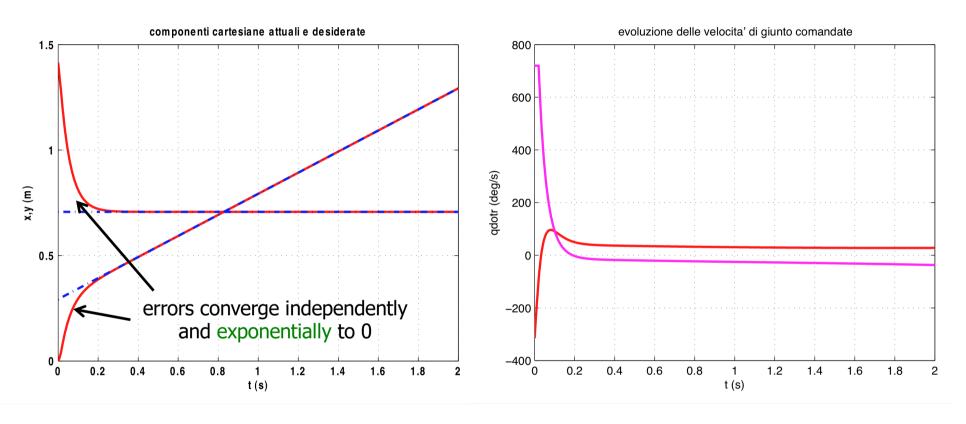


trajectory following phase (about 1.8 s)

# Results for task 1a (cont)



straight line: initial error, no saturation



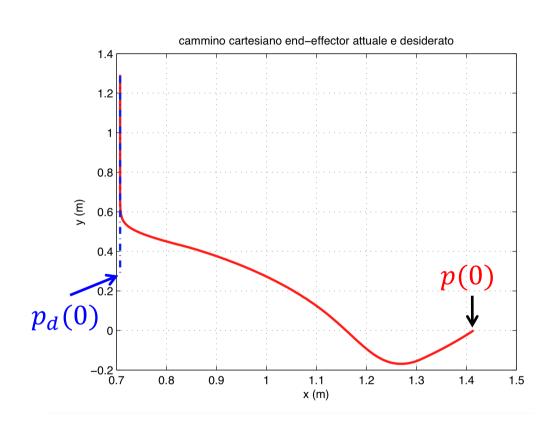
 $p_x$ ,  $p_y$  actual and desired

control inputs  $\dot{q}_{r1}$ ,  $\dot{q}_{r2}$ 

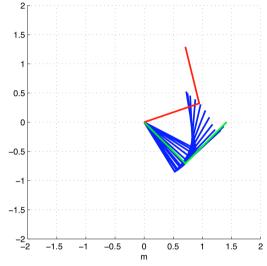
#### Results for task 1b





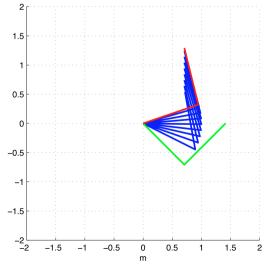


path executed by the robot end-effector (actual and desired)



initial transient phase (about 0.5 s)

stroboscopic view of motion (start and end configurations)



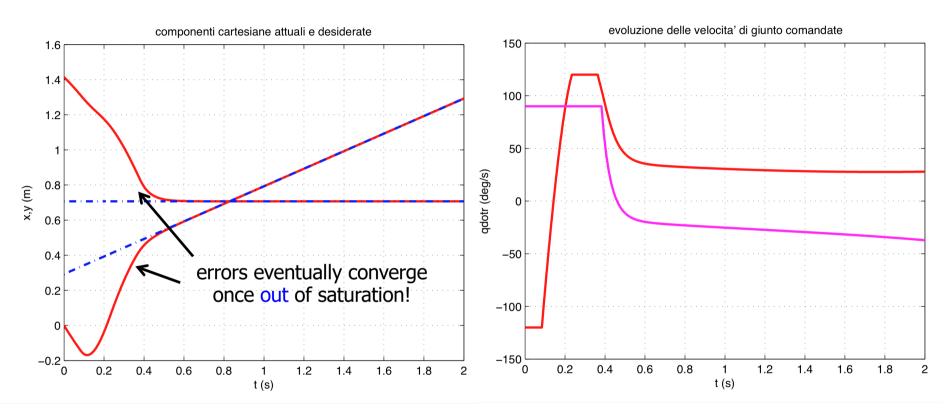
trajectory following phase (about 1.5 s)

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# Results for task 1b (cont)



straight line: initial error, with saturation



 $p_x$ ,  $p_y$  actual and desired

control inputs 
$$\dot{q}_{r1}$$
,  $\dot{q}_{r2}$  (saturated at  $\pm$   $v_{max,1}$ ,  $\pm$   $v_{max,2}$ )

## Simulation data for task 2

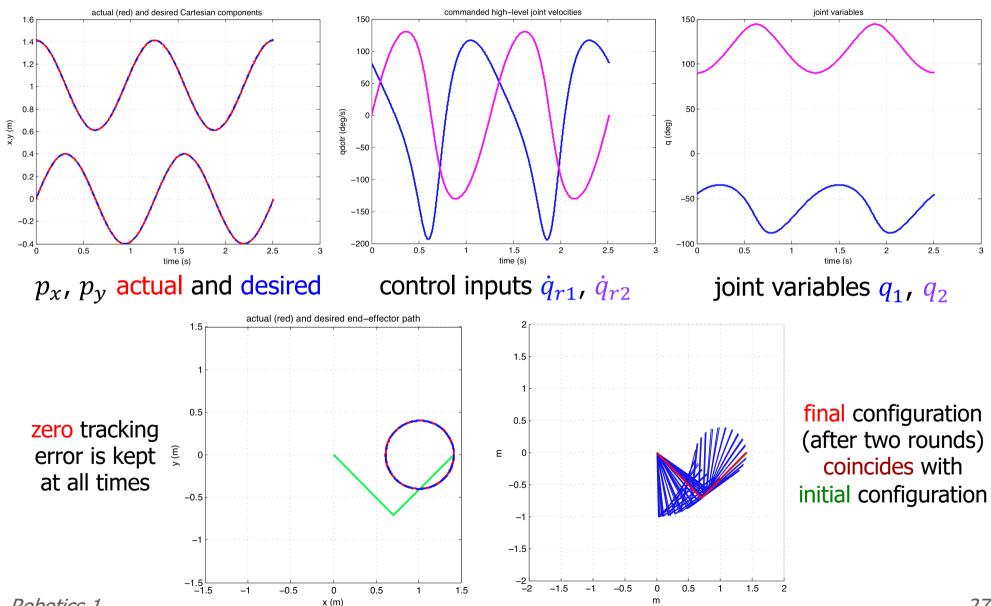


- circular path with constant velocity
  - centered at (1.014, 0) with radius R = 0.4 m;
  - v = 2 m/s, performing two rounds  $\Rightarrow T \approx 2.5$  s
- zero initial error on Cartesian position ("match")
  - $q(0) = (-45^{\circ}, 90^{\circ}) \Rightarrow e_p(0) = 0$
- (a) ideal continuous case (1 kHz), even without feedback
- (b) with sample and hold (ZOH) of  $T_{hold} = 0.02$  s (joint velocity command updated at 50 Hz), but without feedback
- (c) as before, but with Cartesian feedback using the gains
  - $K_p = \text{diag}\{25, 25\}$

#### Results for task 2a



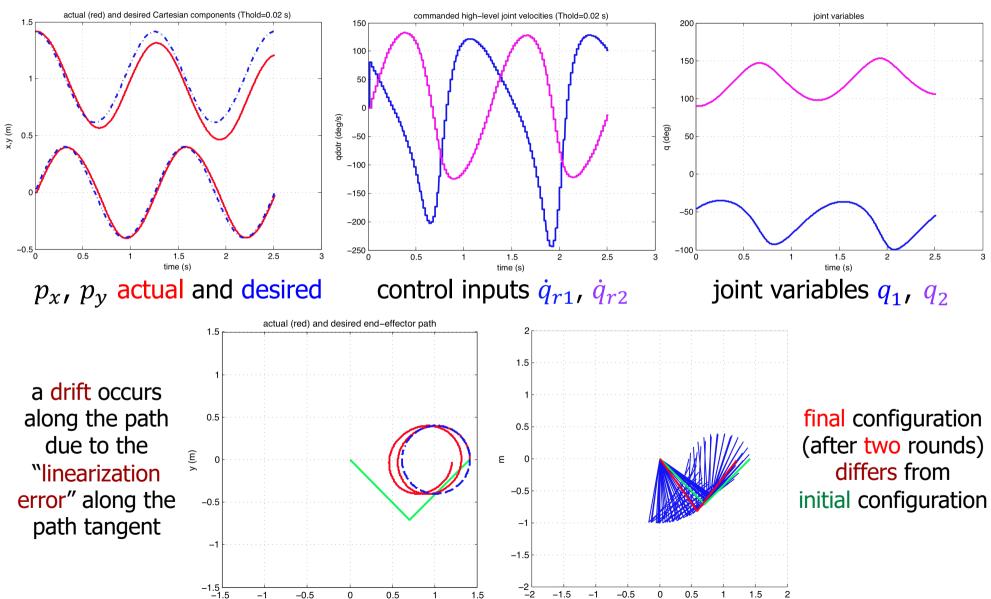
circular path: no initial error, continuous control (ideal case)



#### Results for task 2b



#### circular path: no initial error, **ZOH** at 50 Hz, **no** feedback

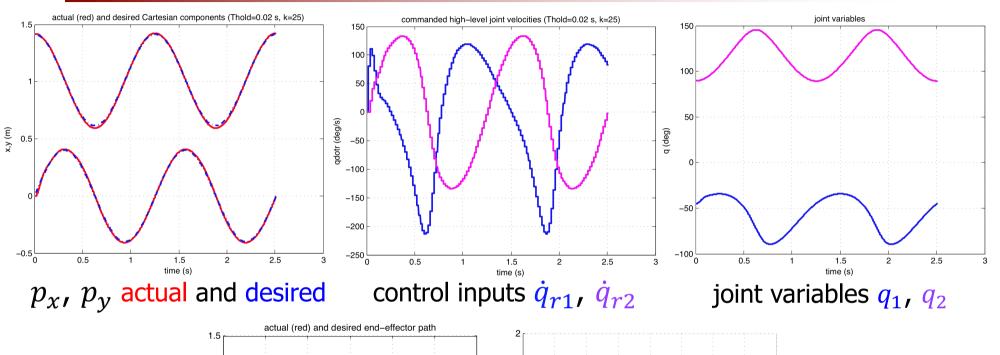


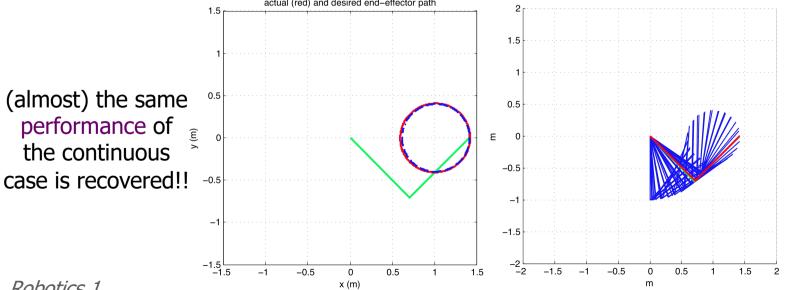
x (m)

#### Results for task 2c



circular path: no initial error, **ZOH** at 50 Hz, **with** feedback



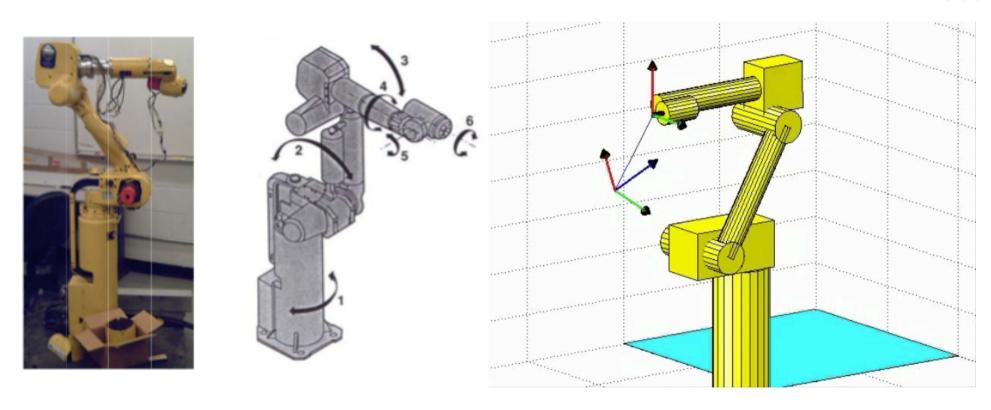


note however that larger P gains will eventually lead to unstable behavior (see: stability problems for discrete-time control systems)

#### 3D simulation



#### video



kinematic control of Cartesian motion of Fanuc 6R (Arc Mate S-5) robot simulation and visualization in Matlab

#### Kinematic control of KUKA LWR



video



# Discrete-Time Redundancy Resolution at the Velocity Level with Acceleration/Torque Optimization Properties

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September 2014

kinematic control of Cartesian motion with redundancy exploitation velocity vs. acceleration level